

Steel Joist System Reliability Report

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9 **Abstract**

10 Current steel design codes primarily adopt member-based resistance factors, which could
11 lead to overly conservative or inefficient designs for structural systems. This study investigates the
12 reliability of steel joists to develop system-based resistance factors that better reflect real structural
13 behavior. Using advanced statistical techniques, Latin hypercube sampling, and structural reliability
14 methods, the influence of various uncertainties on the performance of these systems were evaluated.
15 Sensitivity studies assess the impact of material properties, and geometric imperfections on system
16 stability. The results provide target reliability indices and system-based resistance factors, which
17 can enhance design efficiency while maintaining safety. This research is supported by collaborations
18 with the Steel Joist Institute and the Steel Deck Institute, ensuring that the findings are aligned
19 with industry needs. The proposed system-based resistance factors will contribute to the refinement
20 of design provisions in steel construction codes, offering cost-effective and structurally optimized
21 solutions. Ultimately, this study bridges the gap between theoretical reliability assessment and
22 practical engineering applications, facilitating more efficient and reliable steel structures.

23 **Contents**

24 **1 Introduction** **13**

25 **2 Input Variables** **15**

26 2.1 Material Properties 16

27 2.1.1 Cold Formed Steel Material Data 17

28 2.1.2 Hot Rolled Steel Material Data 18

29 2.2 Cross-Sectional Properties 18

30 2.2.1 HRS Angle Section Data 20

31 2.2.2 CFS Angle and Channel Section Data 22

32 2.3 Weld Lengths 25

33 2.3.1 W Webs Welds 26

34 2.3.2 W2 Webs Welds 26

35 2.3.3 Vertical Webs Welds 27

36 2.4 Material Models 27

37 2.4.1 Cold Formed Steel Material Model 30

38 2.4.2 Hot Rolled Steel Material Model 30

39 **3 Joist Models and Failure Modes** **32**

40 3.1 Joist Models with HRS Sections 32

41 3.2 Joist Models with CFS Sections 33

42 3.3 Failure Modes 33

43	3.3.1	Bottom Chord Yielding Failure	34
44	3.3.2	First Web Yielding Failure	34
45	3.3.3	First Compression Web (W3 Member) Buckling Failure	34
46	4	Finite Element Models	36
47	4.1	Shell Element Models	37
48	4.1.1	Connections	38
49	4.1.2	Loading	38
50	4.1.3	End and Lateral Supports	40
51	4.1.4	Validation of Shell Element Models	41
52	4.2	Models for Calculation of Weld Length Effects (Moment-Rotation Values)	45
53	4.3	Beam Element Models	48
54	4.3.1	Web Connections	49
55	4.3.2	Loading	49
56	4.3.3	Buckling failure models modification	50
57	4.3.4	Validation of Beam Element Models	51
58	4.4	Second Order Nonlinear Analyses Results	55
59	5	Random Value Generation and Sensitivity Study	59
60	5.1	Latin Hypercube Sampling	59
61	5.1.1	Material Properties	60
62	5.1.2	Cross-sectional Imperfections	60
63	5.1.3	Weld Length	62
64	5.2	Sensitivity Study and Sensitivity Results	67
65	5.2.1	Weld Length Sensitivity	68
66	5.2.2	Cross-sectional Imperfection Sensitivity	68

67	5.2.3	Yield Strength Sensitivity	69
68	5.2.4	Discussion	69
69	6	Simulation and Analysis Results	72
70	7	Structural Reliability Sample Framework	77
71	8	Conclusion	85
72	A	Moment-Rotation Outcome of Varying Weld Length Ratios	87
73	B	Sensitivity Study Result Figures	91
74	B.1	Nominal Value System Sensitivity Figures	91
75	B.2	Mean Value System Sensitivity Figures	97
76	B.3	Design Sheets	103

77 **List of Figures**

78	2.1	Yield stress distribution for CFS sections	17
79	2.2	Ultimate stress distribution for CFS sections	18
80	2.3	Yield stress distribution for HRS sections	19
81	2.4	Ultimate stress distribution for HRS sections	19
82	2.5	Left: HRS angle section, Middle: CFS angle section, Right:CFS channel section . .	20
83	2.6	Distributions for HRS angle leg size	21
84	2.7	Distributions for HRS angle leg thickness values	22
85	2.8	Distributions for CFS angle leg size	23
86	2.9	Distributions for CFS angle leg thickness values	23
87	2.10	Distributions for CFS channel section heel width data	24
88	2.11	Distributions for CFS channel section toe width data	24
89	2.12	Webs that are used to measure the weld length at both ends and both sides of webs . .	25
90	2.13	Distributions for W webs weld length data	26
91	2.14	Distributions for W2 web weld length data	27
92	2.15	Distributions for vertical webs weld length data	28
93	2.16	CFS Material Models (Gardner, et al. [1]))	31
94	2.17	HRS Material Models (Yun, et al. [2])	31
95	3.1	Joist with HRS sections (Joist I)	32
96	3.2	Joist with CFS sections (Joist II)	33

97	4.1	HRS angle web crimped at 6 inches at the ends	38
98	4.2	Surface to surface tie connection	39
99	4.3	Weld lines tie connection for open section web ends	39
100	4.4	Uniformly distributed loads on top chord members	39
101	4.5	Seats and end supports of joist ends	40
102	4.6	Lateral supports (orange arrows) at every panel point at bottom chords	41
103	4.7	Alternating lateral supports (orange arrows) at every 12 inches on top chords	41
104	4.8	Filler and weld elements for connection with top chord angles	42
105	4.9	Buckled W3 web member in shell element FE models for joist with 24" depth	43
106	4.10	Buckled W3 web member in shell element FE models for joist with 30" depth	43
107	4.11	Comparison of experiments and shell element FE models for joist with 24" depth	44
108	4.12	Comparison of experiments and shell element FE models for joist with 30" depth	44
109	4.13	Bottom chord tension yielding failure mode shell element FE result	46
110	4.14	First web tension yielding failure mode shell element FE result	46
111	4.15	First compression web buckling failure mode shell element FE result	46
112	4.16	Loading of shell element FE model for moment-rotation analysis for Joist II W webs	48
113	4.17	Shell element FE model result of moment-rotation analysis for Joist II W webs	48
114	4.18	Rigid links between web-chord connection locations and filler locations	49
115	4.19	Uniformly distributed loads	50
116	4.20	Shell vs beam element model load-deflection comparison with angle (a) and channel	
117		(b) sections for W3 web member	52
118	4.21	Bottom chord tension yielding failure mode beam element FE result	52
119	4.22	First web tension yielding failure mode beam element FE result	53
120	4.23	First compression web buckling failure mode beam element FE result	53

121	4.24	Shell vs beam element model load-deflection comparison with nominal (a) and mean	
122		(b) values for BC failure mode	56
123	4.25	Shell vs beam element model load-deflection comparison with nominal (a) and mean	
124		(b) values for FW failure mode	57
125	4.26	Shell vs beam element model load-deflection comparison with nominal (a) and mean	
126		(b) values for W3 failure mode	57
127	5.1	Histogram and statistical parameters of generated random HRS yield stress values . .	61
128	5.2	Histogram and statistical parameters of generated random CFS yield stress values . .	61
129	5.3	Histogram and statistical parameters of generated random HRS leg size values	62
130	5.4	Histogram and statistical parameters of generated random HRS thickness values . . .	63
131	5.5	Histogram and statistical parameters of generated random CFS leg size values	63
132	5.6	Histogram and statistical parameters of generated random CFS thickness values . . .	64
133	5.7	Histogram and statistical parameters of generated random CFS channel toe width values	64
134	5.8	Histogram and statistical parameters of generated random CFS channel heel width	
135		values	65
136	5.9	Histogram and statistical parameters of generated random W webs weld lengths values	65
137	5.10	Histogram and statistical parameters of generated random W2 webs weld lengths values	66
138	5.11	Histogram and statistical parameters of generated random vertical webs weld lengths	
139		values	66
140	5.12	Joist I BC weld length sensitivity analyses results	68
141	6.1	Joist I BC reliability analyses results and fitted distribution	73
142	6.2	Joist I FW reliability analyses results and fitted distribution	73
143	6.3	Joist I W3 reliability analyses results and fitted distribution	74
144	6.4	Joist II BC reliability analyses results and fitted distribution	74

145	6.5	Joist II FW reliability analyses results and fitted distribution	75
146	6.6	Joist II W3 reliability analyses results and fitted distribution	75
147	A.1	Moment-rotation output for different ratio levels of weld length for channel W webs .	87
148	A.2	Moment-rotation output for different ratio levels of weld length for channel W2 webs	88
149	A.3	Moment-rotation output for different ratio levels of weld length for channel vertical	
150		webs	88
151	A.4	Moment-rotation output for different ratio levels of weld length for crimped W webs .	89
152	A.5	Moment-rotation output for different ratio levels of weld length for crimped W2 webs	89
153	A.6	Moment-rotation output for different ratio levels of weld length for crimped vertical	
154		webs	90
155	B.1	Joist I BC yield strength sensitivity analyses results and fitted distribution	91
156	B.2	Joist I BC cross-sectional imperfection sensitivity analyses results and fitted distribution	92
157	B.3	Joist I FW yield strength sensitivity analyses results and fitted distribution	92
158	B.4	Joist I FW cross-sectional imperfection sensitivity analyses results and fitted distribution	93
159	B.5	Joist I W3 yield strength sensitivity analyses results and fitted distribution	93
160	B.6	Joist I W3 cross-sectional imperfection sensitivity analyses results and fitted distribution	94
161	B.7	Joist II BC yield strength sensitivity analyses results and fitted distribution	94
162	B.8	Joist II BC cross-sectional imperfection sensitivity analyses results and fitted distribution	95
163	B.9	Joist II FW yield strength sensitivity analyses results and fitted distribution	95
164	B.10	Joist II FW cross-sectional imperfection sensitivity analyses results and fitted distri-	
165		bution	96
166	B.11	Joist II W3 yield strength sensitivity analyses results and fitted distribution	96
167	B.12	Joist II W3 cross-sectional imperfection sensitivity analyses results and fitted distribution	97
168	B.13	Joist I BC yield strength sensitivity analyses results and fitted distribution	97

169	B.14 Joist I BC cross-sectional imperfection sensitivity analyses results and fitted distribution	98
170	B.15 Joist I FW yield strength sensitivity analyses results and fitted distribution	98
171	B.16 Joist I FW cross-sectional imperfection sensitivity analyses results and fitted distribution	99
172	B.17 Joist I W3 yield strength sensitivity analyses results and fitted distribution	99
173	B.18 Joist I W3 cross-sectional imperfection sensitivity analyses results and fitted distribution	100
174	B.19 Joist II BC yield strength sensitivity analyses results and fitted distribution	100
175	B.20 Joist II BC cross-sectional imperfection sensitivity analyses results and fitted distribution	101
176	B.21 Joist II FW yield strength sensitivity analyses results and fitted distribution	101
177	B.22 Joist II FW cross-sectional imperfection sensitivity analyses results and fitted distri-	
178	bution	102
179	B.23 Joist II W3 yield strength sensitivity analyses results and fitted distribution	102
180	B.24 Joist II W3 cross-sectional imperfection sensitivity analyses results and fitted distribution	122

181 **List of Tables**

182 2.1 Material grades and nominal ultimate stresses 17

183 2.2 Distribution types and calculated parameters of collected data 28

184 2.3 Theoretical mean and standard deviation values derived from the fitted probability

185 distributions 29

186 2.4 Minimum and maximum ratios for collected data 29

187 4.1 Comparison of deflection results under serviceability loads for design sheets and shell

188 element FE models 43

189 4.2 Comparison of load and midspan deflection results of experiments [3] and shell

190 element FE models 45

191 4.3 Comparison of vertical deflection at mid-span results under ultimate loads (load factor

192 1) for shell element and beam element FE models with nominal design values 54

193 4.4 Comparison of vertical deflection at mid-span results under ultimate loads (load factor

194 1) for shell element and beam element FE models with mean design values 54

195 4.5 Maximum LPF reached under ultimate loads for shell element and beam element FE

196 models with nominal design values 55

197 4.6 Maximum LPF reached under ultimate loads for shell element and beam element FE

198 models with mean design values 56

199 4.7 Comparison of failure modes in design sheets and shell element FE models results

200 under ultimate loads 58

201	5.1	Sensitivity analysis results for nominal systems	70
202	5.2	Sensitivity analysis results for mean systems	71
203	6.1	Full simulation analysis results (LPF)	76
204	6.2	Theoretical mean and standard deviation values derived from the fitted probability	
205		distributions from full simulation analysis results (LPF)	76
206	7.1	Coefficient values for each model (Nominal Capacity with SJI calculation)	82
207	7.2	Resistance Factors with varying Target Reliability Index, β_o (Nominal capacity with	
208		SJI calculation)	83
209	7.3	Coefficient values for each model (Nominal Capacity with shell element models) . . .	83
210	7.4	Resistance Factors with varying Target Reliability Index, β_o (Nominal capacity with	
211		shell element models)	84

212 **1. Introduction**

213 Steel joists are widely used in structural engineering due to their efficiency, lightweight
214 nature, and high load-carrying capacity. The design of reliable structures requires comprehensive
215 knowledge of material behavior, robust predictive models, identification of possible failure modes,
216 and rigorous reliability assessment. This study integrates finite element modeling, statistical analyses,
217 and sensitivity studies to evaluate the performance of steel joists under realistic conditions, ensuring
218 structural safety and efficient material use in high-performance applications.

219 The primary objective of this study is to establish system-based resistance factors and
220 target reliability indices that better reflect the true behavior of steel joists. Current design codes
221 predominantly rely on member-based resistance factors, which may not fully capture the interaction
222 effects, system-level dependencies and more importantly the redundancy in the systems (Galambos,
223 [4] and Hendawi, S. and Frangopol, D. M. [5]). By leveraging advanced computational models
224 and probabilistic methods, this study aims to provide insights into joist reliability and proposes
225 adjustments to design methodologies to improve structural efficiency and safety.

226 The research methodology involves stochastic input generation, finite element modeling
227 (FEM) using shell and beam elements, and nonlinear second-order analyses to accurately capture
228 failure modes. Stochastic variables for material properties, cross-section dimensions, and weld
229 lengths are generated using the Latin Hypercube Sampling method, based on collected data from
230 manufacturing plants. These randomized datasets are then used to drive finite element analyses for
231 different failure scenarios.

232 Detailed computational models (FEM) are employed to simulate stress distributions and

233 predict failure onset across the structure. Both beam and shell element models are utilized for
234 validation purposes. The study examines multiple potential failure modes, including chord and
235 web buckling, to determine the critical conditions for system integrity. A significant aspect of this
236 research is its focused investigation into the resistance (R) component of the reliability equation. To
237 demonstrate how the results of this resistance-focused analysis can be translated into engineering
238 practice, the framework of AISI S100 [6] Chapter K is employed to calculate specific resistance
239 factors (ϕ) across a range of target reliability indices (β_o). This approach not only quantifies the
240 inherent variability of the joist capacity but also provides a clear methodology for integrating these
241 probabilistic findings into standardized design procedures. By merging high-fidelity simulations
242 with stochastic calibration, this study extends conventional deterministic methods into a probabilistic
243 domain to enhance the robustness and efficiency of steel joist design.

244 **2. Input Variables**

245 In reliability analyses of structural systems, accurately characterizing input variables is
246 essential for generating realistic stochastic models. This chapter presents the statistical evaluation of
247 key input parameters used in the analyses, including material properties, cross-sectional dimensions,
248 and weld lengths. The data were collected from various sources, normalized by their nominal
249 values, and fitted to appropriate probability distributions to ensure consistency across different design
250 scenarios. The selection of the best-fit distributions was based on empirical data and statistical fitting
251 methods, with distribution parameters provided for each dataset. The following sections detail the
252 statistical distributions of material properties for cold-formed and hot-rolled steel sections, cross-
253 sectional imperfection measurements, and weld length variations, along with the rationale behind
254 their selection.

255 The figures related to data distributions in this section consist of two subplots. The upper
256 plot presents a histogram of the data along with the probability density function (PDF) of the fitted
257 distribution, while the lower plot shows the cumulative distribution function (CDF) of the data and
258 the empirical cumulative distribution function (ECDF) of the fitted distribution. The ECDF is an
259 empirical measure of this probability based on observed data points.

260 The best-fit distributions were determined for each variable, including types such as Lognor-
261 mal, Burr, Stable, and Generalized Extreme Value (GEV). Since these distributions are characterized
262 by different mathematical parameters, a unified four-column structure is used in Table 2.2 to present
263 the results consistently.

264 In this structure, the parameters are categorized based on their functional roles: the first

265 column represents Location, the second represents Scale, and the third and fourth columns provide
266 Shape 1 and Shape 2 parameters, respectively. For example, while the Lognormal distribution is
267 defined by mean (location) and standard deviation (scale), the GEV distribution includes an additional
268 shape parameter (k) in the third column. Similarly, more complex distributions like Burr or Stable
269 utilize the remaining columns to provide their specific shape or stability factors.

270 This organized approach ensures that all probabilistic inputs are clearly documented re-
271 gardless of their distribution type. Table 2.2 provides the complete list of fitted parameters, while
272 Table 2.4 summarizes the minimum and maximum ratios observed in the data after filtration. Fur-
273 thermore, Table 2.3 presents the equivalent mean and standard deviation values derived from these
274 distributions. These values are provided to facilitate a direct comparison with conventional structural
275 design assumptions and to offer a simplified statistical overview of the data's central tendency and
276 dispersion, even when the underlying distribution is non-Gaussian.

277 **2.1. Material Properties**

278 Joists are manufactured using Cold Formed Steel (CFS) and Hot Rolled Steel (HRS)
279 sections. Tensile test results conducted by SJI member companies' plants for both HRS and CFS
280 were randomly collected, analyzed, and fitted to distributions for random variable input generation.
281 A nominal yield strength of 50 ksi was assumed for design purposes in the SJI joist designs; therefore,
282 tensile test results for 50 ksi sections were specifically collected from SJI member companies. Despite
283 focusing on 50 ksi material, the dataset includes various grades of both CFS and HRS sections, with
284 their nominal ultimate stresses provided in Table 2.1. The ratios of measured values to nominal values
285 for both yield stress and ultimate stresses were calculated.

Table 2.1: Material grades and nominal ultimate stresses

	CFS		HRS			
Grade	A1018	A1011	A529- A529NM	A572	A992	A500
F_u (ksi)	65	65	70	65	58	65

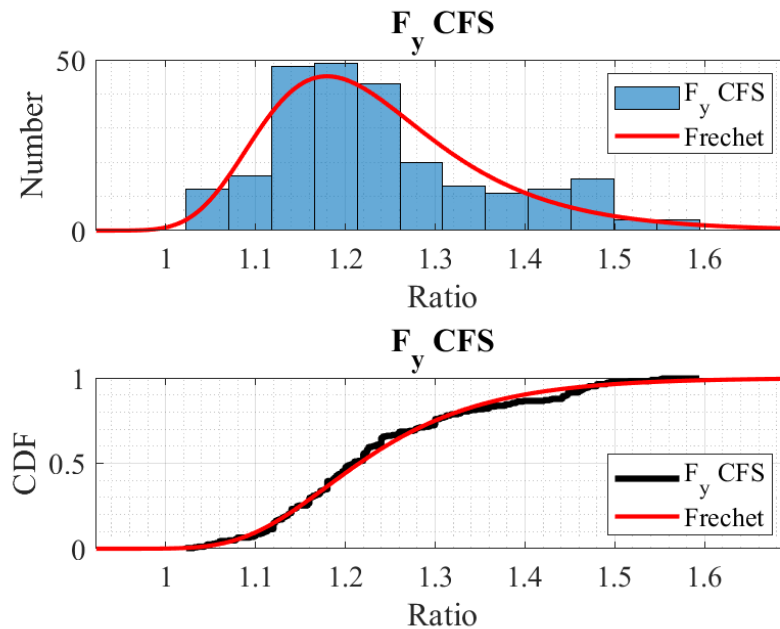


Figure 2.1: Yield stress distribution for CFS sections

286 2.1.1 Cold Formed Steel Material Data

287 The combined tensile test data, collected from different manufacturers, consists of 265
 288 tensile test results. Figure 2.1 shows the histogram and best fit distribution of the collected data for
 289 CFS sections tensile test yield strength results. While there is a high dispersion in the collected data, a
 290 clear distribution fitting was achieved despite a small data concentration of data between ratios of 1.4
 291 and 1.5. The best fit was obtained using Frechet distribution. Also Figure 2.2 shows the histogram
 292 and best fit distributions for ultimate stress data.

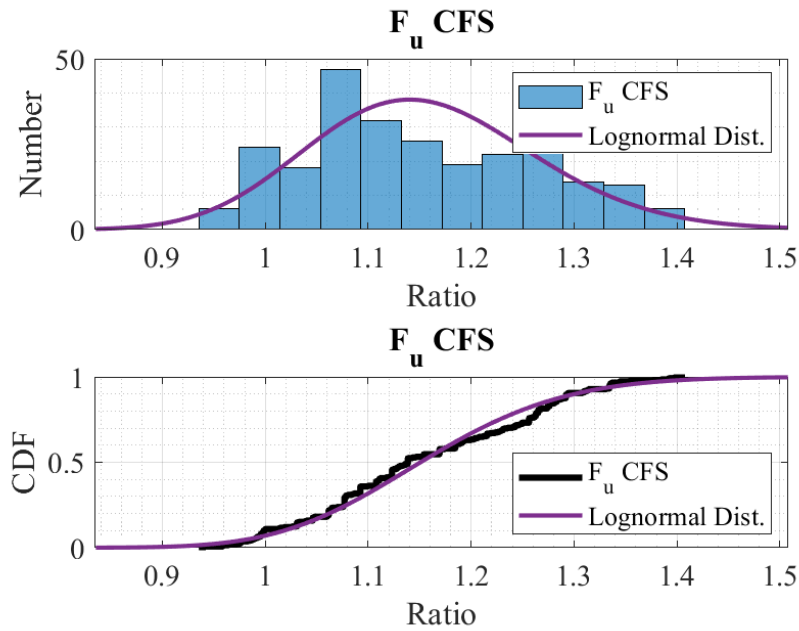


Figure 2.2: Ultimate stress distribution for CFS sections

293 2.1.2 Hot Rolled Steel Material Data

294 Figure 2.3 shows the distribution of 389 HRS tensile test data for yield strength. Compared
 295 to CFS material, the mean and the dispersion are smaller, and the Burr distribution was determined
 296 as the best fit for the collected data. The histogram and the best fit distribution for ultimate stress data
 297 is provided in Figure 2.4.

298 2.2. Cross-Sectional Properties

299 Hot-rolled steel (HRS) and cold-formed steel (CFS) angle and channel sections were ran-
 300 domly selected to generate cross-sectional imperfection data. SJI member companies collected
 301 cross-sectional measurements in varying quantities for the specified section types (HRS angle, CFS

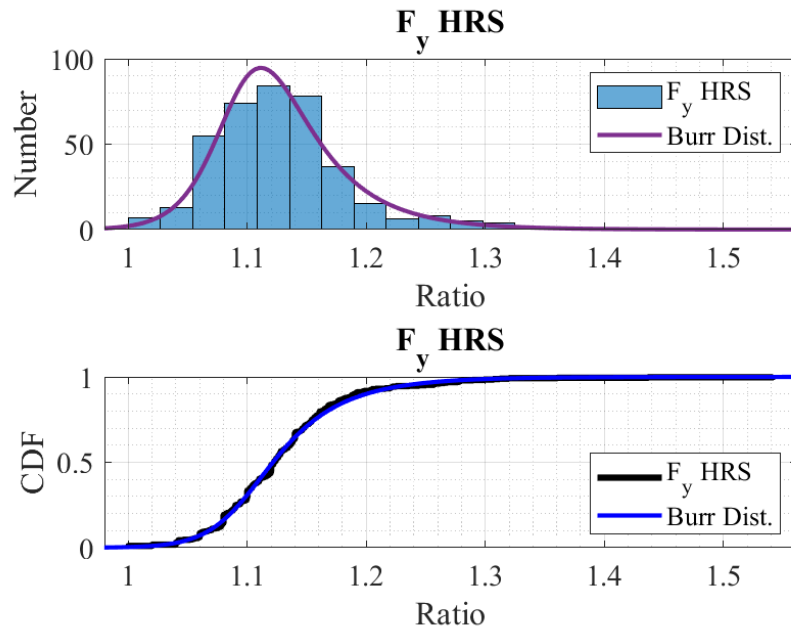


Figure 2.3: Yield stress distribution for HRS sections

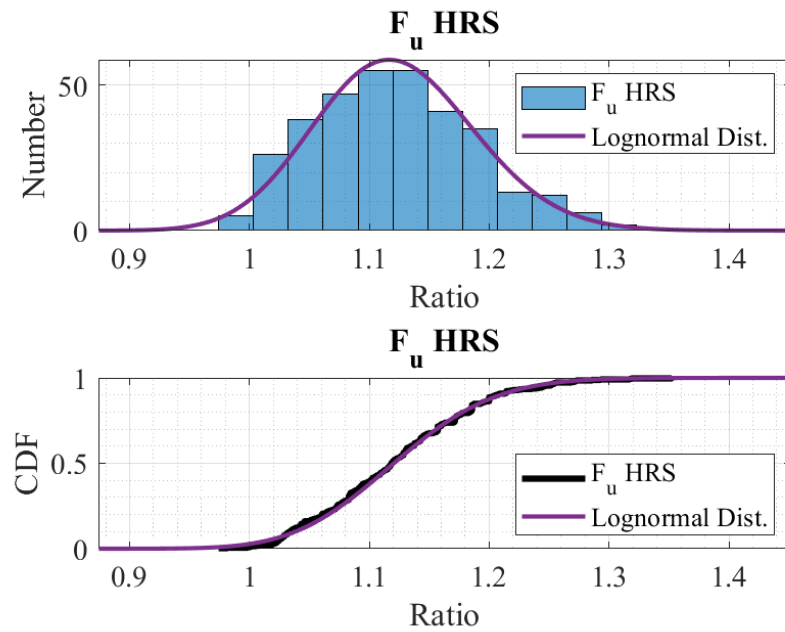


Figure 2.4: Ultimate stress distribution for HRS sections

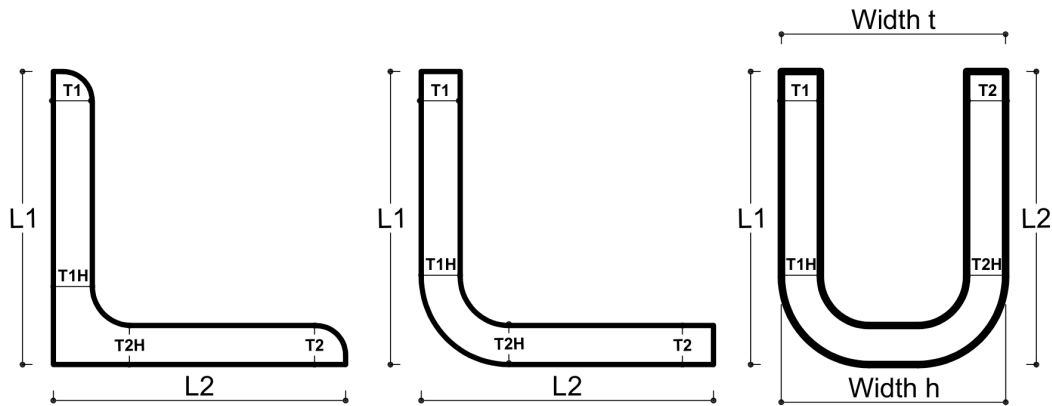


Figure 2.5: Left: HRS angle section, Middle: CFS angle section, Right:CFS channel section

302 angle, and CFS channel), as illustrated in Figure 2.5.

303 For angle sections, there are four thickness measurements per section which are from both
 304 heel (T1H and T2H) and toe (T1 and T2) ends of each leg, along with two leg length measurements
 305 (L1 and L2). For channel sections, toe and heel widths were measured (Width t and Width h,
 306 respectively), whereas for angle sections, the forming angle between legs was recorded to evaluate
 307 forming performance and accurately model the sections. To eliminate sectional differences, the
 308 same normalization method is used for cross-sectional imperfections, with lengths and thicknesses
 309 normalized by their nominal values.

310 2.2.1 HRS Angle Section Data

311 HRS sections are expected to have high consistency in cross-sectional dimensions due to
 312 the manufacturing methods. This high consistency creates additional challenges for distribution
 313 fitting due to very small margins or high repetitions in the data. An example to this is the forming
 314 angle between legs of HRS angle sections predominantly includes data between 89.5 to 90.5, with
 315 the majority of measurements being 90 degrees. Consequently, it was not feasible to generate a
 316 distribution fitting for that specific data.

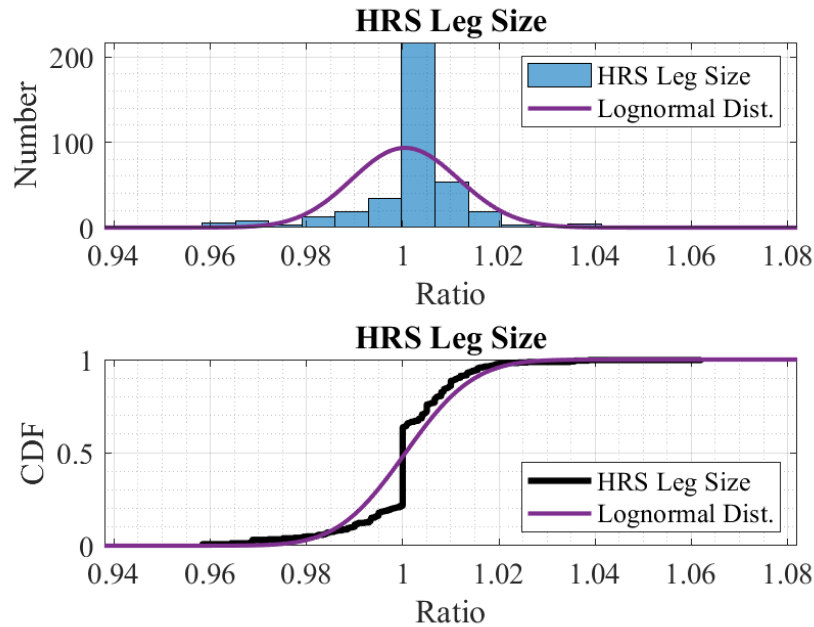


Figure 2.6: Distributions for HRS angle leg size

317 Another challenging dataset is the HRS angle leg sizes. While the variations are slightly
 318 larger than those observed in the forming angles, a significant portion of the data has a ratio of 1,
 319 creating a distinct peak at this value, as illustrated in Figure 2.6. Despite the challenges, the lognormal
 320 distribution was determined to be the best representation of the data.

321 The HRS thickness data, on the other hand, shows a clear distribution and a high concen-
 322 tration around the ratio of 1, as expected. Although using high degree functions in distribution fitting
 323 can lead to overfitting problem, this study relies on actual data collected from joist plants, making
 324 such functions applicable for a more accurate fit. In this case, the Stable distribution was selected as
 325 the best fit for HRS thickness data as shown in Figure 2.7.

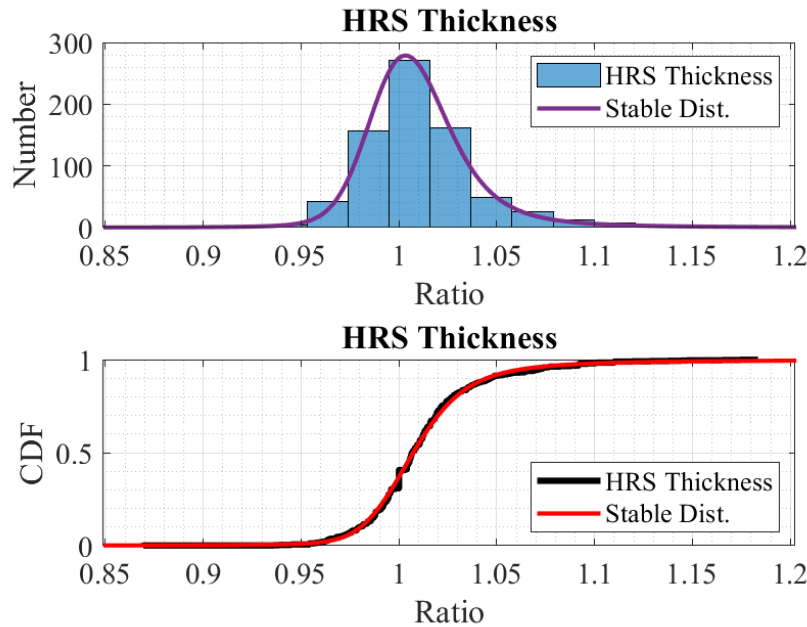


Figure 2.7: Distributions for HRS angle leg thickness values

326 2.2.2 CFS Angle and Channel Section Data

327 Measurements were completed for both CFS channel and angle sections in SJI manufactur-
 328 ing plants. Given that the forming of both section types are made by steel sheets, the thickness and
 329 leg size data showed similar distributions. Therefore, rather than applying separate distributions for
 330 thickness and leg size inputs, the data for each dimension was combined into two groups: CFS leg
 331 sizes and CFS thicknesses. The same distributions were used for both channel and angle sections.
 332 Both leg size and thickness histograms and fitted distributions are given in Figures 2.8 and 2.9.

333 CFS angle forming angle data shows similarity to HRS angle section forming angle data,
 334 making distribution fitting unfeasible. However, forming of CFS channel sections were included in
 335 analyses by including different width values for toe and heel ends of channels. Different distributions
 336 were applied to heel and toe widths, and channel cross-sections were generated based on these
 337 distributions at each step of the analysis.

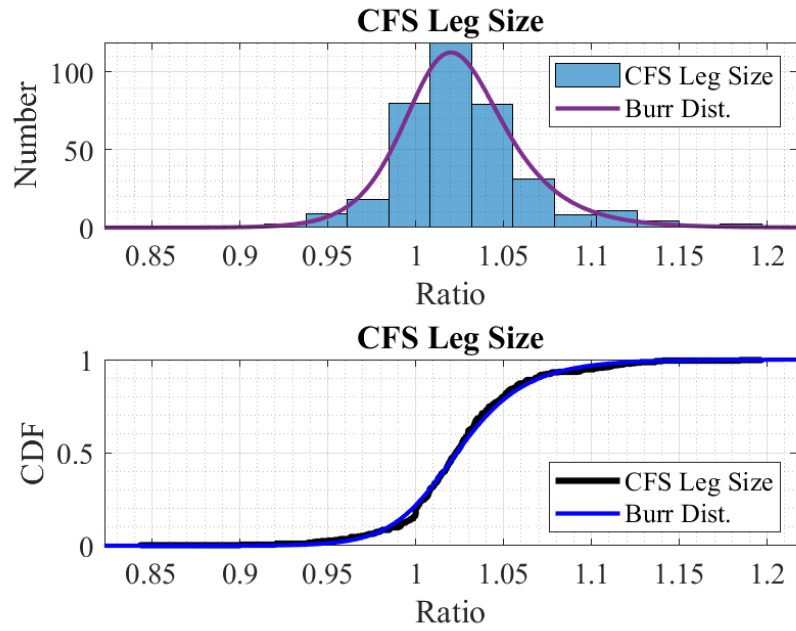


Figure 2.8: Distributions for CFS angle leg size

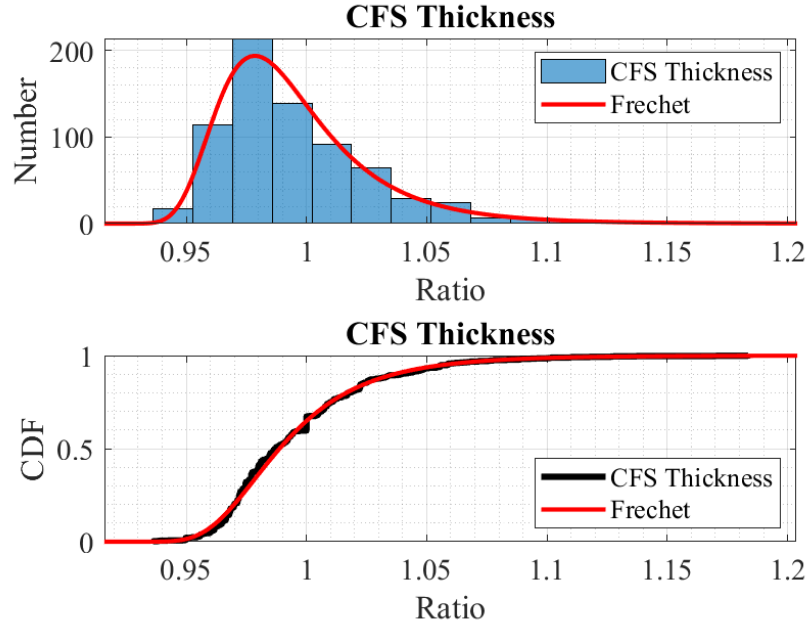


Figure 2.9: Distributions for CFS angle leg thickness values

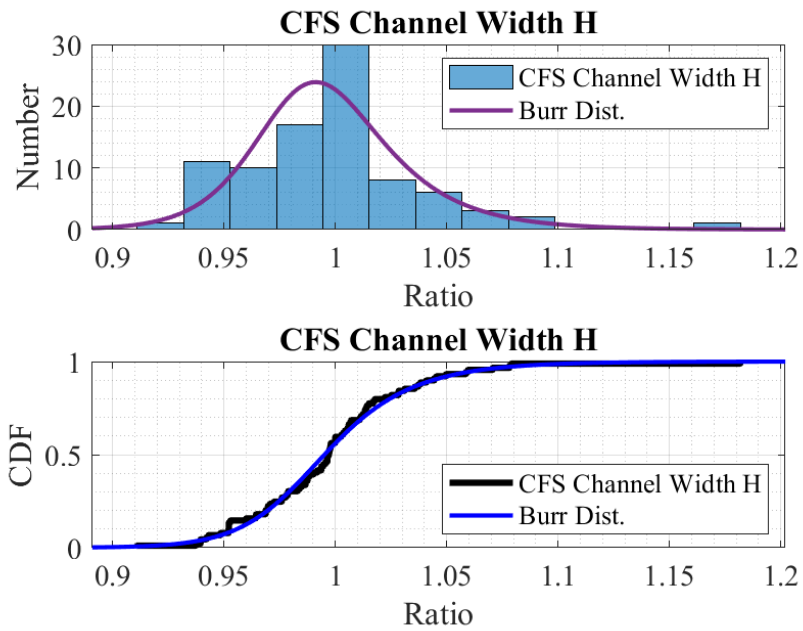


Figure 2.10: Distributions for CFS channel section heel width data

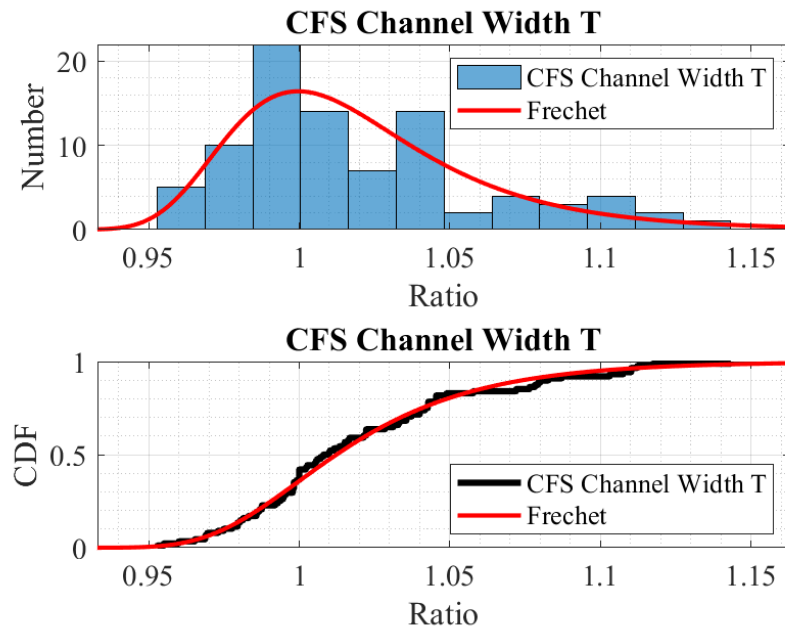


Figure 2.11: Distributions for CFS channel section toe width data

338 2.3. Weld Lengths

339 Another selected variable for random inputs is web weld lengths. The first six webs were
340 considered, and weld lengths were measured from both sides of joists and both ends of the webs (top
341 and bottom chord ends). Locations and names of the selected webs are shown in Figure 2.12. A
342 filtration was applied to data to eliminate misentered inputs. The limits for this filtration was defined
343 as 0.5 to 4 in ratios.

344 Weld lengths differentiates at every joist designs and at every web member. Ratio of mea-
345 sured weld lengths to the nominal weld length were used to eliminate these differences between
346 different joist designs. After analyzing each web separately and generating their respective distribu-
347 tions, similar web weld length data were grouped together, reducing the total number of categories
348 from six to three. The final groupings are as follows:

- 349 • W webs group (Combined data from W3, W4 and W5 web weld length data),
- 350 • W2 webs group (only the data includes the first webs),
- 351 • Vertical webs group (D2 and V1 webs).

352 The Frechet distribution was determined to be the best fit for each of these groups. More
353 details, including distribution parameters and visualizations, are provided in this section.

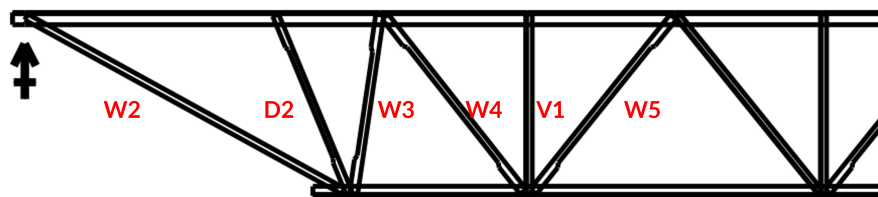


Figure 2.12: Webs that are used to measure the weld length at both ends and both sides of webs

354 **2.3.1 W Webs Welds**

355 This weld length data is a combined data coming from three different webs; W3, W4 and W5
356 webs. While the distribution fitting provides a single representation of these weld lengths, separately
357 generated ratios were applied to each web in the analyses, ensuring independent random values for
358 each case (uncorrelated).

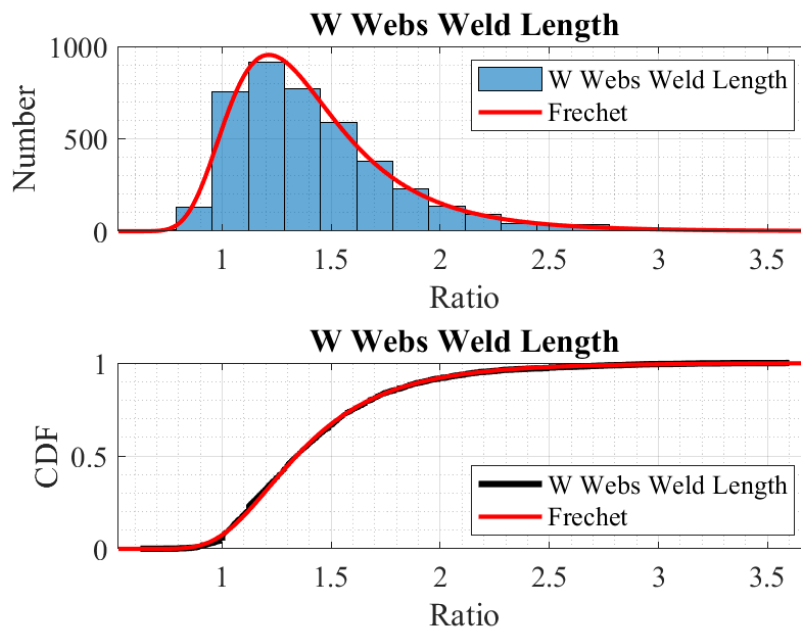


Figure 2.13: Distributions for W webs weld length data

359 **2.3.2 W2 Webs Welds**

360 The first web weld length data was analyzed separately from other web groups due to its
361 distinct distribution and the importance of the first web given that one of the failure mode specifically
362 focused on this member. The range is similar to the vertical web group but it is considerably larger
363 than the W webs group.

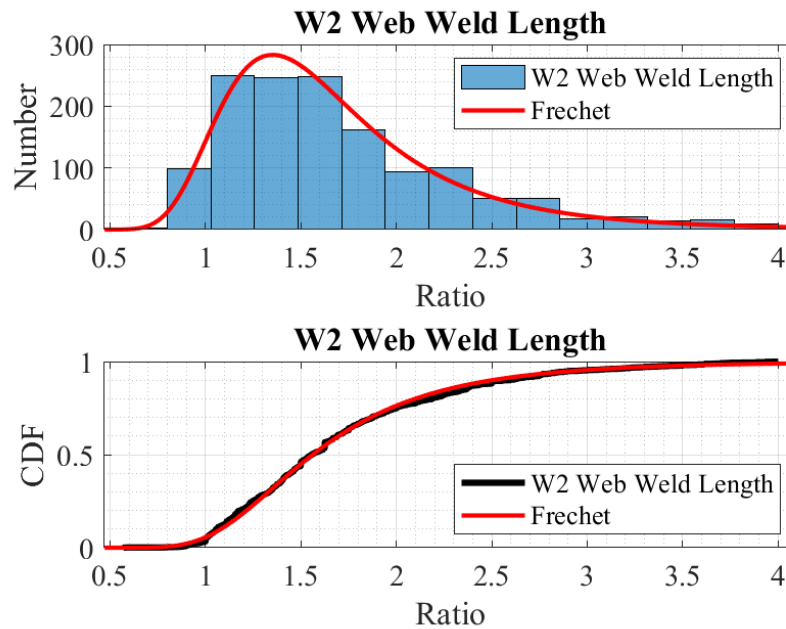


Figure 2.14: Distributions for W2 web weld length data

364 2.3.3 Vertical Webs Welds

365 The vertical webs group is the combination of weld length data from D2 and V1 webs.
 366 This group has the widest range among all web categories and has the highest mean ratio value. Its
 367 variability is greater compared to the W and W2 web groups, requiring a distinct distribution fitting
 368 for accurate representation in the analyses.

369 2.4. Material Models

370 In previous studies, it has been shown that CFS and HRS sections exhibit different material
 371 behaviors. Since nonlinear second-order analysis was used in this study, the nonlinear behavior
 372 of these sections were explicitly defined in ABAQUS. Models were generated based on the given

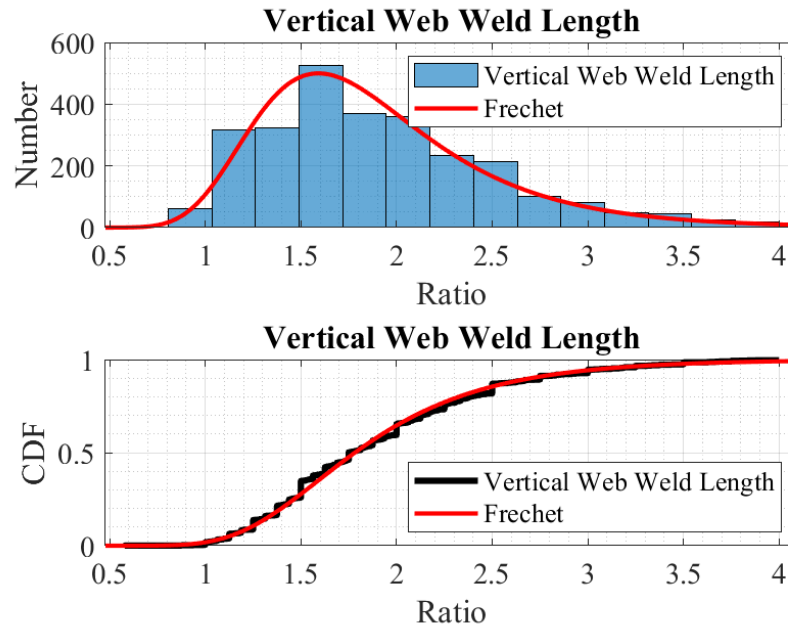


Figure 2.15: Distributions for vertical webs weld length data

Table 2.2: Distribution types and calculated parameters of collected data

Collected Data	Distribution Type	Location / Mean (μ)	Scale / St. Dev. (σ)	Shape 1	Shape 2	# of Data
HRS Yield Stress	Burr	-	1.098	52.059	0.497	389
CFS Yield Stress	Frechet	1.181	0.095	0.011	-	265
HRS Ult. Stress	Lognormal	0.114	0.059	-	-	389
CFS Ult. Stress	Lognormal	0.140	0.096	-	-	265
HRS Leg Size	Lognormal	0.0006	0.011	-	-	377
HRS Thickness	Stable	1.584	0.675	0.016	1.005	740
CFS Leg Size	Burr	-	1.015	60.029	0.711	365
CFS Thickness	Frechet	0.980	0.023	0.089	-	717
CFS Ch. Heel W.	Burr	-	0.985	58.576	0.675	89
CFS Ch. Toe W.	Frechet	1.0008	0.031	0.038	-	88
W Webs WL	Frechet	1.241	0.267	0.106	-	4163
W2 Webs WL	Frechet	1.407	0.414	0.141	-	1380
Vert. Webs WL	Frechet	1.613	0.458	0.048	-	2725

Abbreviations: Ult: Ultimate, WL: Weld Length, W: Width

Table 2.3: Theoretical mean and standard deviation values derived from the fitted probability distributions

Collected Data	Distribution Type	Mean	Standard Deviation	Number of Data
HRS Yield Stress	Burr Dist.	1.129	0.173	389
CFS Yield Stress	Frechet Dist.	1.237	0.124	265
HRS Ultimate Stress	Lognormal Dist.	1.122	0.067	389
CFS Ultimate Stress	Lognormal Dist.	1.156	0.111	265
HRS Leg Size	Lognormal Dist.	1.001	0.011	377
HRS Thickness	Stable Dist.	1.005	-	740
CFS Leg Size	Burr Dist.	1.015	0.142	365
CFS Thickness	Frechet Dist.	0.980	0.033	717
CFS Ch. Heel Width	Burr Dist.	0.985	0.141	89
CFS Ch. Toe Width	Frechet Dist.	1.020	0.042	88
W Webs Weld Length	Frechet Dist.	1.427	0.402	4163
W2 Webs Weld Length	Frechet Dist.	1.712	0.666	1380
Vert. Webs Weld Length	Frechet Dist.	1.900	0.629	2725

Table 2.4: Minimum and maximum ratios for collected data

Collected Data	Minimum Ratio	Maximum Ratio
HRS Yield Stress	1.000	1.542
CFS Yield Stress	1.023	1.594
HRS Ultimate Stress	0.974	1.352
CFS Ultimate Stress	0.935	1.408
HRS Leg Size	0.958	1.062
HRS Thickness	0.869	1.184
CFS Leg Size	0.844	1.197
CFS Thickness	0.936	1.184
CFS Ch. Heel Width	0.911	1.182
CFS Ch. Toe Width	0.953	1.143
W Webs Weld Length	0.625	3.600
W2 Webs Weld Length	0.571	4.000
Vert. Webs Weld Length	0.578	4.000

373 formulations in literature for preferred material models and updated by using randomly generated
 374 yield and ultimate stresses at every analysis. Consequently, each analysis featured different material

375 models for each chord and each web member according to the section type. It should also be noted
376 that the members with same sections have the same material properties in each model (they are
377 correlated) since that the same sections are most likely be coming from the same batch.

378 The nominal modulus of elasticity values were set as 29,000 ksi for HRS materials ([7]) and
379 29,500 ksi for CFS materials [6]. Additionally, since ABAQUS uses true stress - true strain behavior,
380 the created material models were also converted to the true stress - true strain values before starting
381 the analysis.

382 Material models allow modifying the F_y and F_u values along with the E value. These
383 models then calculate the strains and the predictive model curvatures according to the formulas that
384 were created by using the experimental background used in these studies.

385 **2.4.1 Cold Formed Steel Material Model**

386 The material model for CFS sections was taken from study of Gardner, et al. [1] and a plot
387 for 50 ksi material with $E=29,500$ is given in Figure 2.16.

388 **2.4.2 Hot Rolled Steel Material Model**

389 HRS sections material models is different than the CFS section materials as mentioned
390 before. The biggest difference is that this model has a clear yield plateau before the strain hardening
391 starts. This model was taken from study of Yun, et al. [2] and a plot for 50 ksi material with $E=29,000$
392 is given in Figure 2.17.

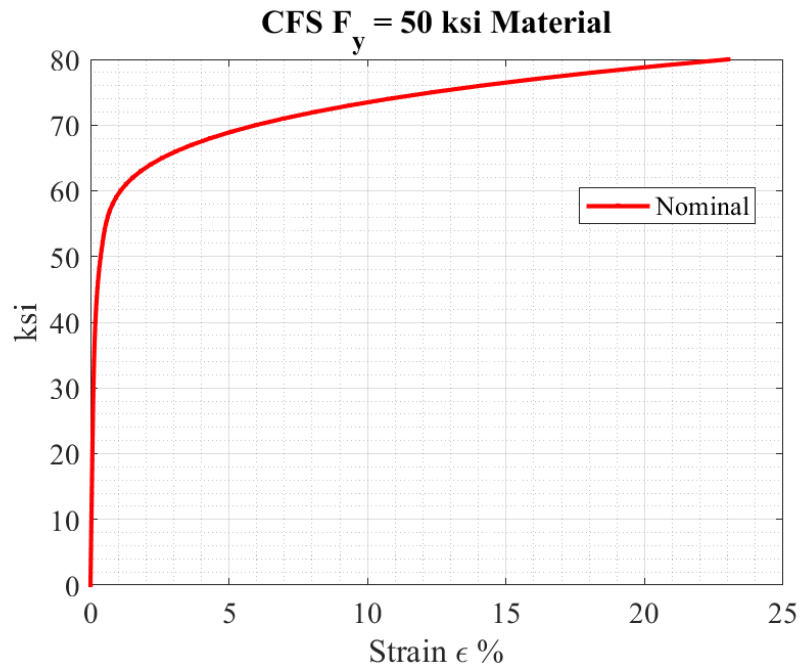


Figure 2.16: CFS Material Models (Gardner, et al. [1])

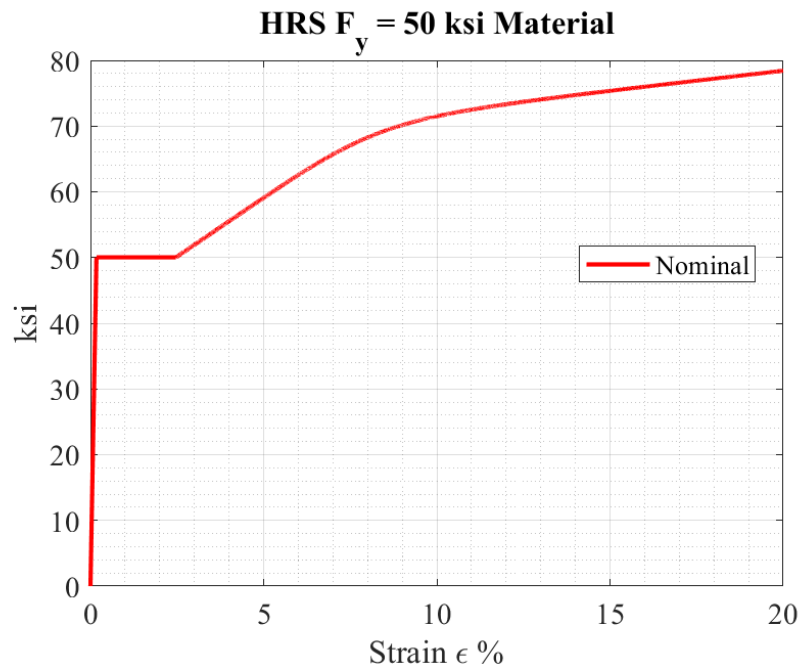


Figure 2.17: HRS Material Models (Yun, et al. [2])

393 **3. Joist Models and Failure Modes**

394 Two different joist designs, both with a 50 ft span and 30-inch deep, were used in this study.
395 Each design corresponds to a different section type: hot-rolled steel (HRS) and cold-formed steel
396 (CFS). These core designs were specifically selected and developed by the SJI Research Committee
397 to ensure they represent current industry practices and were subsequently provided for use in this
398 research; the design-sheets for these models are provided in the Appendix B.3. These core designs
399 were further modified to have three different failure modes, leading to variations in ultimate load
400 capacities in each designs and failure modes.

401 **3.1. Joist Models with HRS Sections**

402 A generic shape of first joist design (Joist I) is provided in Figure 3.1. The Joist I has rod
403 sections as first webs, and uses crimped angle sections for web members. These angle web members
404 are crimped 6 inches from their ends to fit between the chord angles.

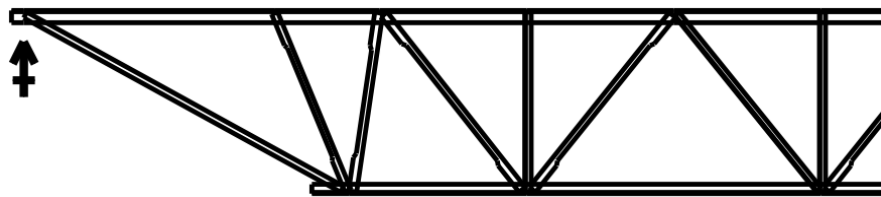


Figure 3.1: Joist with HRS sections (Joist I)

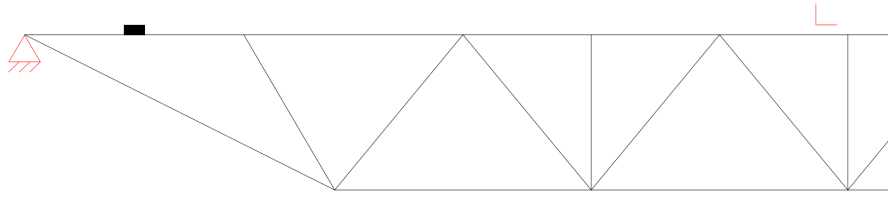


Figure 3.2: Joist with CFS sections (Joist II)

405 3.2. Joist Models with CFS Sections

406 Joist with CFS sections (Joist II) uses channel sections for all webs and uses CFS angles for
407 chord members (Figure 3.2).

408 3.3. Failure Modes

409 Three primary failure modes were selected for further investigation for each joist design:

- 410 • Bottom Chord Yielding Failure
- 411 • First Web Yielding Failure
- 412 • Compression Web (W3 Member) Buckling Failure

413 Additionally, a serviceability limit state was considered based on the $L/60$ deflection limit,
414 based on discussions with SJI research committee representatives. Although the International Build-
415 ing Code (IBC, [8]) typically defines the serviceability limit as $L/120$ for similar structural members,
416 the SJI representatives recommended adopting twice this deflection ($L/60$) as the threshold for
417 these analyses to better capture the ultimate behavior and extensive deformation capacity of the joist
418 systems. Given the 600-inch span length, a 10-inch deflection limit was applied to all models.

419 **3.3.1 Bottom Chord Yielding Failure**

420 Yielding first initiates in the bottom chord, specifically around the midspan of the joist. As
421 the load and deflection increase, this yielding spreads from the midspan toward the ends of the bottom
422 chord. This increase in tension stresses also causes higher stress levels and yielding in the first web
423 members. Due to the ductility of steel, this process results in significantly larger maximum deflections
424 compared to other failure modes. Consequently, this is the failure mode that most frequently reaches
425 the 10-inch deflection limit.

426 **3.3.2 First Web Yielding Failure**

427 In the second yielding failure mode, first web members with weaker cross-sections expe-
428 rience high yielding, specifically at both ends where rotational forces develop due to the deflected
429 shape of the joist. As the first webs yield due to the deflected shape, high stresses are also induced in
430 the bottom chord.

431 An important outcome of weakened first webs is the reduced rotational stiffness of the
432 modified webs, which increases the likelihood of top chord buckling at the end panels. This failure
433 mode is the second most frequent mode that can reach to 10 inches of deflection limit since there is a
434 high stresses on both bottom chord and first webs.

435 **3.3.3 First Compression Web (W3 Member) Buckling Failure**

436 W3 web members are the first compression webs under gravity loads. As the load and
437 deflection increase, bending and high-stress regions start to form at the ends of the W3 members
438 due to their weakness. As the deflected shape progresses, these end rotations also cause additional
439 stress at the ends of the W2 end webs. However, the bending in W3 results in failure due to buckling
440 before the yielding reaches to the failure in W2 members or midspan deflections reach the $L/60$

441 limit. Because of this relatively early buckling, the overall deflections are smaller for this failure
442 mode compared to others. Since compression buckling is the primary failure mode, imperfections or
443 notional loads have a high impact on the accuracy of the analysis results.

444 Both implementing initial imperfections or notional loads to the system increase the analysis
445 accuracy. Both methods can be affected by the material properties and cross-sectional properties.
446 Since the initial imperfection method requires additional analysis to determine and utilize in the
447 ABAQUS models, to increase the efficiency, this model includes notional loads on the midpoint of
448 W3 web members. These notional loads were calculated using Eq. 3.1:

$$\text{Notional Load} = N = 0.002F_y A \quad (3.1)$$

449 where F_y is the yield stress of W3 web material, and A is the area of W3 web section. Since
450 F_y and A change at each random realization, the notional loads were updated accordingly to maintain
451 consistency with the assigned input values.

452 **4. Finite Element Models**

453 All failure mode designs for both Joist I and Joist II models were first modeled with shell
454 elements and solid elements (rod and filler sections) as this is the most accurate analysis type. Next,
455 new finite element models were created using beam elements as they have significantly reduced run
456 time compared to shell element models. Nonlinear second-order RIKS analyses were completed in
457 ABAQUS. Loads, lateral and end supports, connections, and material models are presented in this
458 chapter for the FE models.

459 Most of the modeling procedures used in developing the Abaqus shell-element models
460 were adapted from previously validated studies with proven consistency (Sippel, Ziemian, and Blum
461 [9], Rahnavard et al. [10], Adany and Schafer [11], Kapoor, Bogh and Peterman, [12] and Sippel,
462 Ziemian, and Blum [13]). The methods for representing welded connections, end supports, and
463 lateral restraints were primarily derived from earlier work (Sippel, Ziemian, and Blum [9]), with
464 project-specific modifications developed in coordination with the SJI Research Committee. Crimped
465 sections and filler components were also replicated following the approaches reported in previous
466 studies. Material modeling was enhanced by replacing earlier simplified assumptions with more
467 detailed nonlinear material definitions. For shell elements, the S4R element—widely recommended
468 and used in the literature (Rahnavard et al. [10], Adany and Schafer [11], and Kapoor, Bogh and
469 Peterman, [12])—was adopted, and mesh sizes were selected following guidance from prior research
470 (Sippel, Ziemian, and Blum [13]), with additional refinement applied to compression members to
471 ensure accurate representation of localized buckling behavior.

472 Shell models were verified by comparing the load-deflection results of FE models and

473 designs sheets provided by SJI at the service load levels. After the verification at the service load
474 levels, the design loads were applied to the system with RIKS analysis to obtain the actual capacity
475 of the designed joists for the following steps in the project.

476 Given that the reliability study requires high number of analyses, running shell elements
477 would require excessive amount of time to run all possible design combinations. Therefore, beam
478 element finite element models were used for the reliability study. Same material models, loads, and
479 lateral and end supports were used in both models. The connections, however, were modeled with a
480 different method for the beam FEM compared to the shell FE models.

481 Beam element models are not able to include the change in the weld length effectively.
482 Therefore, rather than using rigid connection at the web end - chord connections, rotational springs
483 with specific stiffness values for web groups were assigned to web ends. The method for spring
484 stiffness calculations for varying weld lengths is explained this section. After the models were
485 created, beam element FE models were verified by comparing the load-deflection results at service
486 level with SJI design sheets and at design load level with shell element FE model results.

487 **4.1. Shell Element Models**

488 Shell element FE models were created first due to their accurate and realistic results.
489 Detailed 3D models were created for each failure mode design. Previously mentioned material
490 models were used, welded connections were modeled according to the given length in the provided
491 design sheets with the given loads on top chords, and the supports were applied as in the actual joists.

492 HRS angle web members were crimped starting from 6 inches at the ends and these
493 crimpings were also modeled in shell element models in ABAQUS with a transition region from
494 regular angle to crimped angle sections, as illustrated in Figure 4.1.

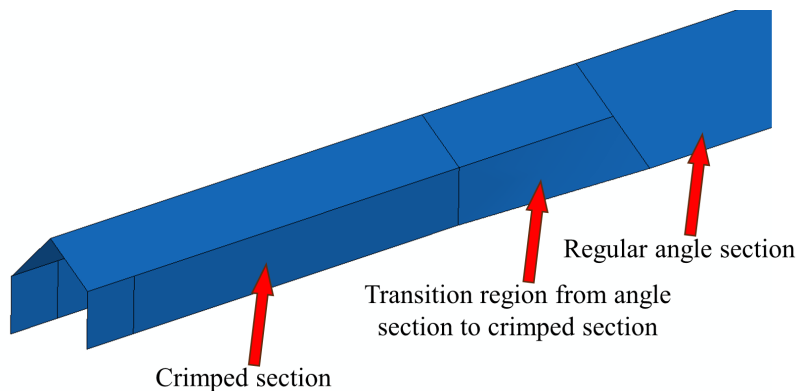


Figure 4.1: HRS angle web crimped at 6 inches at the ends

495 **4.1.1 Connections**

496 There were two types of connections used in shell element FE models for these two different
 497 weld types (bevel and fillet). The first connection type is surface to surface tie connection which was
 498 used in bevel welds (connections between solid element welds and chords). An example from rod end
 499 for this type of connections is shown in Figure 4.2. Additional weld elements with a different weld
 500 material with a yield stress of 75 ksi was used in this connection type. The second type connection
 501 is the welded connection between shell element webs and shell element chord members which was
 502 done by using only the edges of the web members to represent the fillet welds, presented in Figure
 503 4.3.

504 **4.1.2 Loading**

505 Loads were applied as uniformly distributed surface loads to the top chord angles. Since
 506 [13] demonstrated the significant effects of torsional stiffness on top chord members in joist elements,
 507 the inner sides of the top chord angles were specifically chosen for load application. This approach
 508 was preferred to prevent generating additional torsional forces on the top chord angles. Figure 4.4
 509 shows the loading configuration on the top chords.

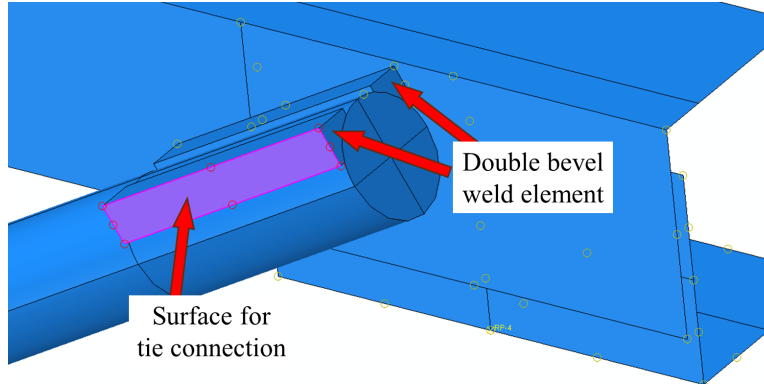


Figure 4.2: Surface to surface tie connection

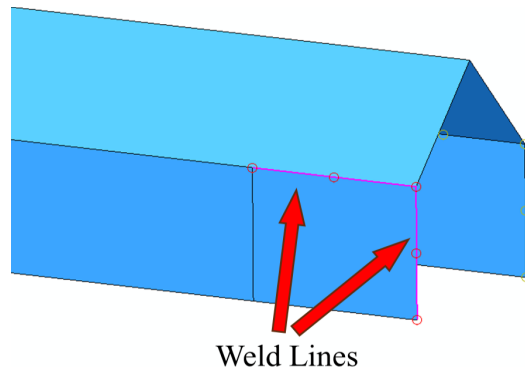


Figure 4.3: Weld lines tie connection for open section web ends

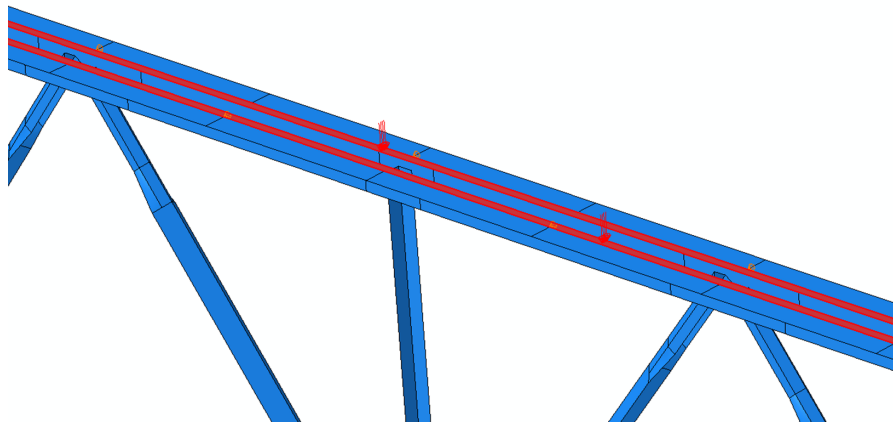


Figure 4.4: Uniformly distributed loads on top chord members

510 **4.1.3 End and Lateral Supports**

511 End supports were modeled in the same way with simply supported beams, a pinned
512 connection on one end and a roller connection on the other end. However, the supports were not
513 directly applied to the top chord angles but to seats angles. Seats were added to both ends and
514 connected to the top chord angles on both sides to transfer the forces to the supports from top chords.

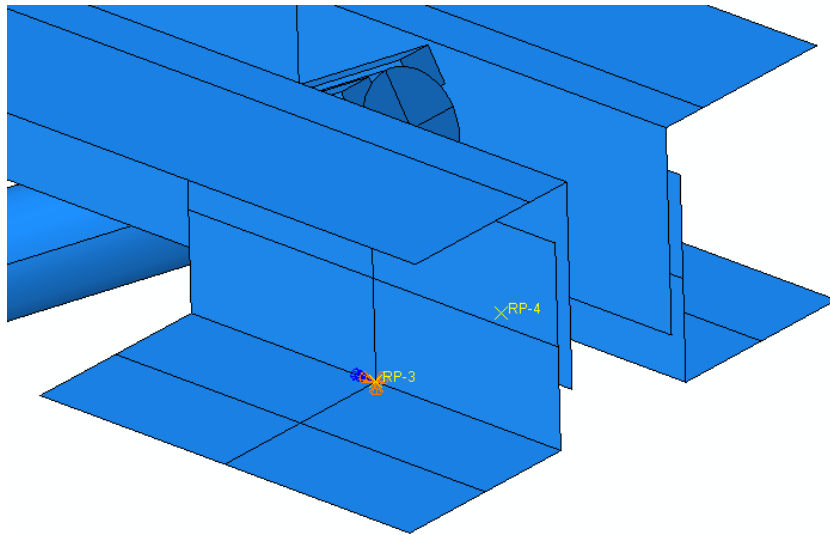


Figure 4.5: Seats and end supports of joist ends

515 Lateral supports were applied to the joist models in the same way with actual joists on both
516 chords. Bottom chords were laterally supported at every panel point. Additional angle members were
517 connected to the bottom chord members and the supports were applied to these members. Figure 4.6
518 includes an example to this lateral support type with the additional angle support member. A different
519 method was used for top chord lateral supports. The supports were applied to the top chord angles
520 directly alternating at every 12 inches to represent the connection between chord angles and deck on
521 top, as the deck provides lateral restraint to the top chord.

522 In addition to lateral supports, fillers were used to prevent buckling of top chord members
523 in steel joists, and were also included in FE models. The same sections with solid rod members were

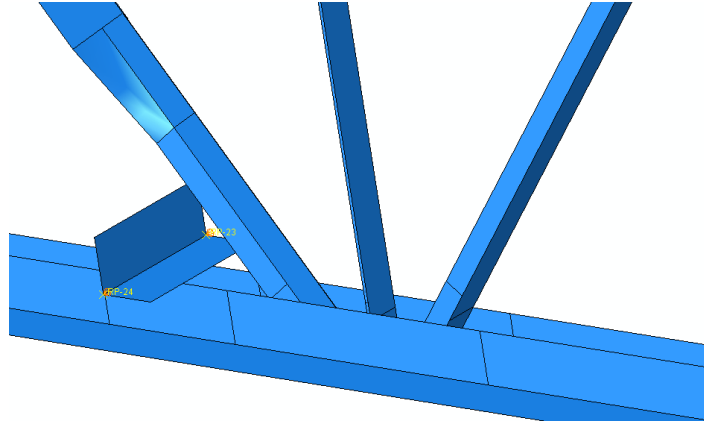


Figure 4.6: Lateral supports (orange arrows) at every panel point at bottom chords

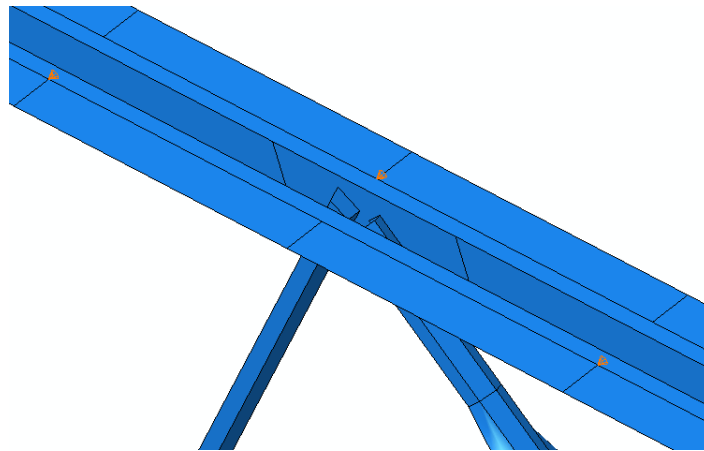


Figure 4.7: Alternating lateral supports (orange arrows) at every 12 inches on top chords

524 placed in the designated locations and welded connections were modeled.

525 **4.1.4 Validation of Shell Element Models**

526 Two different validation processes were completed to verify the shell element FE models.
527 In the first validation, the shell element finite element (FE) model results were compared to the Steel
528 Joist Institute (SJI) calculated displacements under serviceability loads. The reference values in Table
529 4.2 were provided by SJI designs; following the completion of the FE models, the vertical deflections
530 under serviceability loads were compared against these reference values. The minimal percentage

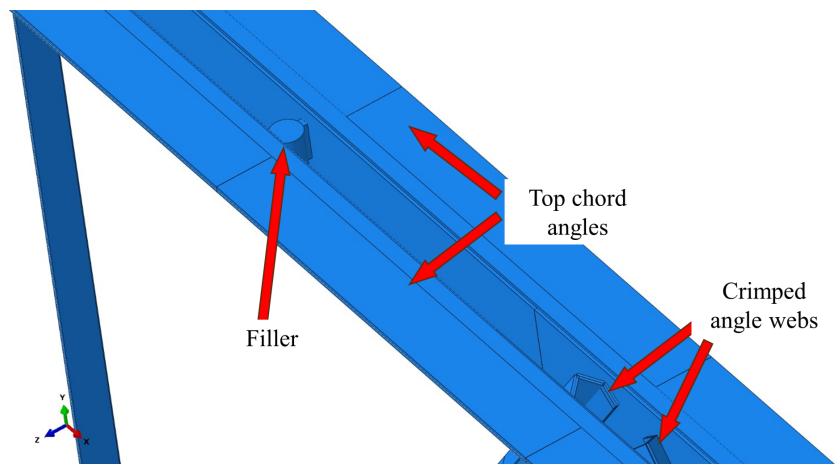


Figure 4.8: Filler and weld elements for connection with top chord angles

531 differences indicate that the FE models achieved high accuracy in predicting displacements within
 532 the serviceability range.

533 The second validation phase involved comparing the FE results with experimental data from
 534 two different joist models (24" and 30" depth) reported by Yost et al. [3]. While the study provides
 535 fundamental dimensions for the joist geometry, certain secondary parameters, such as specific weld
 536 lengths, web orientations, precise lateral support locations, and end support details, were not explicitly
 537 detailed in the original publication. Furthermore, material property documentation was primarily
 538 focused on the tested middle web members, which exhibited a yield strength of 57 ksi (exceeding
 539 the nominal 50 ksi specification). However, detailed stress-strain data or elasticity properties for the
 540 chords and other web members remained undefined.

541 To address these missing parameters, a series of engineering assumptions were made
 542 regarding support conditions and member orientations to reconstruct the models as faithfully as
 543 possible. Despite these inherent modeling challenges, the FE analyses demonstrated strong correlation
 544 with the experimental results. Figures 4.9 and 4.10 illustrate the failure modes, characterized by the
 545 buckling of W3 web members - a behavior consistent with the experimental observations. Moreover,
 546 the load-midspan deflection plots in Figures 4.11 and 4.12 reveal an excellent agreement in joist

Table 4.1: Comparison of deflection results under serviceability loads for design sheets and shell element FE models

Joist Type	Failure mode	Shell Element FEM (in)	Designsheets (in)	Difference (%)
Joist I	BC	1.685	1.670	0.9
	FW	1.642	1.600	2.6
	W3	1.640	1.600	2.5
Joist II	BC	1.636	1.60	2.2
	FW	1.600	1.600	0
	W3	1.631	1.600	1.9

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

547 stiffness. The FE models accurately captured the failure occurring shortly after the linear elastic
 548 stage, mirroring the trends seen in the three experiments conducted by Yost et al. [3].

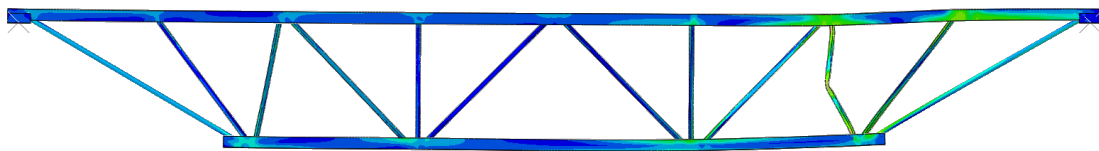


Figure 4.9: Buckled W3 web member in shell element FE models for joist with 24" depth

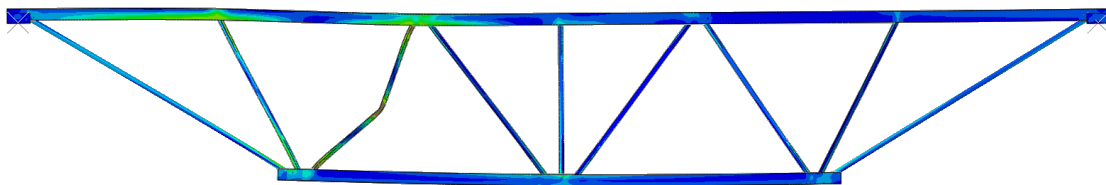


Figure 4.10: Buckled W3 web member in shell element FE models for joist with 30" depth

549 Following the verification process, the shell element FE models were analyzed under full
 550 loading conditions, leading to the identification of three failure modes: bottom chord yielding failure,
 551 first web yielding failure, and first compression web buckling failure. The results of these shell element
 552 FE models are presented in Figures 4.13 to 4.15, corresponding to each failure mode, respectively.
 553 The figures show the Von Mises stress distributions across the joist members. The red colored areas

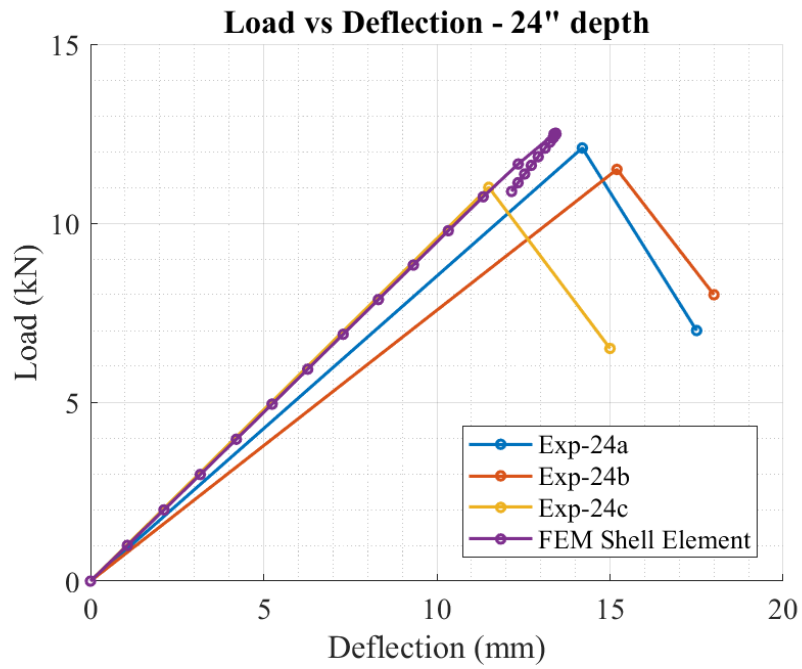


Figure 4.11: Comparison of experiments and shell element FE models for joist with 24" depth

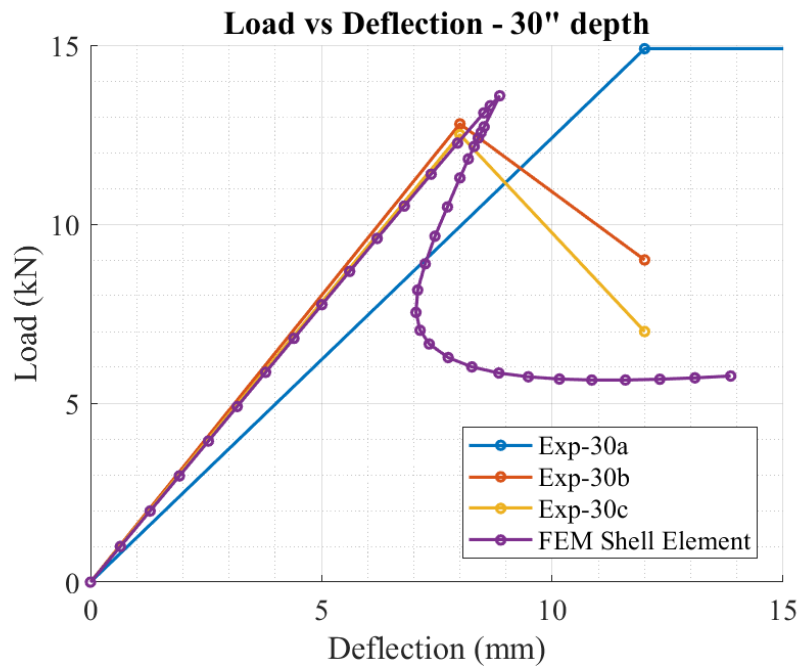


Figure 4.12: Comparison of experiments and shell element FE models for joist with 30" depth

Table 4.2: Comparison of load and midspan deflection results of experiments [3] and shell element FE models

Joist Type	Experiment [3]		FEM Shell	Difference (%)
	Load (kN)	Avg. Load (kN)	Load (kN)	
24a	12.1	11.53	12.5	8.48
24b	11.5			
24c	11.0			
30a	14.9	13.40	13.6	1.49
30b	12.8			
30c	12.5			
Joist Type	Deflection (mm)	Average Deflection (mm)	Deflection (mm)	Difference (%)
24a	14.2	13.63	13.43	1.46
24b	15.2			
24c	11.5			
30a	12	9.33	8.86	5.05
30b	8			
30c	8			

554 represent the high stress regions whereas the blue colored regions are having the least stresses in the
 555 analysis.

556 4.2. Models for Calculation of Weld Length Effects (Moment-Rotation Values)

557 Beam element FE models are not able to reflect the welded end connection effects as
 558 accurately as the results from shell element FE. Assuming fixed or pin end for the web connections
 559 affects the behavior of not only web members but also chord members. Different combinations of
 560 chord strengths and web strengths might lead to buckling in chord or web members. An example to
 561 this is shown in a previous study of Cicek, Sputo, and Blum [14].

562 Given that this study includes web compression buckling failure as one of the main failure
 563 modes, the end conditions of web members are critically important. Therefore, rotational springs

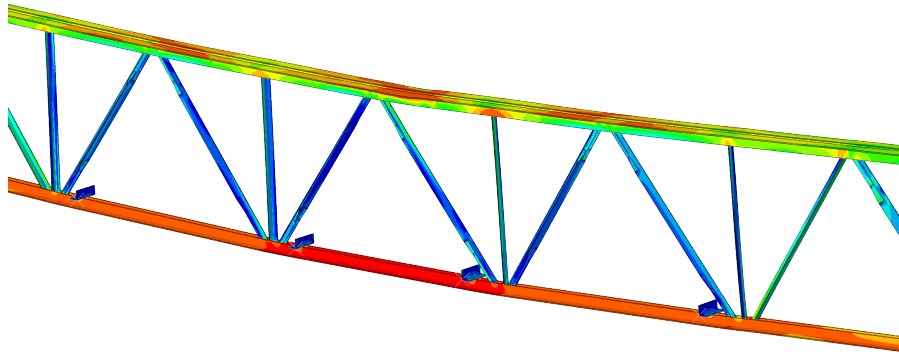


Figure 4.13: Bottom chord tension yielding failure mode shell element FE result

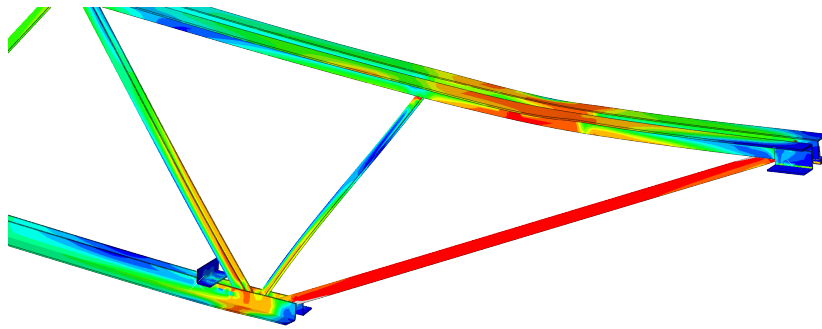


Figure 4.14: First web tension yielding failure mode shell element FE result

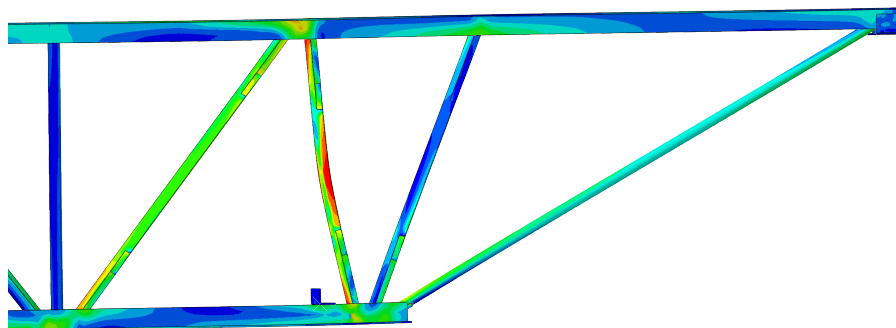


Figure 4.15: First compression web buckling failure mode shell element FE result

564 were assigned to web member ends and the rotational stiffness values of these springs were calculated
565 by modifying the shell element FE models previously created in this study.

566 This modified models only include the bottom chord and part of the webs from each groups
567 and updated with different web weld length ratio that were captured in statistical analysis on collected
568 weld length data. For each web group, the minimum, mean and maximum weld length ratios were
569 applied to the modified shell element FE model. The main criteria was obtaining the same moment
570 at each web in each model with the same load. According to the rotation of the webs under these
571 same moment values, moment-rotations of web groups for each weld length ratio were obtained, and
572 the rotational stiffness values were calculated by using these results.

573 Figure 4.16 shows part of the modified Joist II model and loading, and Figure 4.17 shows
574 the deflected shape of selected web members. Calculated moment-rotation curves of each weld groups
575 with minimum, mean, and maximum weld length ratio levels are given in Figures A.1 through A.6
576 in Appendix Section A for both HRS crimped angle and CFS channel sections.

577 The boundaries for rotational stiffness values were calculated from moment-rotation curves
578 by using minimum and maximum weld lengths. A linear formulation was defined between weld length
579 ratio input and the rotational stiffness values for each weld group and section type. The effect of
580 change in weld length was applied to the simulation beam element model with the change in rotational
581 stiffness values instead of updating the weld lengths inside the model, and the defined formula was
582 used at each weld length groups to calculate this rotational stiffness value. To evaluate the sensitivity
583 of the model to these connections, additional analyses were performed using conventional "pin-pin"
584 and "fix-fix" end conditions for the web members. As expected, the structural response of the models
585 with assigned rotational springs fell consistently between these two idealized boundaries, providing
586 a more realistic and advanced representation of the actual semi-rigid behavior of the welded joints.

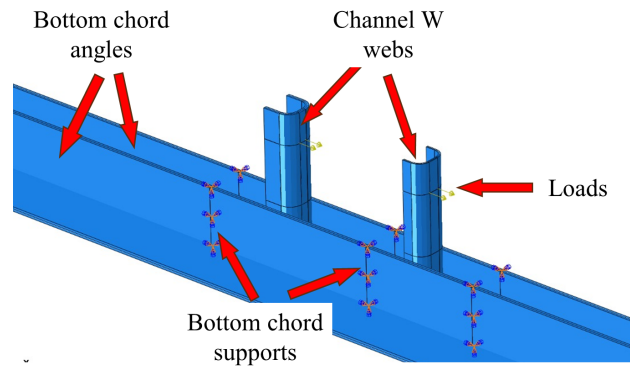


Figure 4.16: Loading of shell element FE model for moment-rotation analysis for Joist II W webs

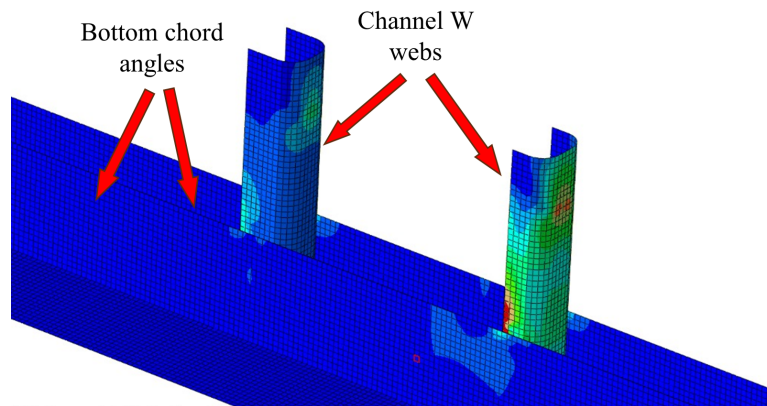


Figure 4.17: Shell element FE model result of moment-rotation analysis for Joist II W webs

587 4.3. Beam Element Models

588 Beam element FE models were preferred in this study for reliability analyses. The main
 589 reason for this is to reduce the time and storage cost of the whole study. Despite the lesser details in
 590 models than the shell element models, beam element FE models proved to be effective and showed
 591 that it can accurately predict the results. The same material models, load values, and input variables
 592 were used with necessary changes mainly in connections and supports. An important modification
 593 was applied to the W3 web buckling failure mode beam element models and explained in this chapter.

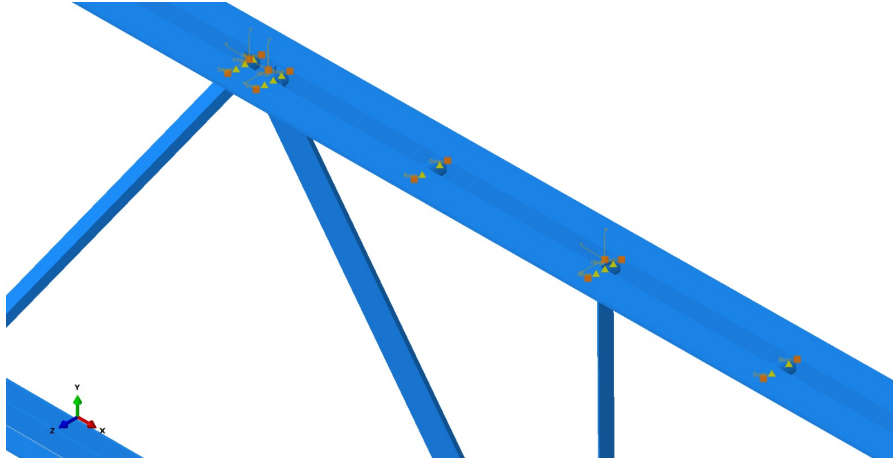


Figure 4.18: Rigid links between web-chord connection locations and filler locations

594 4.3.1 Web Connections

595 Chord angles were connected to each other with a rigid link in between chord angles at
 596 web end locations to create the same rigidity at web-chord connections. These rigid links were also
 597 used as filler members in filler locations. For the web-chord connections, web ends connected to the
 598 midpoint of these rigid links and the rotational springs (as detailed in Section 4.2) were assigned to
 599 the connection point.

600 4.3.2 Loading

601 Same ultimate load values were applied to the beam element FE models. The load were
 602 applied as surface loads in shell element models but for beam elements, uniformly distributed line
 603 loads were applied to the center of gravity of both top chord angles to prevent additional torsional
 604 forces.

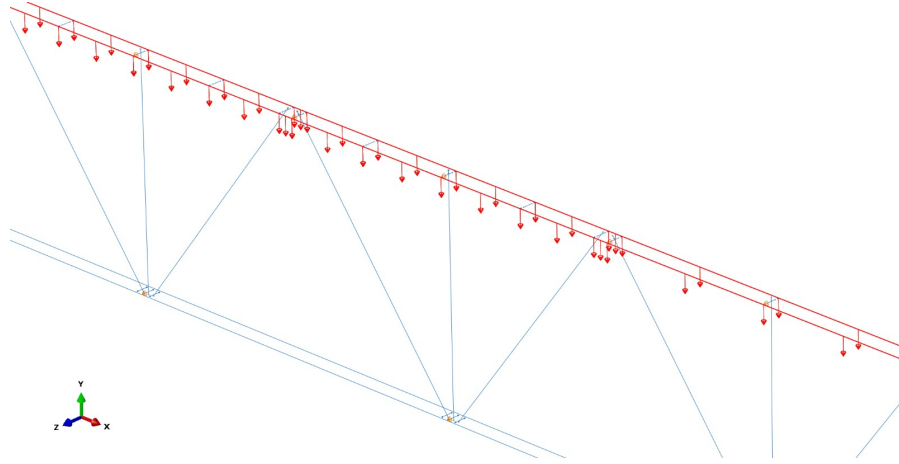


Figure 4.19: Uniformly distributed loads

605 4.3.3 Buckling failure models modification

606 A significant modification in the buckling failure mode of the beam element models involves
 607 the reduction of yield strength in the W3 web materials. While the shell element models clearly
 608 exhibited W3 web buckling failure, the beam element models did not capture this behavior and
 609 instead predicted approximately 12–15% higher load capacities compared to the shell element models.
 610 Several studies ([15], [16], [17], [18]) suggest that reducing the capacity of members in beam element
 611 models can increase the accuracy between the shell and beam element models. Two types of stiffness
 612 reduction was suggested in these studies, member stiffness reduction or system stiffness reduction by
 613 changing the tangent stiffness. Since the main focus of this study is to be able to capture the realistic
 614 capacity of the given designs, system stiffness reduction method is not the most feasible method,
 615 therefore, stiffness reduction of a single member method was selected. In this study, it was found that
 616 reducing only the yield strength of W3 web members, rather than changing the stiffness, increased
 617 the accuracy between the shell and beam element models, both in terms of load capacity and failure
 618 mode.

619 For Joist I, a reduction factor of 0.8 was adopted, as suggested in Section C2.3(a) of Chapter

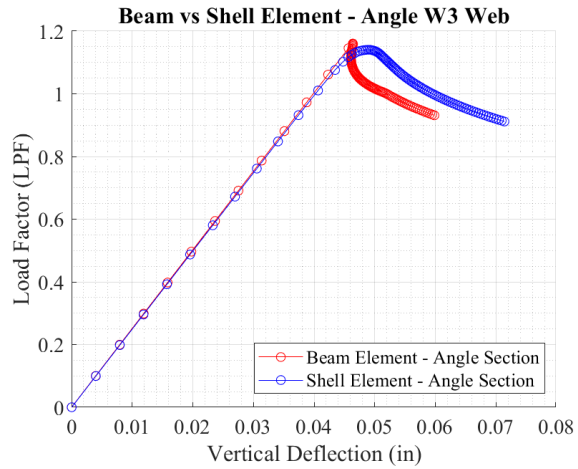
620 C in AISC 360-22 [19]. For Joist II, an initial reduction factor of 0.9 provided the best results for
621 singular web element models. The Figure 4.20 illustrates comparison of load-deflection responses
622 between the beam and shell element models for a single W3 web member under compression, utilizing
623 both angle and channel sections. With the applied reduction factors for yield strength, the accuracy of
624 the predicted buckling loads between the beam and shell element models was significantly improved.

625 Following multiple analyses with randomly assigned variables, it was observed that the
626 resultant Load Proportionality Factor (LPF) values in the beam element models were higher than
627 expected. In the context of the nonlinear Riks analysis used in this study, the LPF acts as a dimension-
628 less scaling multiplier for the applied load, which in this case, represents the specified load capacity
629 for the joist design. Therefore, an LPF value indicates the ratio of the simulated failure load to the
630 nominal design strength. To further investigate this difference, 300 random beam element models
631 were selected and identical 300 shell element models were generated and analyzed. These simulations
632 indicated that a reduction factor of 0.85 provided a higher degree of accuracy for cold-formed steel
633 (CFS) systems. Consequently, the previously adopted 0.9 reduction factor was revised to 0.85, after
634 which the full stochastic analyses were completed.

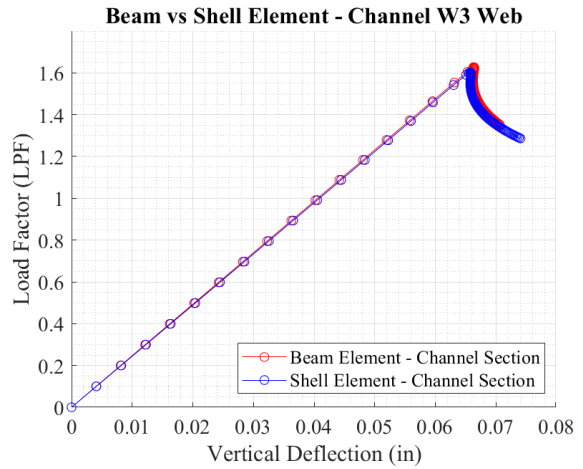
635 **4.3.4 Validation of Beam Element Models**

636 After the mentioned modifications were completed, the beam element models for six de-
637 signed joists were analyzed with second order nonlinear analyses and the load-deflection (vertical
638 deflection at mid-span) results were completed with the corresponding shell element models. Figures
639 4.21 to 4.23 show the outcome of each failure mode after the modified beam element FE models were
640 analyzed.

641 Model comparisons were completed for joists designed with both nominal and mean values.
642 Joists that were modeled with nominal value inputs were used in sensitivity analyses and joists that
643 were modeled with mean value inputs were used to ensure the accuracy of the joists with full statistical



(a) Angle section W3 web



(b) Channel section W3 web

Figure 4.20: Shell vs beam element model load-deflection comparison with angle (a) and channel (b) sections for W3 web member

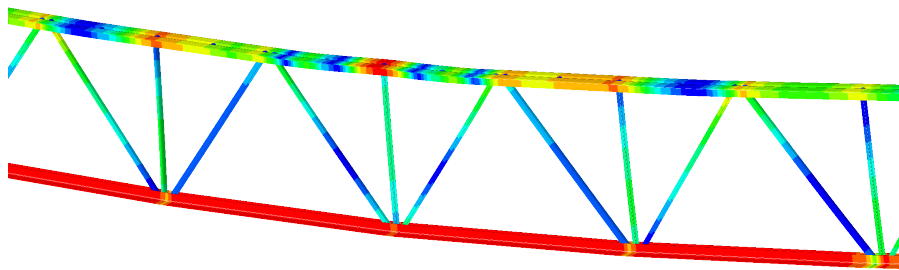


Figure 4.21: Bottom chord tension yielding failure mode beam element FE result

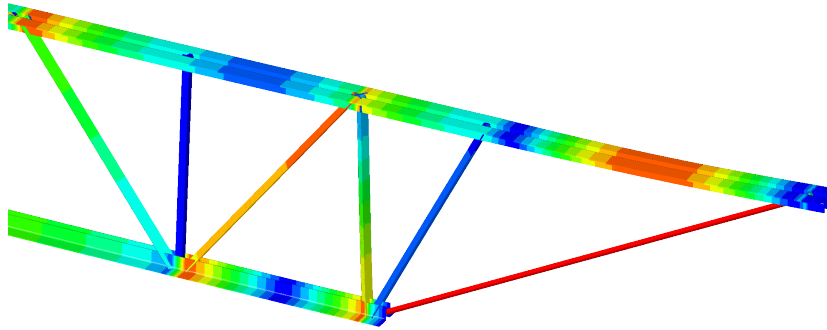


Figure 4.22: First web tension yielding failure mode beam element FE result

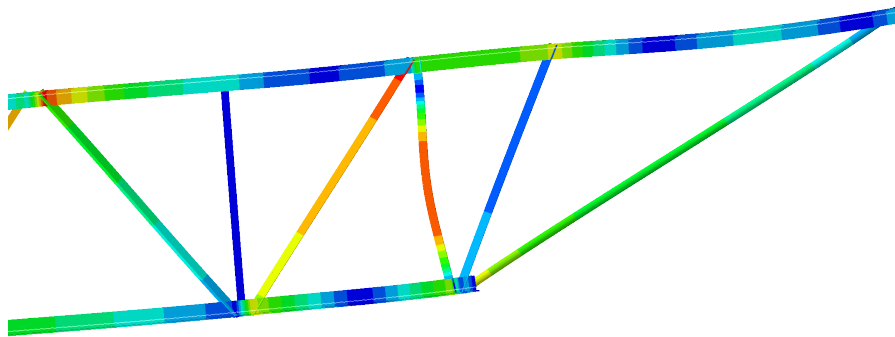


Figure 4.23: First compression web buckling failure mode beam element FE result

644 inputs. Table 4.3 and Table 4.4 shows the deflection comparison between shell and beam element
 645 models for nominal and mean value designed joists, respectively. Figures 4.24, 4.25, and 4.26 show
 646 the load-deflection curves of full joist analyses of six different models for both nominal and mean
 647 value designed joists.

Table 4.3: Comparison of vertical deflection at mid-span results under ultimate loads (load factor 1) for shell element and beam element FE models with nominal design values

Failure mode	Shell Element FEM (in)	Beam Element FEM (in)	Difference (%)
Joist I BC	4.272	4.279	0.16
Joist I FW	4.266	4.310	1.03
Joist I W3	2.701	2.707	0.22
Joist II BC	3.903	3.928	0.64
Joist II FW	3.219	3.241	0.68
Joist II W3	3.071	3.072	0.03

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

Table 4.4: Comparison of vertical deflection at mid-span results under ultimate loads (load factor 1) for shell element and beam element FE models with mean design values

Failure mode	Shell Element FEM (in)	Beam Element FEM (in)	Difference (%)
Joist I BC	4.029	4.015	0.035
Joist I FW	4.243	4.296	1.249
Joist I W3	2.691	2.701	0.372
Joist II BC	3.928	3.944	0.407
Joist II FW	3.237	3.265	0.865
Joist II W3	3.079	3.085	0.195

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

648 The comparisons indicate a high degree of accuracy between the shell and beam element FE
 649 models for both nominal and mean-value-designed joists. The strong agreement in overall stiffness of
 650 the joists is clear in the linear behavior phase of the joists and this extends to the nonlinear behavior
 651 range of the analyzed joist models. As a result of this, the generated beam element FE models provide

652 a reliable basis for conducting the reliability analyses.

653 **4.4. Second Order Nonlinear Analyses Results**

654 After the validation of both shell and beam element FE models were completed, full analyses
655 with ultimate loads were completed and maximum load capacity of the models were obtained. Non-
656 linearity was integrated by both material and geometric properties in this study. Material nonlinearity
657 was included using the material models previously given (Section 2.4), whereas the geometric non-
658 linearity was simulated by performing second-order analyses, and also including initial imperfection
659 in the designs predicting W3 buckling failure modes. Tables 4.5 and 4.6 include the maximum load
660 factors (LPF) obtained from each models for nominal and mean value designed systems. Additional
661 to the given tables, Figures 4.24, 4.25, and 4.26 present the behavior of each failure modes of each
662 joist for nominal and mean value shell and beam FE models.

Table 4.5: Maximum LPF reached under ultimate loads for shell element and beam element FE models with nominal design values

Failure mode	Shell Element FEM (LPF)	Beam Element FEM (LPF)	Difference (%)
Joist I BC	1.096	1.109	1.19
Joist I FW	1.100	1.106	0.55
Joist I W3	1.290	1.323	2.56
Joist II BC	1.414	1.416	0.14
Joist II FW	1.579	1.560	1.20
Joist II W3	1.364	1.313	3.74

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

663 The failure criterion for conventional member-based linear design is defined as the point at
664 which a member reaches its yield stress. However, for nonlinear systems, this is not always the case.
665 Nonlinear systems can sustain higher loads even after multiple members have yielded due to load

Table 4.6: Maximum LPF reached under ultimate loads for shell element and beam element FE models with mean design values

Failure mode	Shell Element FEM (LPF)	Beam Element FEM (LPF)	Difference (%)
Joist I BC	1.227	1.241	1.14
Joist I FW	1.234	1.236	0.16
Joist I W3	1.407	1.419	0.85
Joist II BC	1.580	1.586	0.38
Joist II FW	1.716	1.706	0.58
Joist II W3	1.462	1.430	2.19

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

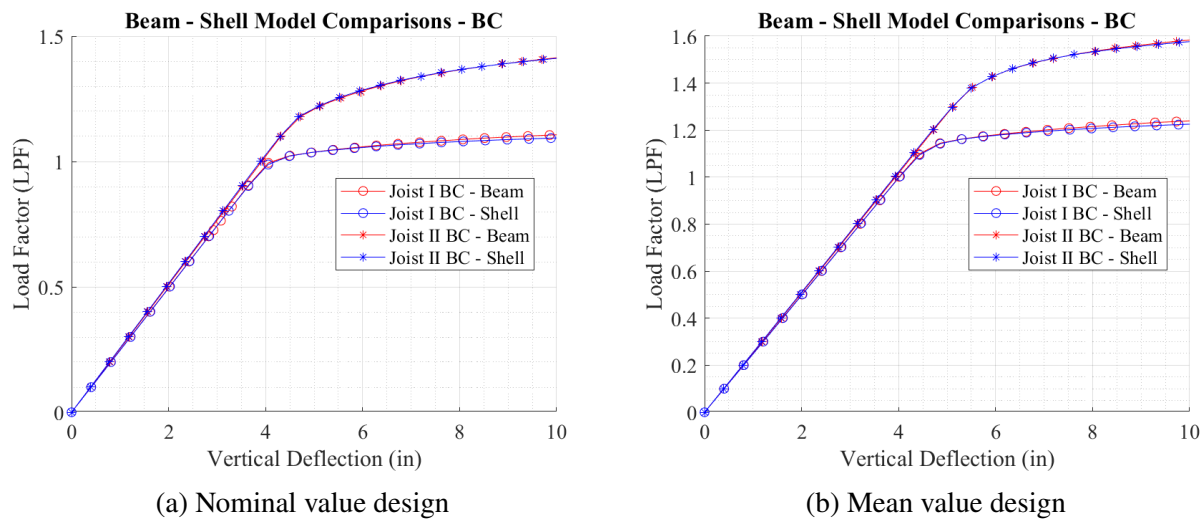
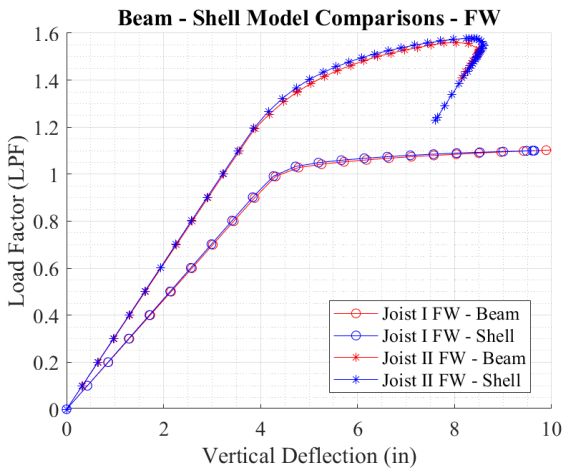


Figure 4.24: Shell vs beam element model load-deflection comparison with nominal (a) and mean (b) values for BC failure mode

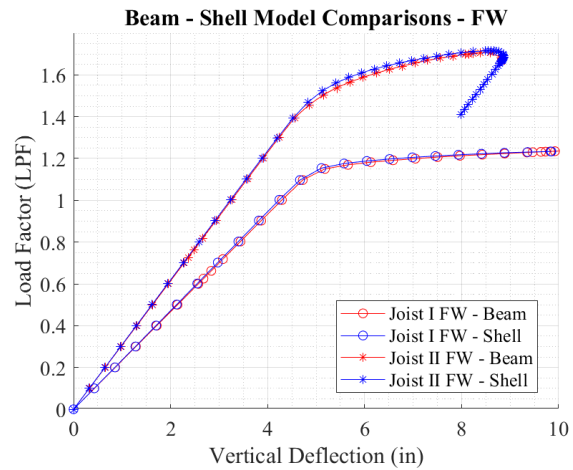
666 redistribution, provided that linear buckling does not occur in any member.

667 In the second-order nonlinear analyses of the modeled systems, none of the anticipated
 668 failure modes occurred under a load factor of 1. Second-order nonlinear Riks analysis provides the
 669 absolute highest load factor that the system can reach regardless of the failure mode. As a result, the
 670 analyses continued until one of the following conditions was met:

- 671 • A tension member (or multiple members) attained their ultimate stress levels or excessive strains

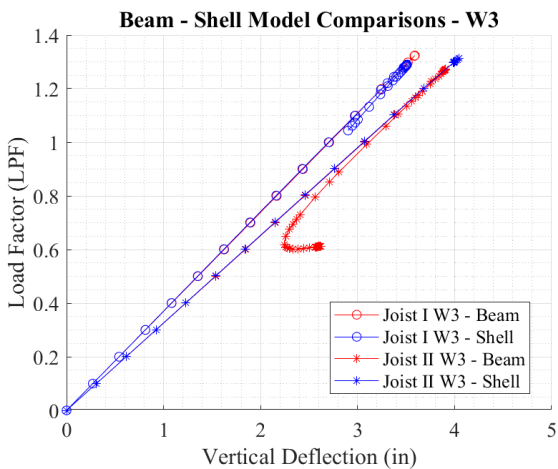


(a) Nominal value design

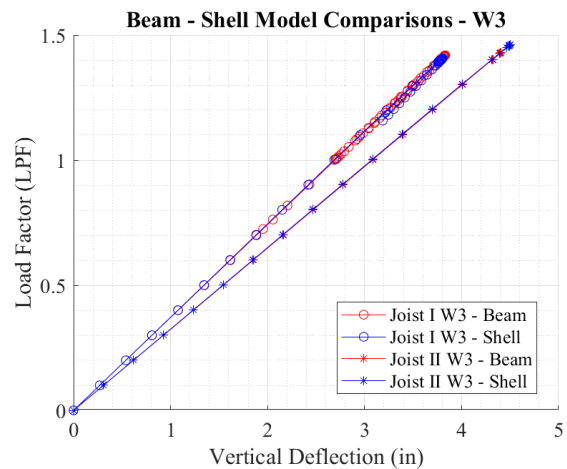


(b) Mean value design

Figure 4.25: Shell vs beam element model load-deflection comparison with nominal (a) and mean (b) values for FW failure mode



(a) Nominal value design



(b) Mean value design

Figure 4.26: Shell vs beam element model load-deflection comparison with nominal (a) and mean (b) values for W3 failure mode

672 (serviceability limit mentioned in Section 3.3)

- 673 • A compression member underwent compression buckling.

674 The obtained failure modes and anticipated failure modes are presented along with ultimate

675 design loads in Table 4.7.

Table 4.7: Comparison of failure modes in design sheets and shell element FE models results under ultimate loads

Joist Model	Ultimate Load (plf)	Designsheets anticipated failure mode	Shell Element FEM failure mode
Joist I	340	BC	BC
	367	FW	BC
	254	W3	W3
Joist II	337	BC	BC
	284	FW	FW
	271	W3	W3

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

676 **5. Random Value Generation and Sensitivity Study**

677 **5.1. Latin Hypercube Sampling**

678 Latin Hypercube Sampling (LHS) was preferred in this reliability study as an efficient
679 alternative of Monte Carlo simulations. LHS was chosen to increase the computational efficiency and
680 accuracy of the analysis, given the complexity and the number of the systems under consideration.
681 The study focuses on three primary variables for two different systems with different failure modes,
682 hence a robust sampling method was needed to adequately obtain the variability and combinations
683 within the complex data. LHS method was proven to reduce the necessary number of sampling, hence
684 the total number of analyses, and still acquire high performance. This efficiency is highly critical
685 and beneficial for accurate probabilistic assessments. As a result, LHS method was adopted for the
686 random sampling through this study.

687 While generating random samples for the simulations, truncation was applied to the prob-
688 ability distributions to enhance the physical accuracy of the models. The truncation limits were
689 established by considering the range of the collected data while ensuring that the sampled values
690 remained within realistic boundaries; specifically, extreme values that are theoretically possible in a
691 standard distribution but practically impossible in manufacturing were discarded. In defining these
692 truncated bounds, the limits for hot-rolled sections were determined based on ASTM A6/A6M speci-
693 fications [20], while the limits for cold-formed sections were set in accordance with the AISI S240-20
694 [21] standard. This approach ensures that the stochastic variables not only reflect the variability of the
695 collected data but also strictly adhere to the mandatory thickness and dimensional tolerances defined

696 by structural codes.

697 Due to the section type and size variety in a single joist, multiple random sets for same
698 inputs such as yield stresses, leg thicknesses, were generated for repeatedly at each simulation. All
699 these generated set of random values then verified with their own distribution parameters to ensure
700 the consistency in input statistics. Example distributions of these random variables are provided in
701 this section.

702 **5.1.1 Material Properties**

703 Different sections are manufactured from different batches in a manufactured joist. This
704 means that in a single joist there might be several different steel material properties among different
705 members. To include this complexity in the reliability study, every different section was assigned its
706 own material model created with a different set of random values. Following the recommendations
707 of the SJI Research Committee, a correlation was maintained between the material properties of
708 identical sections within a single joist, while distinct sections were treated independently. Predefined
709 distributions and distribution parameters were used to create different number of material sets for
710 each design and these were embedded into batch analysis code scripts.

711 Figures 5.1 and 5.2 show the histograms of generated random numbers and fitted distribu-
712 tions.

713 **5.1.2 Cross-sectional Imperfections**

714 Both HRS and CFS sections might have cross-sectional imperfections due to manufacturing
715 processes. The collected data shows that the variety of cross-sectional imperfections are higher in
716 CFS sections than HRS sections. According to the calculated statistics, random numbers for different
717 sections were created at each simulation. Assigning different set of random values for different type

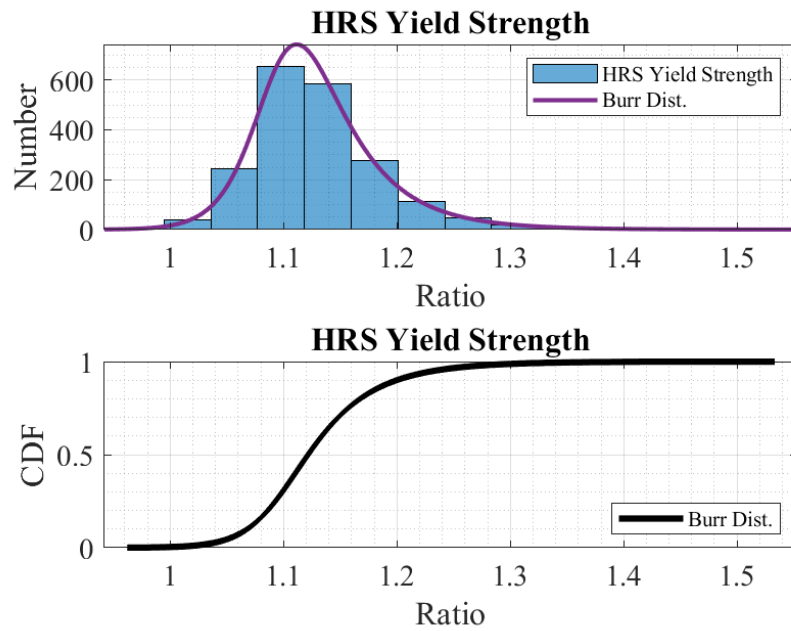


Figure 5.1: Histogram and statistical parameters of generated random HRS yield stress values

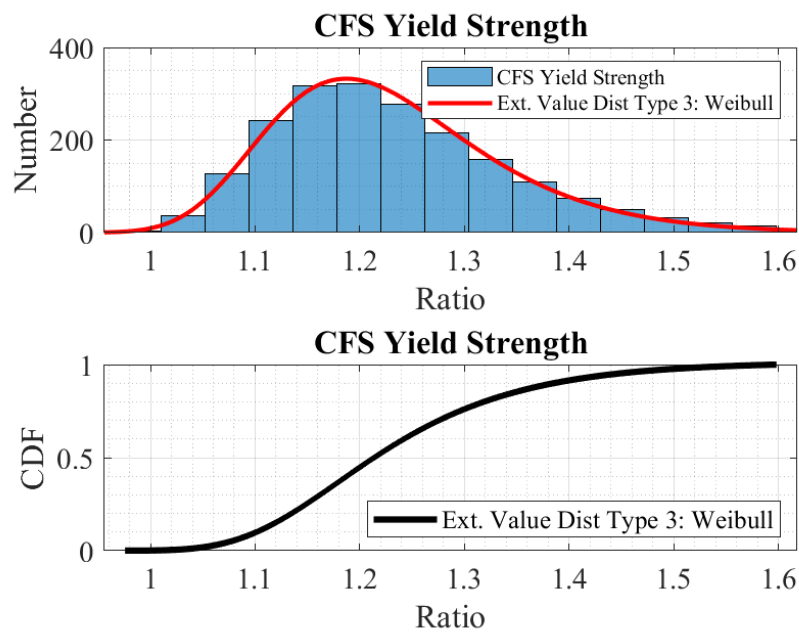


Figure 5.2: Histogram and statistical parameters of generated random CFS yield stress values

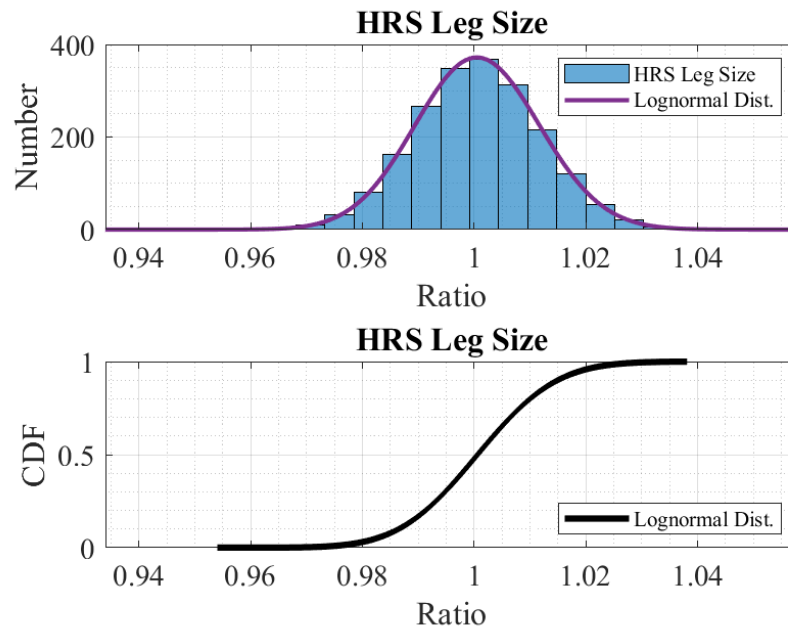


Figure 5.3: Histogram and statistical parameters of generated random HRS leg size values

718 of cross-sectional dimensions created the variability that the actual joist systems might have. Figures
 719 from 5.3 to 5.8 show the generated random numbers and fitted distributions for the cross-sectional
 720 imperfections input variables.

721 5.1.3 Weld Length

722 As detailed in Section 2.3, the weld length data were separated into three groups and
 723 statistical parameters were calculated for these groups. According to the random values, rotational
 724 springs were assigned with calculated rotational stiffness and the weld length effect was included
 725 in the joist design. Figures 5.9, 5.10 and 5.11 show the histograms of generated data and the fitted
 726 distributions.

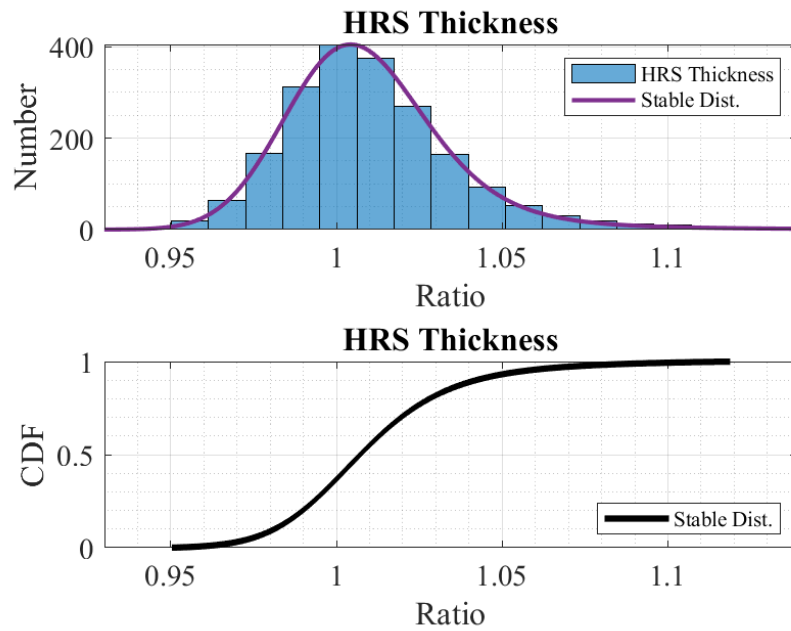


Figure 5.4: Histogram and statistical parameters of generated random HRS thickness values

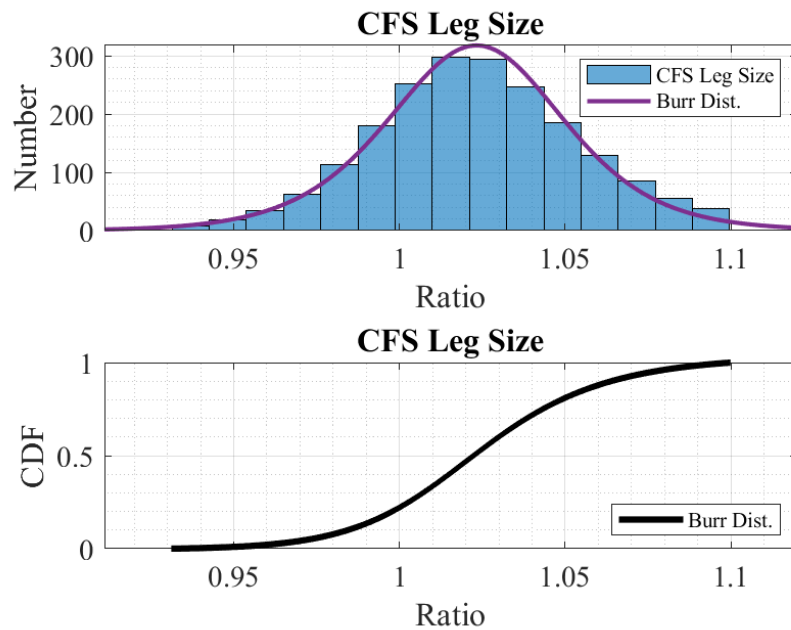


Figure 5.5: Histogram and statistical parameters of generated random CFS leg size values

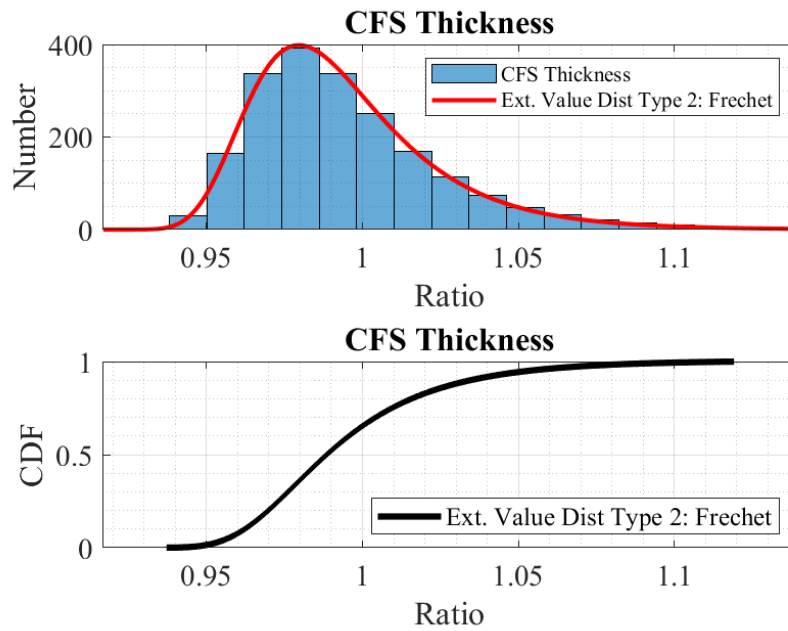


Figure 5.6: Histogram and statistical parameters of generated random CFS thickness values

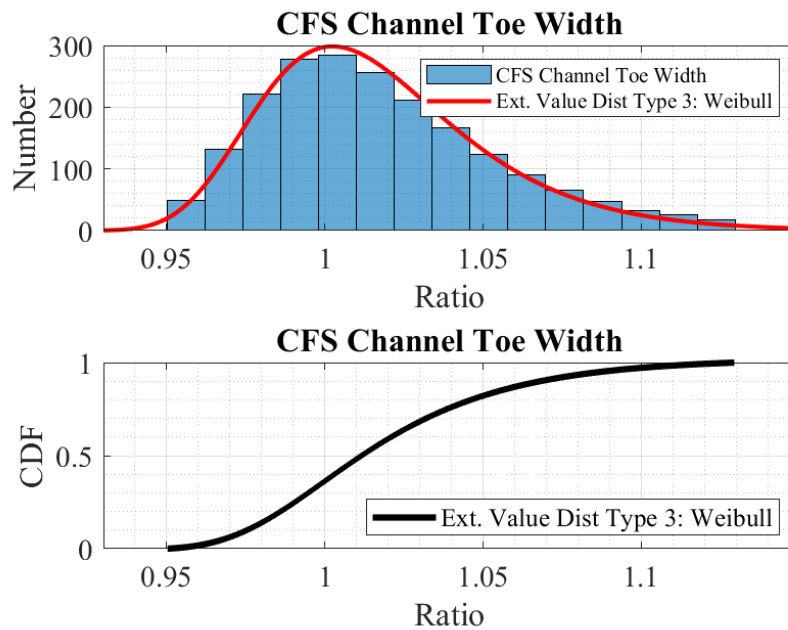


Figure 5.7: Histogram and statistical parameters of generated random CFS channel toe width values

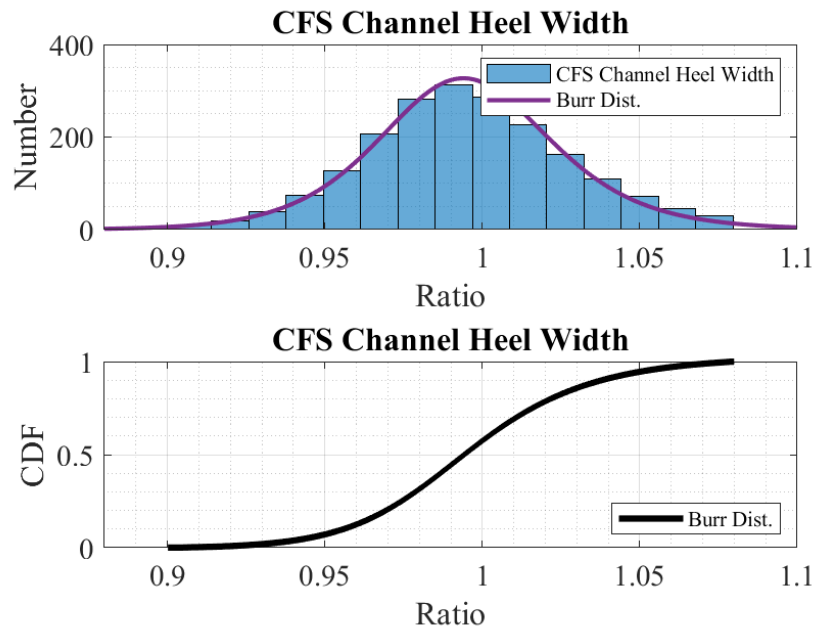


Figure 5.8: Histogram and statistical parameters of generated random CFS channel heel width values

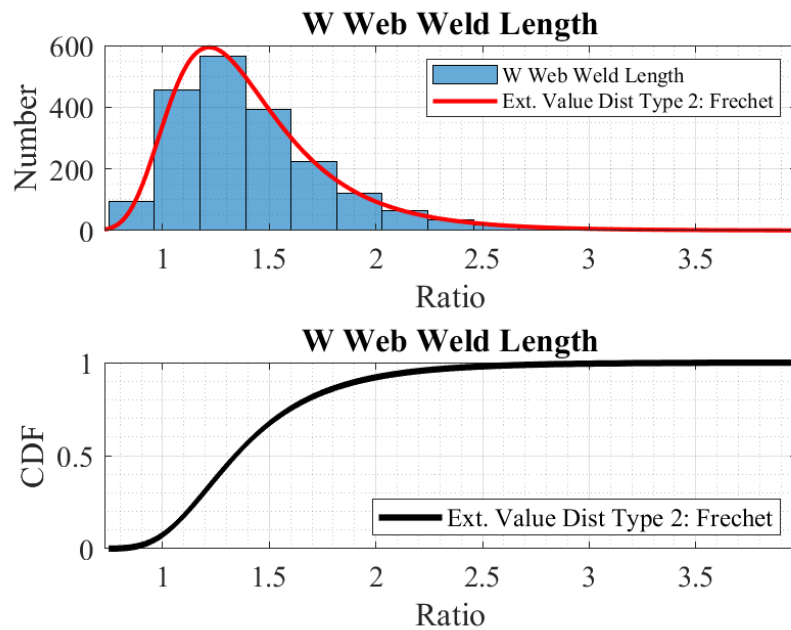


Figure 5.9: Histogram and statistical parameters of generated random W webs weld lengths values

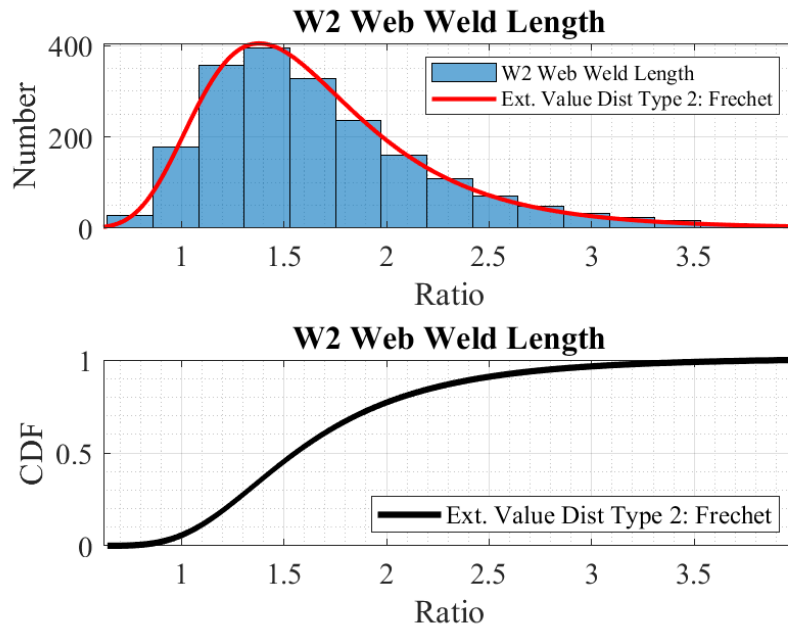


Figure 5.10: Histogram and statistical parameters of generated random W2 webs weld lengths values

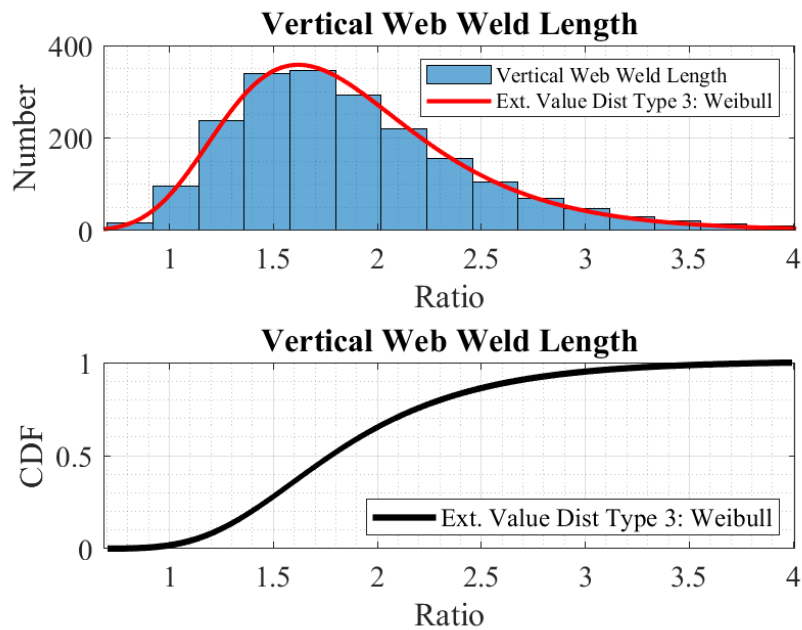


Figure 5.11: Histogram and statistical parameters of generated random vertical webs weld lengths values

727 **5.2. Sensitivity Study and Sensitivity Results**

728 Sensitivity study is a useful method to measure the impact of a single variable or a group
729 of variables on a system behavior. By systematically changing the selected variables, it is possible to
730 determine the influence of each variables by investigating the system responses.

731 In this study, sensitivity analyses were completed for all three variables for all failure modes
732 of both joists. It was first completed using nominal design values for all variables in each joist design,
733 to obtain the effect of each variable on a nominal system. The second sensitivity study was completed
734 on joist systems modeled using mean values of collected data. Using these means for all variables
735 simulated similar conditions closer to realistic joists. This dual approach provides understanding the
736 effects of each selected variable on both ideal systems and on more realistic systems. The details and
737 results of this sensitivity study, presented below and also provided with figures in the appendix, can
738 be found in Cicek, Sputo, and Blum [22].

739 Table 5.1 and 5.2 present the mean load factors of each model calculated from the sensitivity
740 analyses for each parameter for nominal and mean value systems, respectively. 1000 runs were
741 completed for each parameter for each joist design. Although the number of analysis was primarily
742 determined by stabilization of mean value of LPF results at each analysis, it was aimed to have at least
743 1000 analyses results to ensure the accuracy in distribution fitting. Also, to enhance the reliability of
744 the outcomes, prematurely terminated analyses, such as LPF results with 0.3, were discarded from
745 distribution fitting process. The figures of mean LPF value vs number of analysis for each failure
746 mode are given in Appendix Section B.

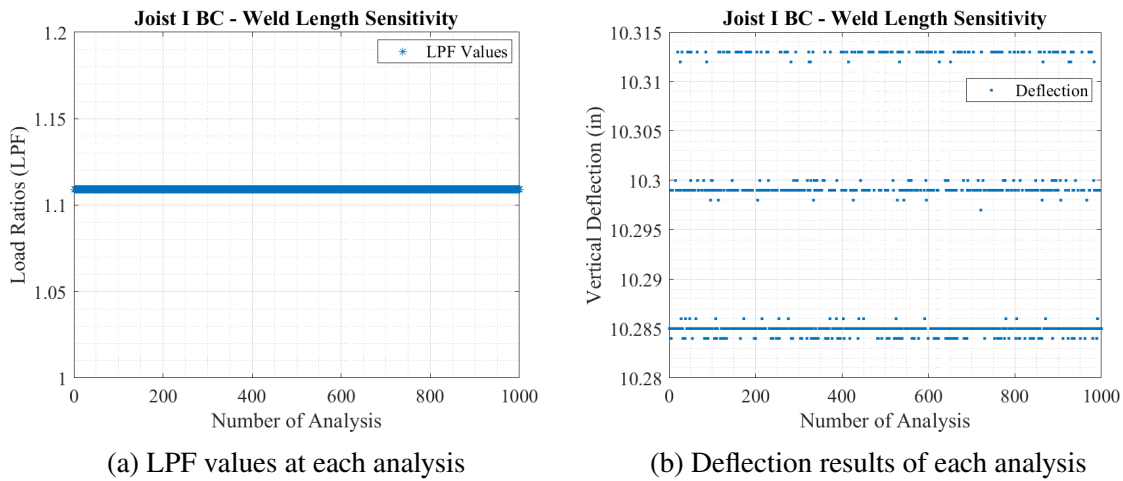


Figure 5.12: Joist I BC weld length sensitivity analyses results

747 5.2.1 Weld Length Sensitivity

748 Earlier in this study, it was found that adding springs to web ends influences the behavior
 749 of the joist and increase the accuracy. Despite accounting the effect of weld lengths in models, the
 750 sensitivity analysis showed that variations in weld length have negligible impact on the load capacity
 751 of joists. For all 1,000 analyses conducted for each model, the LPF values remained unchanged or
 752 significantly small changes were captured. This indicates that the given range of weld length variations
 753 coming from the collected data is not sufficient to influence the overall joist capacity significantly.
 754 Figure 5.12 show LPF values and deflection results for weld length sensitivity of Joist I BC design.
 755 Therefore, the weld length results were excluded from the results presented in this paper, as they do
 756 not contribute to the sensitivity findings.

757 5.2.2 Cross-sectional Imperfection Sensitivity

758 The mean LPF values calculated from the cross-sectional imperfection sensitivity analysis
 759 show no significant differences compared to the mean LPF values obtained from the beam element

760 FE models with nominal system parameters. However, despite similar mean LFP values to nominal
761 system, the dispersion of results indicates that the cross-sectional imperfections can increase and
762 decrease the capacity of the designed joist. The results presented in the figures in Appendix B show
763 the reduced capacity can vary between 5% and 15% under certain conditions. These results indicates
764 the importance of the manufacturing processes and the quality control in manufacturing plants.

765 **5.2.3 Yield Strength Sensitivity**

766 For both HRS and CFS joists, yield strength was found to be the most critical parameter,
767 significantly affecting the mean LFP values and creating a bigger spread in the distribution. All joists
768 exhibited higher mean LFP values than the the original models as shown in Table 5.1 and 5.2. This
769 differences show a parallel behavior to the collected data since both HRS and CFS materials show
770 higher mean yield strength values relative to nominal. Another important outcome of the sensitivity
771 study is the differences between nominal LFP value and the mean LFP value are higher for Joist II
772 than Joist I for the yield strength sensitivity analysis. This difference between the two joist types can
773 also be explained by the collected data. The CFS material has a higher mean yield stress than HRS
774 materials as it was shown in Table 2.2. Therefore, the CFS systems have a higher sensitivity to the
775 yield strength value than HRS material systems and as a result the increase in the mean LFP values
776 are higher.

777 **5.2.4 Discussion**

778 The first outcome of sensitivity study is that both beam and shell element FE models
779 show that including the material nonlinearity and using the semi-rigid web end connections instead
780 of pinned-end webs increases the overall load-carrying capacity of the joist designs. Additionally,
781 the sensitivity analyses demonstrate that yield strength has the most significant influence on joist

782 performance, particularly for CFS designs, where higher mean yield strength values resulted in greater
783 increases in LPF mean values compared to HRS designs, which can be explained by the collected data.
784 Cross-sectional imperfections sensitivity showed that the changes in the cross-sectional properties
785 caused reductions in joist capacity by up to 15% under specific conditions, emphasizing the need
786 for quality control in manufacturing processes. Weld length variations, however, showed negligible
787 impact on joist performance, indicating sufficient weld length in the data at hand. As a result, these
788 findings highlight the importance of both material and geometric parameters in providing safe and
789 efficient joist designs.

Table 5.1: Sensitivity analysis results for nominal systems

Failure Mode	Distribution Type	Mean	Standard Deviation
Joist I BC Yield Strength	Weibull Dist.	1.238	0.051
Joist I BC Sect. Impf.	Weibull Dist.	1.120	0.028
Joist I FW Yield Strength	Normal Dist.	1.210	0.035
Joist I FW Sect. Impf.	Normal Dist.	1.105	0.023
Joist I W3 Yield Strength	Weibull Dist.	1.411	0.033
Joist I W3 Sect. Impf.	Weibull Dist.	1.337	0.040
Joist II BC Yield Strength	Weibull Dist.	1.615	0.082
Joist II BC Sect. Impf.	Lognormal Dist.	1.378	0.044
Joist II FW Yield Strength	Weibull Dist.	1.756	0.081
Joist II FW Sect. Impf.	Weibull Dist.	1.554	0.053
Joist II W3 Yield Strength	Weibull Dist.	1.367	0.062
Joist II W3 Sect. Impf.	Normal Dist.	1.304	0.063

Modes: BC: bottom chord failure, FW: first web failure, W3: first web buckling failure

Table 5.2: Sensitivity analysis results for mean systems

Failure Mode	Distribution Type	Mean	Standard Deviation
Joist I BC Yield Strength	Weibull Dist.	1.245	0.052
Joist I BC Sect. Impf.	Weibull Dist.	1.223	0.031
Joist I FW Yield Strength	Normal Dist.	1.218	0.035
Joist I FW Sect. Impf.	Normal Dist.	1.206	0.026
Joist I W3 Yield Strength	Weibull Dist.	1.423	0.034
Joist I W3 Sect. Impf.	Weibull Dist.	1.410	0.041
Joist II BC Yield Strength	Weibull Dist.	1.653	0.082
Joist II BC Sect. Impf.	Lognormal Dist.	1.661	0.062
Joist II FW Yield Strength	Weibull Dist.	1.792	0.083
Joist II FW Sect. Impf.	Weibull Dist.	1.788	0.064
Joist II W3 Yield Strength	Weibull Dist.	1.446	0.072
Joist II W3 Sect. Impf.	Normal Dist.	1.451	0.080

Modes: BC: bottom chord failure, FW: first web failure, W3: first web buckling failure

790 **6. Simulation and Analysis Results**

791 In this section, full-scale simulations conducted using the beam element FE models, which
792 are previously verified in earlier sections, are presented. These simulations are a crucial step in
793 evaluating the joists performance under the variations in the randomness of the selected parameters
794 (material properties, cross-sectional properties, weld lengths) and represents the foundation for the
795 upcoming reliability analysis.

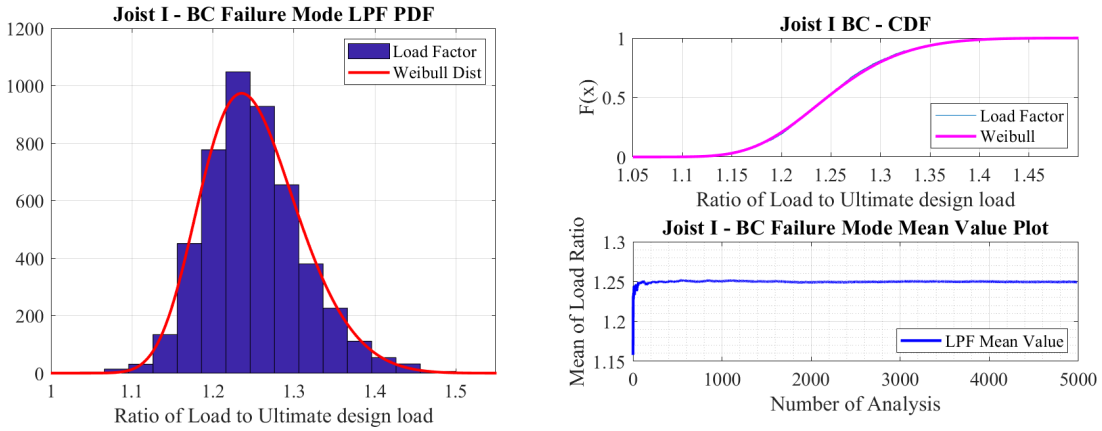
796 To ensure statistical robustness, the number of analysis should be adequate to fit a distribution
797 with high accuracy so that it would represent the randomness in input variables on both ends of the
798 spectrum. To determine the adequate number of simulations the same method for the sensitivity study
799 was used. The mean LPF value of each analysis result was recorded and the changes were observed.
800 It was found out that after 2500 analyses all of the LPF results reached a plateau indicating that further
801 analyses would not significantly impact the accuracy of the calculated statistics.

802 Increasing the number of analysis both increases the accuracy of the distribution fitting and
803 increasing the likelihood of having a higher number of simulations with near-extreme conditions.
804 Therefore, even though the figures show that 2000 analyses would be adequate to obtain a stable mean
805 LPF value, 5000 analyses were conducted for each joist for all failure modes.

806 As it was mentioned in sensitivity study section that during the simulations a small number
807 of analyses terminated prematurely and these failed analyses were identified and filtered out to ensure
808 the integrity of the dataset. The remaining valid analyses were used to calculate statistical parameters.

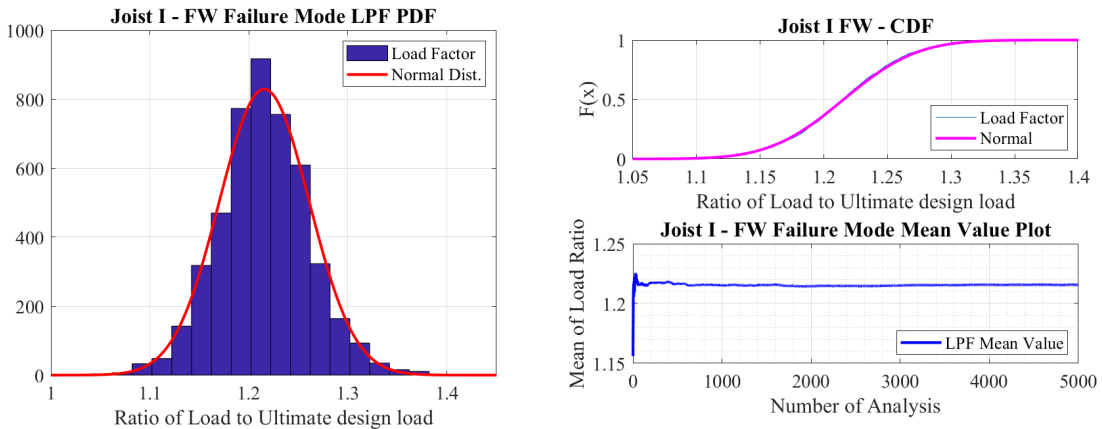
809 The outcomes of these simulations are summarized in Table 6.1 and Figures 6.1 through
810 6.6. For each model, fitted distribution and related mean and standard deviation of the load factor

811 (LPF) values were provided. Furthermore, plots showing the convergence of the mean LPF values
 812 as the number of analyses increases were provided to demonstrate the adequacy of the number of
 813 simulations. These results set the basis for the reliability and resistance factor evaluation, which will
 814 be detailed in the next section.



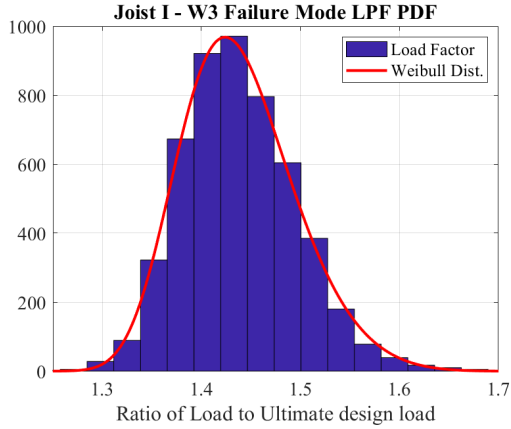
(a) Histogram of LPF and fitted distribution PDF (b) CDF and mean LPF value at each step

Figure 6.1: Joist I BC reliability analyses results and fitted distribution

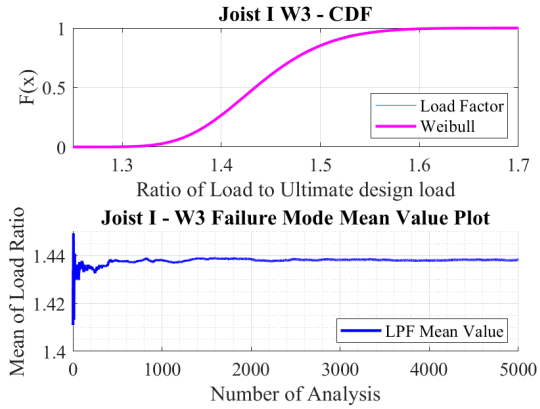


(a) Histogram of LPF and fitted distribution PDF (b) CDF and mean LPF value at each step

Figure 6.2: Joist I FW reliability analyses results and fitted distribution

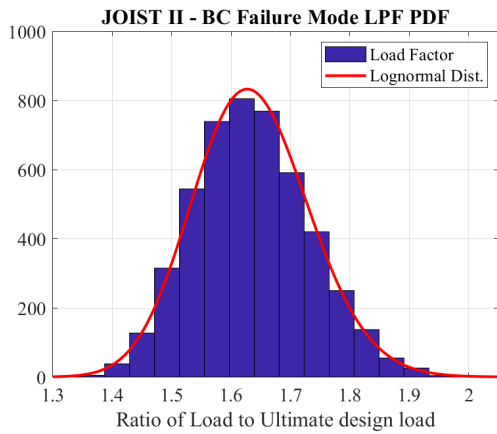


(a) Histogram of LPF and fitted distribution PDF

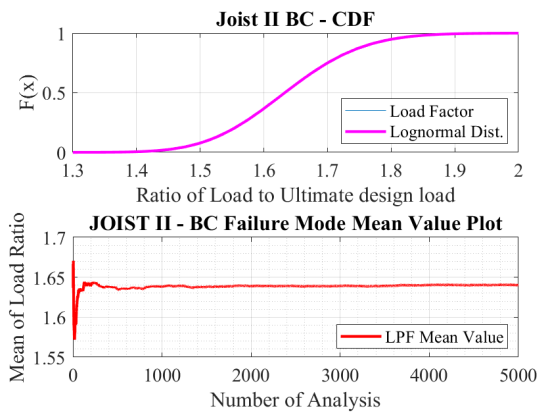


(b) CDF and mean LPF value at each step

Figure 6.3: Joist I W3 reliability analyses results and fitted distribution

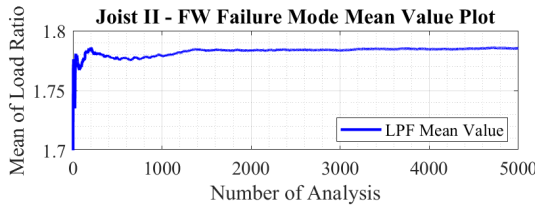
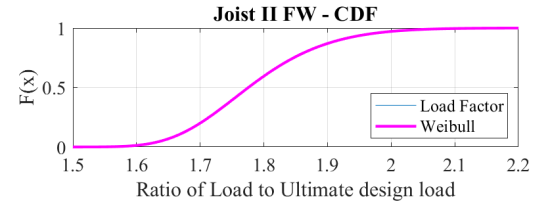
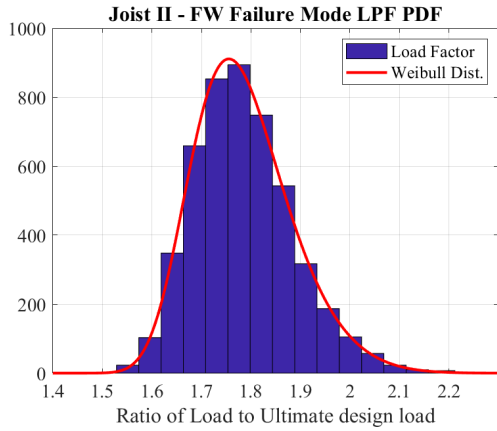


(a) Histogram of LPF and fitted distribution PDF



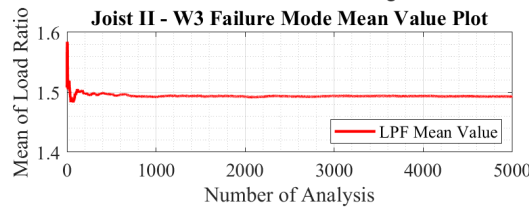
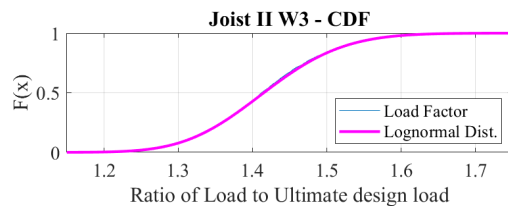
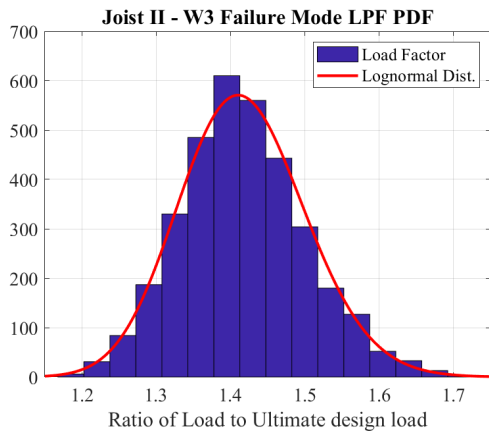
(b) CDF and mean LPF value at each step

Figure 6.4: Joist II BC reliability analyses results and fitted distribution



(a) Histogram of LPF and fitted distribution PDF (b) CDF and mean LPF value at each step

Figure 6.5: Joist II FW reliability analyses results and fitted distribution



(a) Histogram of LPF and fitted distribution PDF (b) CDF and mean LPF value at each step

Figure 6.6: Joist II W3 reliability analyses results and fitted distribution

Table 6.1: Full simulation analysis results (LPF)

Failure Mode	Distribution Type	Location / Mean (μ)	Scale / St. Dev. (σ)	Shape (k)
Joist I BC	Weibull Dist.	1.226	0.056	-0.156
Joist I FW	Normal Dist.	1.215	0.045	-
Joist I W3	Weibull Dist.	1.415	0.053	-0.157
Joist II BC	Lognormal Dist.	0.490	0.0597	-
Joist II FW	Weibull Dist.	1.744	0.0894	-0.125
Joist II W3	Lognormal Dist.	0.347	0.0598	-

Modes: BC: bottom chord failure, FW: first web failure, W3: first web buckling failure

Table 6.2: Theoretical mean and standard deviation values derived from the fitted probability distributions from full simulation analysis results (LPF)

Failure Mode	Distribution Type	Location / Mean (μ)	Scale / St. Dev. (σ)
Joist I BC	Weibull Dist.	1.251	0.061
Joist I FW	Normal Dist.	1.215	0.045
Joist I W3	Weibull Dist.	1.439	0.058
Joist II BC	Lognormal Dist.	1.636	0.098
Joist II FW	Weibull Dist.	1.785	0.100
Joist II W3	Lognormal Dist.	1.418	0.085

Modes: BC: bottom chord failure, FW: first web failure, W3: first web buckling failure

815 **7. Structural Reliability Sample Framework**

816 In structural engineering, reliability is defined as the probability that a structure or com-
817 ponent will fulfill its intended function safely under specified conditions for a given duration. To
818 evaluate this performance, a limit state function, also known as a performance function, is typically
819 utilized to define the boundary between safe and unsafe regions. As discussed by Nowak, A. and
820 Collins, K. [23], this relationship can be fundamentally expressed as:

$$g(R, Q) = R - Q \quad (7.1)$$

821 where R represents the resistance (capacity) and Q represents the load effect (demand). In
822 this traditional safety margin framework, the structure is considered safe when $g \geq 0$, whereas the
823 condition $g < 0$ signifies failure. Since both R and Q are continuous random variables characterized
824 by their own probability density functions (PDFs), the safety of the system is governed by the
825 probability of failure (P_f), expressed as:

$$P_f = P(R - Q < 0) = P(g < 0) \quad (7.2)$$

826 While structural reliability involves the interplay between demand and capacity, this project
827 specifically focuses on the resistance (R) side of the reliability equation. The objective is to accurately
828 characterize the variability in joist capacity resulting from uncertainties in material properties and
829 geometric configurations. This emphasis on the resistance component is consistent with the reliability
830 provisions of AISI S100 Chapter K ([6]), which provides a framework for establishing resistance

831 factors (ϕ) based on statistical data. Code committees could combine the results of this project on
832 resistance variability with loading statistics and variability of their choosing.

833 To generate the necessary data for this resistance-focused evaluation, Latin Hypercube
834 Sampling (LHS) with truncated distributions was employed. This method efficiently captures the
835 variability of the input variables affecting resistance, while truncation ensures that the generated
836 samples remain within physically realistic bounds based on collected data. By isolating and analyzing
837 the stochastic nature of the joist capacity through high-fidelity FEA, the coefficients required for the
838 AISI S100 reliability equations were calculated. Specifically, the data collected and analyzed in this
839 study allow for a refined calibration of the resistance factors, ensuring that the target reliability index
840 (β) is achieved when these joists are subjected to standard load combinations.

$$\phi = C_{\phi}(M_m F_m P_m) e^{-\beta_o \sqrt{V_M^2 + V_F^2 + C_P V_P^2 + V_Q^2}} \quad (7.3)$$

841 Resistance Factor (ϕ) for each system were calculated by using Equation 7.3. Explanations
842 and formulations of each coefficient are given in AISI S100. The ϕ coefficient was calculated
843 according to the distribution parameters of material and cross-sectional properties, and the calculated
844 distribution parameters of LPF simulation results of each joist model.

845 Certain coefficients in the reliability equation are not derived from the collected data or
846 the FEA results but are based on established load and reliability theories. The AISI Specification
847 provides recommended values for C_{ϕ} , β_o , and V_Q , which are functions of the live-to-dead load ratio
848 (α). These values are derived from the mean load intensities and the corresponding coefficients of
849 variation established by Ellingwood [24]. While the Specification typically assumes a ratio of $\alpha = 5$,
850 the SJI research committee representatives suggested using $\alpha = 3$ to better reflect realistic service
851 conditions for steel joists.

852 Consequently, instead of using the default tabulated values from AISI, C_{ϕ} and V_Q were

853 recalculated using the corresponding equations provided in the Commentary to the Specification and
 854 here in Eqs. 7.4, 7.5 and 7.6 (more details can be found in paper of Meimand and Schafer [25]).
 855 This approach, following the probabilistic framework developed by Ellingwood [24], ensures that the
 856 derived resistance factor ϕ_{sys} accurately represents the behavior of the steel joist system under the
 857 combined uncertainties of material, fabrication, and loading effects. This provides a rational basis
 858 for the reliability calibration presented in Section 4.3.

$$C_\phi = \frac{\frac{1.2 + 1.6\alpha}{\alpha}}{\frac{1.05 + \alpha}{\alpha}} \quad (7.4)$$

$$\beta = \frac{\ln \left[\frac{M_m \cdot F_m \cdot P_m \cdot \Omega \cdot \left(\frac{1 + \alpha}{\alpha} \right)}{\frac{1.05 + \alpha}{\alpha}} \right]}{\sqrt{V_M^2 + V_F^2 + V_P^2 + V_Q^2}} \quad (7.5)$$

$$V_Q = \sqrt{\frac{\left(\frac{1.05}{\alpha} \right)^2 \cdot 0.1^2 + 0.25^2}{\frac{1.05 + \alpha}{\alpha}}} \quad (7.6)$$

859 where $\alpha = \frac{L}{D}$

860 The coefficients related to the materials and sectional imperfections are also included in the
 861 formulation. Since the joists were designed using CFS and HRS materials separately, the M_m and V_M
 862 parameters resulted in different values for Joist I and Joist II. These values were determined based
 863 on the Coefficient of Variation (C.O.V) values obtained from the mean and standard deviation of the
 864 material data provided by SJI, which was previously discussed in Section 2.

865 Similarly, the coefficients F_m and V_F in the formula are related to the sectional property
 866 distribution parameters. For the cross-sectional properties, distribution parameters are available for

867 both thickness and leg sizes, based on the data and distributions previously analyzed in Section 2.
868 To determine a single representative value for these coefficients, a sensitivity analysis was performed
869 by separately varying only the thickness and only the leg size. This sensitivity analysis involved
870 1000 simulations for each parameter for both Joist I and Joist II. The results showed that thickness
871 and leg size have nearly the same impact on the load-carrying capacity. Therefore, the mean and
872 standard deviation values from both thickness and leg size were averaged (separately for CFS and
873 HRS materials) and used as the final distribution parameters for the calculations in Eq. 7.3.

874 Coefficients P_m , V_P , and C_P are the inputs related to the analyses or test results of the study
875 where:

- 876 • P_m represents the mean value of professional factor (P) for tested component (which is the
877 mean LPF values),
- 878 • V_P denotes coefficient of variation of test results (C.O.V of obtained LPF distribution), with a
879 minimum value of 0.065.
- 880 • C_P coefficient is given as the number of simulations/tests completed.

881 These input parameters are derived from the LPF distribution results of the 5000 reliability
882 analyses per joist. The LPF is defined as the load ratio, which is calculated by dividing the maximum
883 load obtained from the analysis by the nominal capacity of the joist determined by the SJI truss
884 method.

885 Initially, the nominal strength was taken from SJI capacity calculations where the load
886 factor was set to 1 (LPF = 1). However, as Table 4.5 shows, shell FE models show that the designed
887 systems can actually achieve higher load capacities than the truss method predicts. Therefore, a new
888 normalization was also applied to the P_m calculations. In this updated approach, the P_m values were
889 normalized using the load factors obtained from the shell FE models (previously provided in Table
890 4.5) with all random variables at their nominal values, instead of using LPF = 1.

891 This method more accurately reflects the impact of the randomness of the input variables

892 since the shell model represents joist behavior more precisely than the design calculations. Since the
893 nominal load factors from the shell FE models are higher than $LPF = 1$, this normalization resulted in
894 lower P_m values, and therefore, lower resistance factors and reliability values compared to the initial
895 method. The updated coefficient values and the calculated resistance factors with predefined target
896 reliability values are presented in Tables 7.3 and 7.4, respectively.

897 Tables 7.1 and 7.3 present the values for each coefficient associated with each failure mode
898 design. These tables utilize P_m and M_m values derived from the nominal distribution equivalent
899 parameters provided in Table 6.2. The decision to use equivalent normal distribution parameters is
900 primarily based on the operational characteristics of the First-Order Reliability Method (FORM), as
901 the accuracy of FORM is significantly enhanced when input variables follow a Gaussian distribution.
902 While FORM can accommodate non-normal distributions, the precision of the method tends to
903 decrease as the input distributions deviate further from the normal shape.

904 A potential disadvantage of this transformation is the risk of losing accuracy if the equiva-
905 lent normal distribution fails to capture the extreme tail behavior of the original best-fit distributions.
906 However, a comparative analysis of the distributions used in this study indicates that both the best-fit
907 and normal distribution fits cover the tail regions effectively, justifying the use of normal equivalents.
908 Ultimately, while both approaches—using original non-normal distributions or their normal equiv-
909 alents—are viable within the FORM framework, the choice depends on balancing computational
910 accuracy with the specific characteristics of the data. Given the strong tail alignment observed in
911 this study, the normal equivalent parameters were adopted to ensure higher reliability in the FORM
912 results.

913 Based on these inputs, Resistance Factors (ϕ) were calculated for Target Reliability Indices
914 (β_o) of 2.5, 2.6, 3.0, 3.25, and 3.5. These specific β_o values were selected based on the recommenda-
915 tions from the SJI research committee representatives and the corresponding standard reliability index
916 levels specified in ASCE 7-16 [26]. The results are provided in Tables 7.2 and 7.4. Additionally,

917 these tables present the Reliability Index values for a constant Resistance Factor (ϕ) of 0.9.

Table 7.1: Coefficient values for each model (Nominal Capacity with SJI calculation)

Failure Mode	Joist I			Joist II		
	BC	FW	W3	BC	FW	W3
C_ϕ		1.48			1.48	
M_m		1.098			1.237	
F_m		1.003			0.977	
P_m	1.251	1.215	1.439	1.636	1.785	1.418
V_M		0.158			0.1	
V_F		0.011			0.123	
V_P (min = 0.065)	0.065	0.065	0.065	0.065	0.065	0.065
C_P	1	1	1	1	1	1
V_Q		0.19			0.19	

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

Table 7.2: Resistance Factors with varying Target Reliability Index, β_o (Nominal capacity with SJI calculation)

	Resistance Factors										Reliability Index
	$\beta_o = 2.5$		$\beta_o = 2.6$		$\beta_o = 3$		$\beta_o = 3.25$		$\beta_o = 3.5$		$\phi = 0.9$
	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	β_o
Joist I BC	1.076	1.196	1.049	1.165	0.947	1.052	0.888	0.987	0.833	0.926	3.199
Joist I FW	1.046	1.162	1.020	1.133	0.921	1.023	0.864	0.960	0.810	0.900	3.088
Joist I W3	1.238	1.375	1.246	1.341	1.089	1.210	1.022	1.135	0.959	1.065	3.747
Joist II BC	1.543	1.715	1.504	1.671	1.358	1.509	1.274	1.415	1.195	1.328	4.608
Joist II FW	1.684	1.872	1.642	1.824	1.482	1.647	1.390	1.545	1.304	1.449	4.950
Joist II W3	1.338	1.486	1.303	1.449	1.117	1.308	1.104	1.226	1.036	1.151	4.049

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

Table 7.3: Coefficient values for each model (Nominal Capacity with shell element models)

Failure Mode	Joist I			Joist II		
	BC	FW	W3	BC	FW	W3
C_ϕ		1.48			1.48	
M_m		1.098			1.237	
F_m		1.003			0.977	
P_m	1.140	1.105	1.115	1.160	1.131	1.096
V_M		0.158			0.1	
V_F		0.011			0.123	
V_P (min = 0.065)	0.065	0.065	0.065	0.065	0.065	0.0779
C_P	1	1	1	1	1	1
V_Q		0.19			0.19	

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

Table 7.4: Resistance Factors with varying Target Reliability Index, β_o (Nominal capacity with shell element models)

	Resistance Factors										Reliability Index
	$\beta_o = 2.5$		$\beta_o = 2.6$		$\beta_o = 3$		$\beta_o = 3.25$		$\beta_o = 3.5$		$\phi = 0.9$
	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	ϕ	$\phi/0.9$	β_o
Joist I BC	0.981	1.090	0.957	1.063	0.864	0.960	0.811	0.901	0.760	0.845	2.840
Joist I FW	0.951	1.057	0.927	1.030	0.837	0.930	0.785	0.872	0.736	0.818	2.715
Joist I W3	0.959	1.066	0.935	1.039	0.844	0.938	0.792	0.880	0.743	0.826	2.750
Joist II BC	1.091	1.213	1.064	1.182	0.960	1.067	0.901	1.001	0.845	0.939	3.254
Joist II FW	1.067	1.185	1.040	1.155	0.939	1.043	0.881	0.978	0.826	0.918	3.164
Joist II W3	1.025	1.139	0.998	1.109	0.900	1.000	0.844	0.937	0.791	0.878	3.000

Modes: BC: bottom chord failure, FW: first web failure, W3: web buckling failure

918 **8. Conclusion**

919 This study provides a comprehensive evaluation of steel joist reliability through the integra-
920 tion of high-fidelity shell and beam finite element modeling with advanced stochastic analyses. By
921 shifting the focus from traditional member-based assessments to a system-based resistance approach,
922 this research accurately captures the complex interactions and failure mechanisms inherent in joist
923 systems. The methodology successfully incorporates realistic variations in material properties, cross-
924 sectional dimensions, and weld lengths, providing a more refined representation of actual structural
925 capacity.

926 A central contribution of this work is the detailed investigation of the resistance (R) com-
927 ponent of the reliability equation. By isolating the variability in joist capacity, the study underscores
928 how material strength fluctuations and geometric imperfections—captured via Latin Hypercube Sam-
929 pling—directly influence structural robustness. The research demonstrates that while the First-Order
930 Reliability Method (FORM) is a versatile tool, its application using normal equivalent distribution
931 parameters provides a stable and accurate framework for deriving design values, provided that tail
932 behaviors are carefully aligned.

933 Furthermore, the results support the premise that current structural standards, which are pri-
934 marily based on member reliability, tend to underestimate the inherent reliability of the entire system.
935 As shown in Table 7.4, although these joists were originally designed for a target reliability index
936 (β_o) of 2.5, the actual calculated indices using the AISI S100 Chapter K formulation and probabilistic
937 analysis yields significantly higher values, often exceeding 3.0. This discrepancy confirms that the
938 actual system reliability is higher than prescribed target values, suggesting that current member-based

939 design codes may lead to overly conservative or inefficient designs.

940 To bridge the gap between probabilistic research and engineering practice, the findings were
941 implemented within the AISI S100 Chapter K framework. By calculating system-level resistance
942 factors (ϕ) across a diverse range of target reliability indices (β_o), this study provides a practical
943 roadmap for the industry. These results illustrate how high-resolution resistance data can be seamlessly
944 translated into codified design parameters. Code committees can implement this study on the
945 variability in resistance with their own assumptions on the variability of loading demand. Ultimately,
946 the provided framework and calibrated factors offer a robust foundation for future design standards,
947 enabling more efficient, economical, and safer steel joist applications that better reflect true structural
948 performance.

A. Moment-Rotation Outcome of Varying Weld Length Ratios

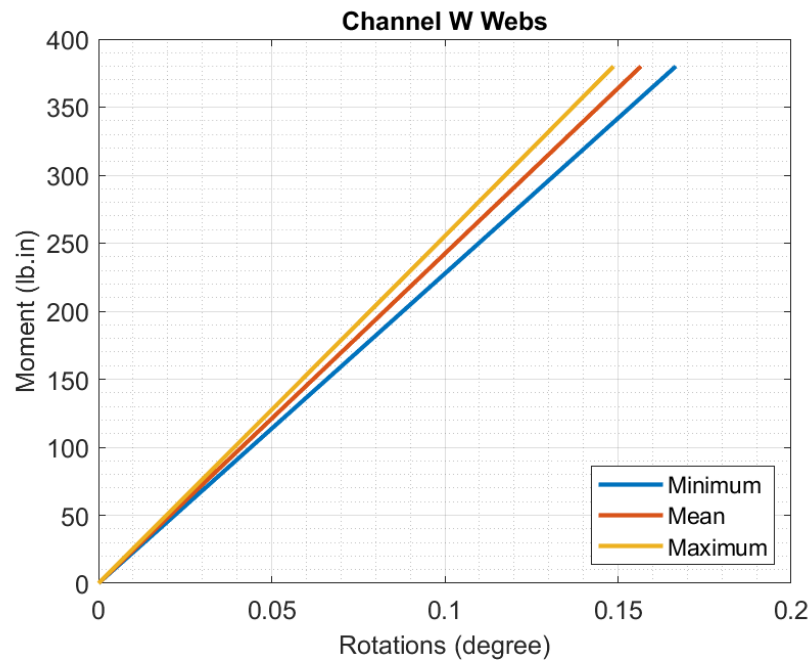


Figure A.1: Moment-rotation output for different ratio levels of weld length for channel W webs

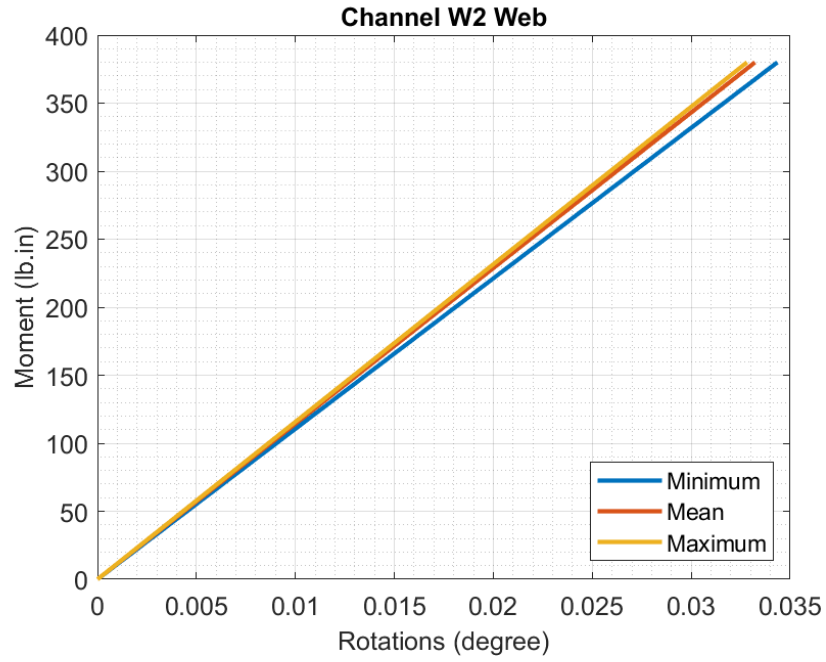


Figure A.2: Moment-rotation output for different ratio levels of weld length for channel W2 webs

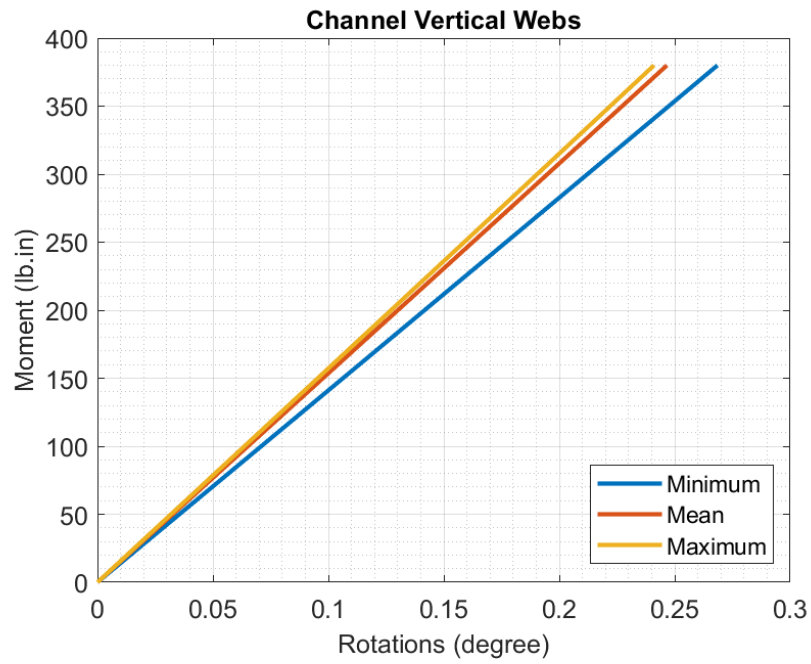


Figure A.3: Moment-rotation output for different ratio levels of weld length for channel vertical webs

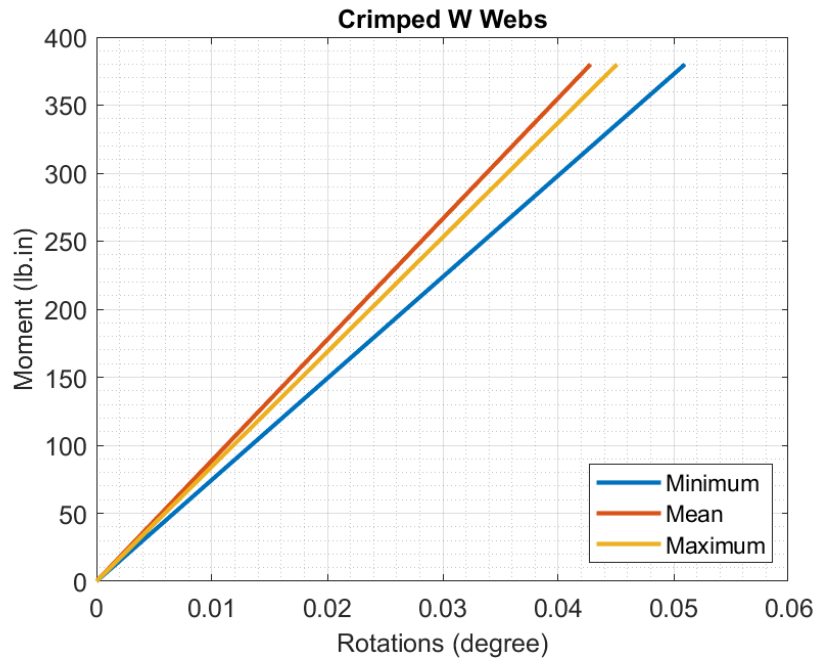


Figure A.4: Moment-rotation output for different ratio levels of weld length for crimped W webs

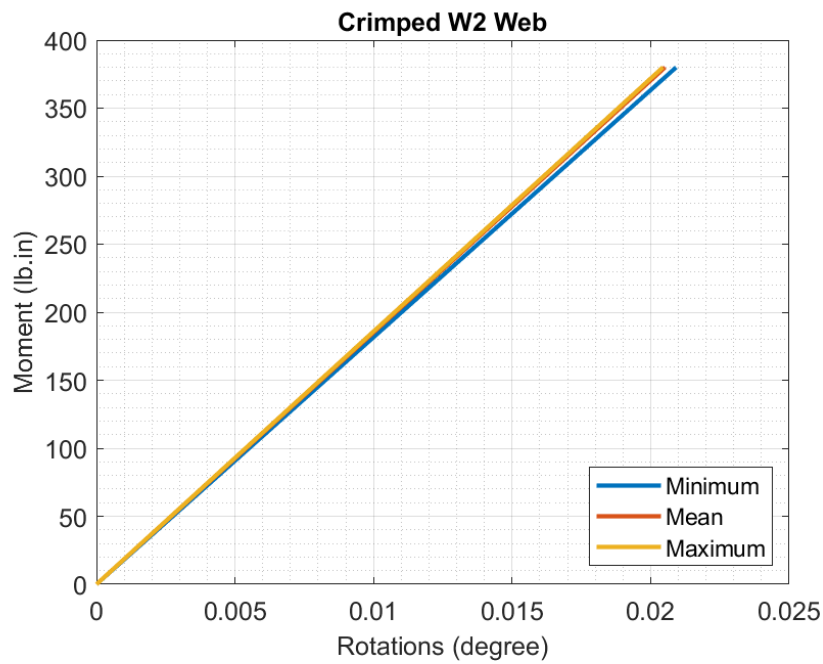


Figure A.5: Moment-rotation output for different ratio levels of weld length for crimped W2 webs

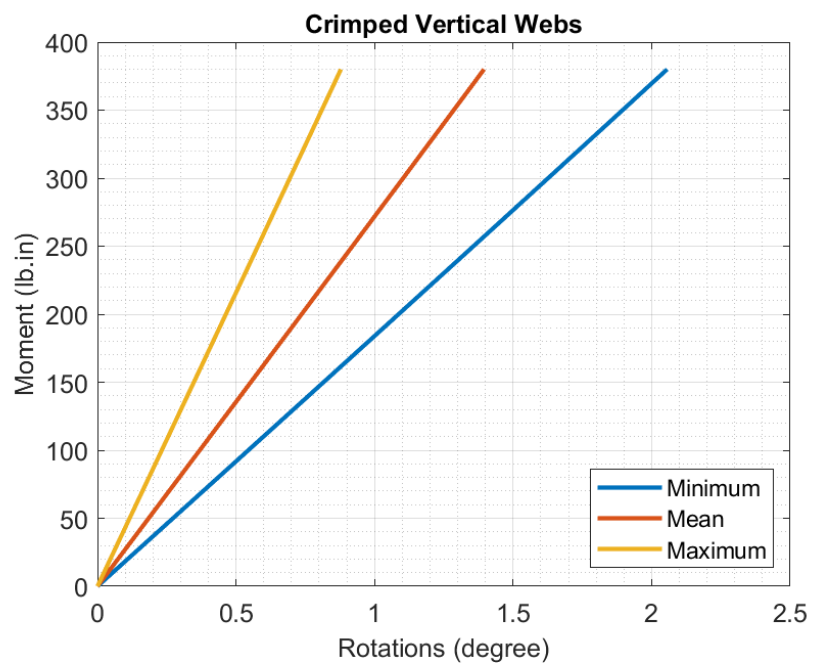


Figure A.6: Moment-rotation output for different ratio levels of weld length for crimped vertical webs

950 **B. Sensitivity Study Result Figures**

951 **B.1. Nominal Value System Sensitivity Figures**

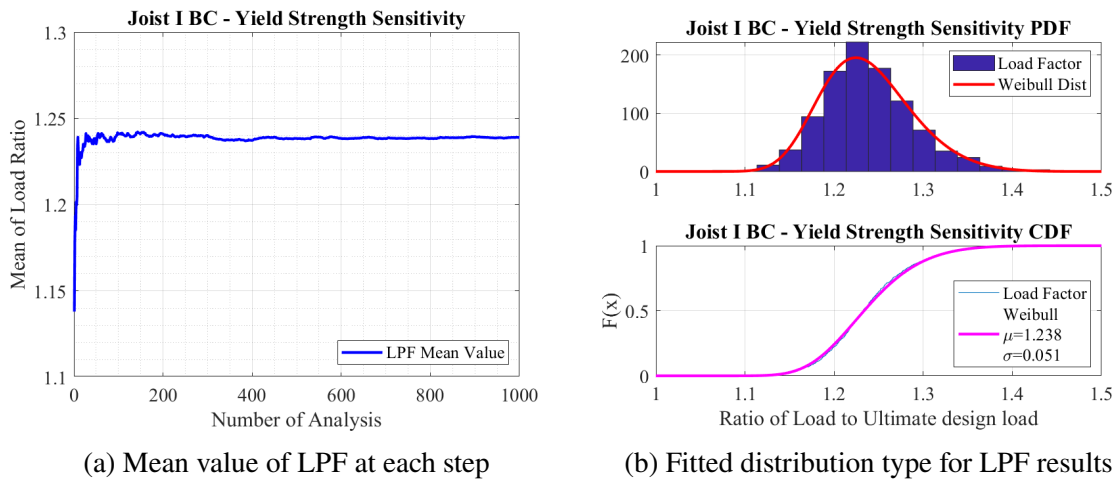
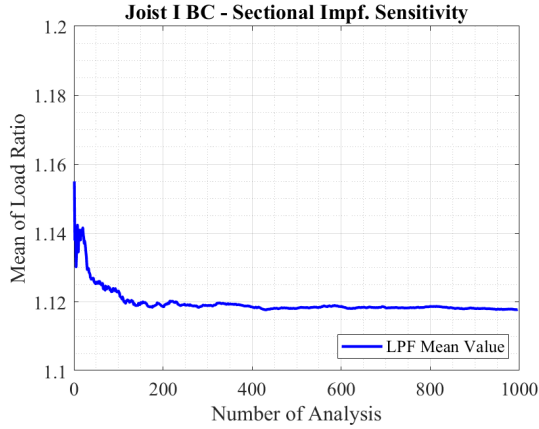
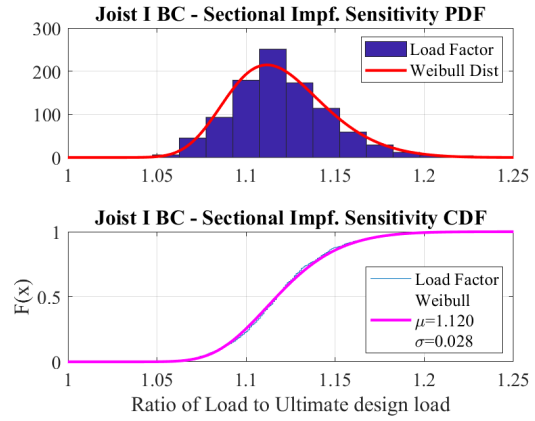


Figure B.1: Joist I BC yield strength sensitivity analyses results and fitted distribution

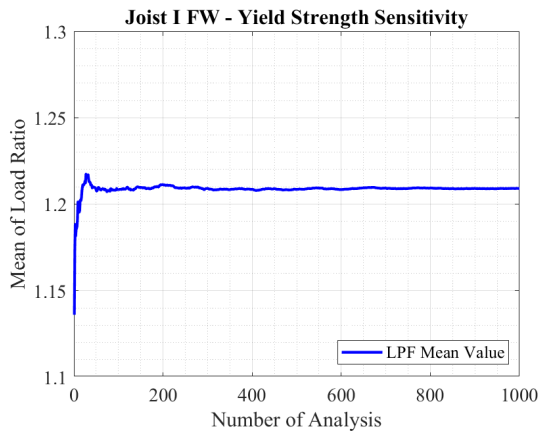


(a) Mean value of LPF at each step

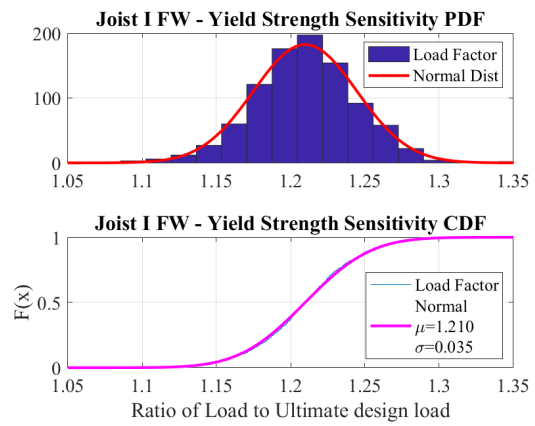


(b) Fitted distribution type for LPF results

Figure B.2: Joist I BC cross-sectional imperfection sensitivity analyses results and fitted distribution

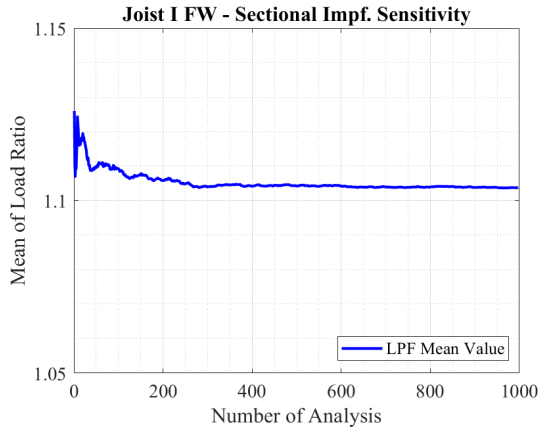


(a) Mean value of LPF at each step

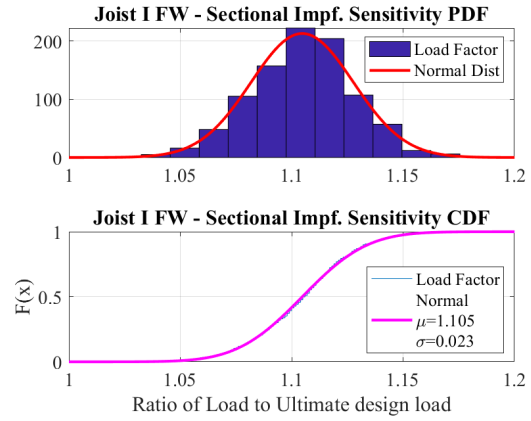


(b) Fitted distribution type for LPF results

Figure B.3: Joist I FW yield strength sensitivity analyses results and fitted distribution

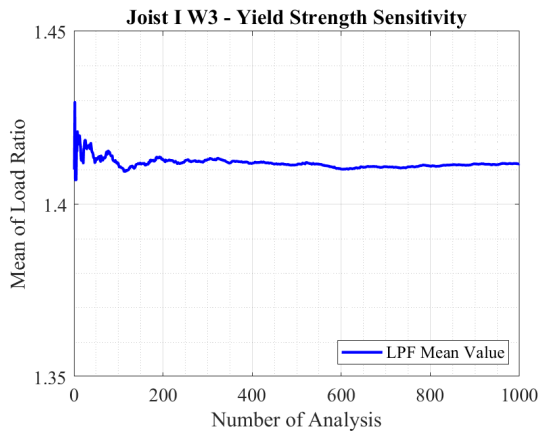


(a) Mean value of LPF at each step

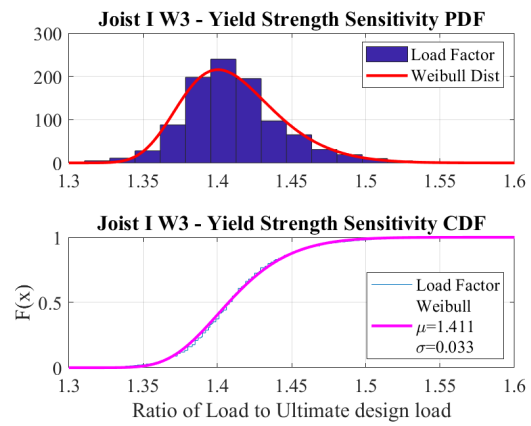


(b) Fitted distribution type for LPF results

Figure B.4: Joist I FW cross-sectional imperfection sensitivity analyses results and fitted distribution

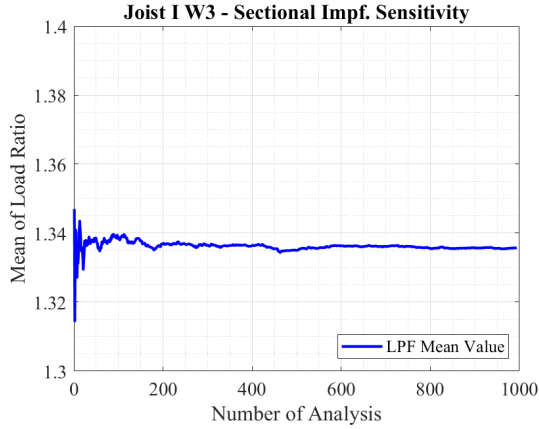


(a) Mean value of LPF at each step

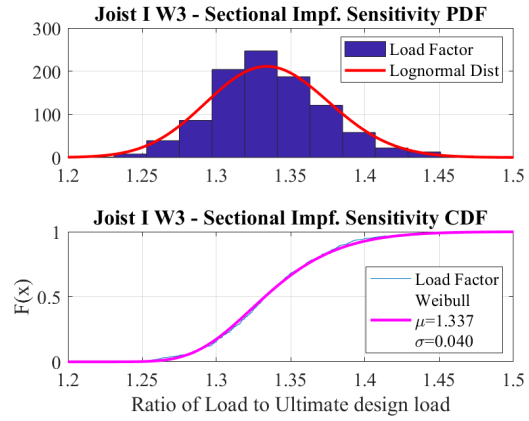


(b) Fitted distribution type for LPF results

Figure B.5: Joist I W3 yield strength sensitivity analyses results and fitted distribution

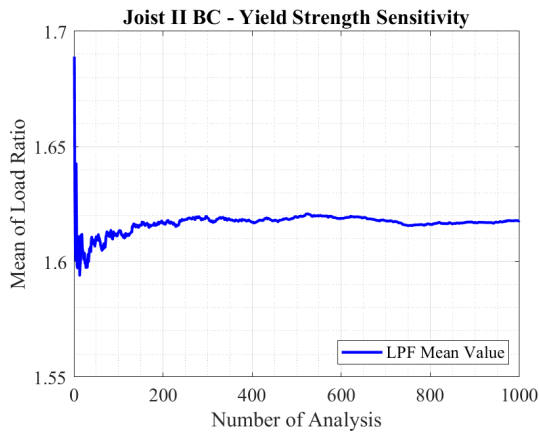


(a) Mean value of LPF at each step

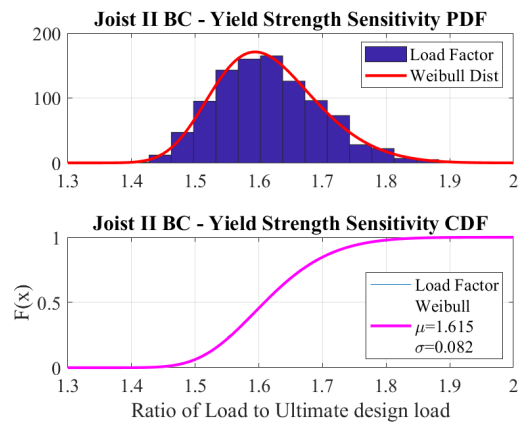


(b) Fitted distribution type for LPF results

Figure B.6: Joist I W3 cross-sectional imperfection sensitivity analyses results and fitted distribution

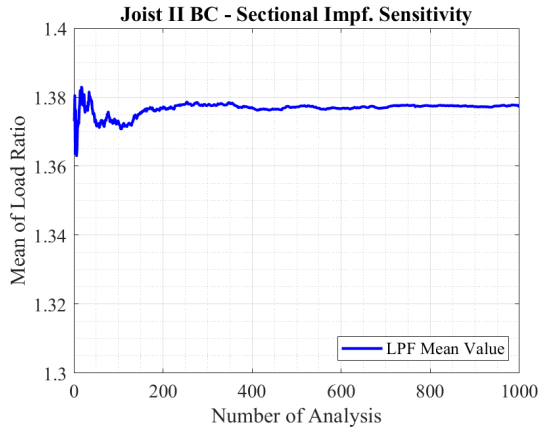


(a) Mean value of LPF at each step

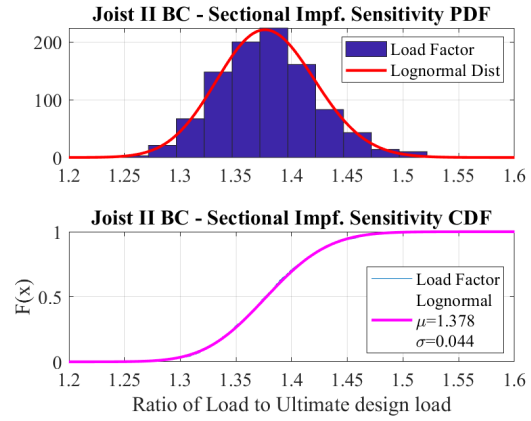


(b) Fitted distribution type for LPF results

Figure B.7: Joist II BC yield strength sensitivity analyses results and fitted distribution

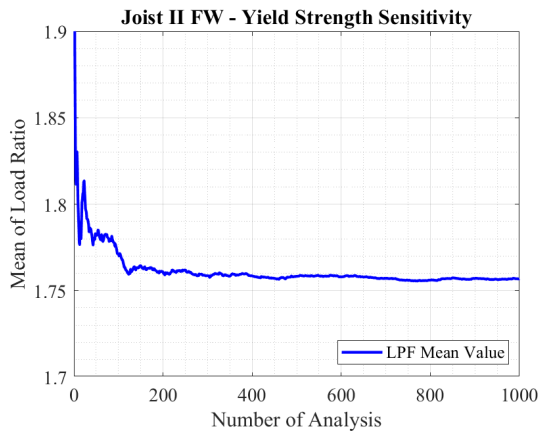


(a) Mean value of LPF at each step

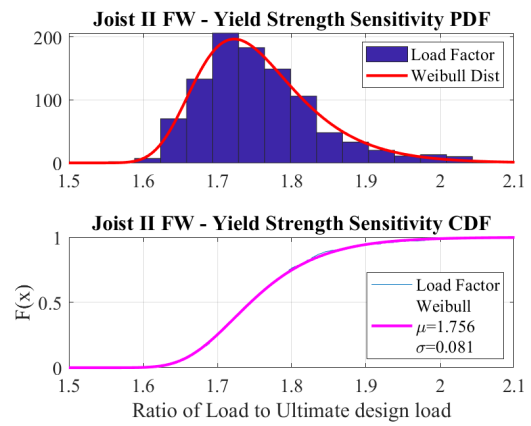


(b) Fitted distribution type for LPF results

Figure B.8: Joist II BC cross-sectional imperfection sensitivity analyses results and fitted distribution

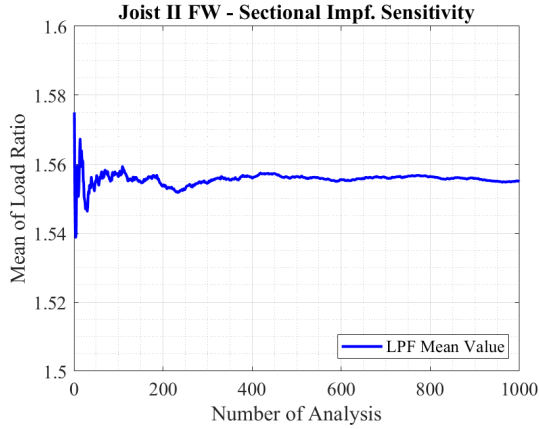


(a) Mean value of LPF at each step

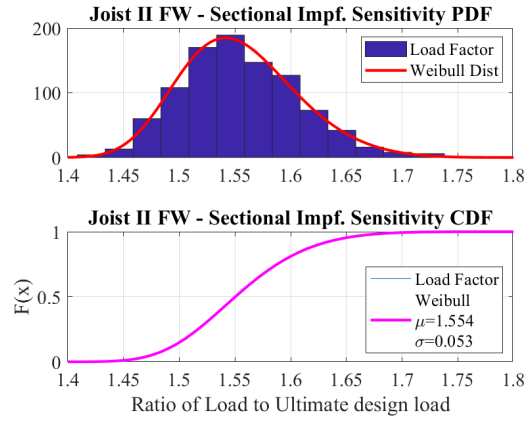


(b) Fitted distribution type for LPF results

Figure B.9: Joist II FW yield strength sensitivity analyses results and fitted distribution

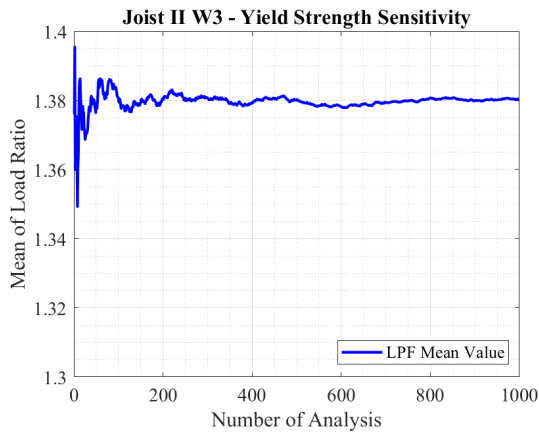


(a) Mean value of LPF at each step

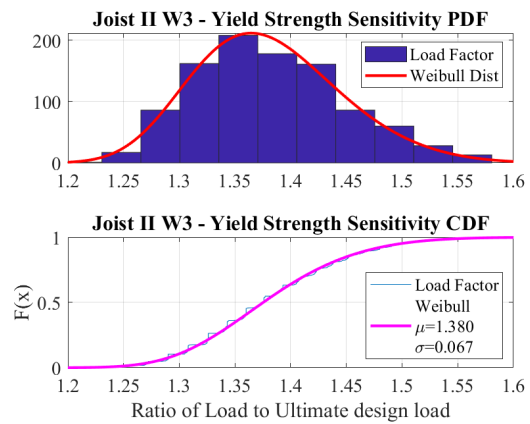


(b) Fitted distribution type for LPF results

Figure B.10: Joist II FW cross-sectional imperfection sensitivity analyses results and fitted distribution

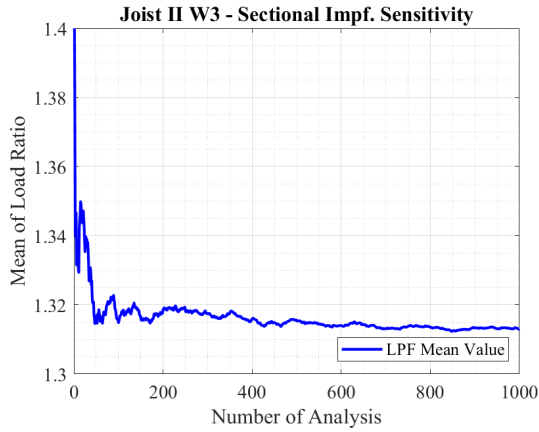


(a) Mean value of LPF at each step

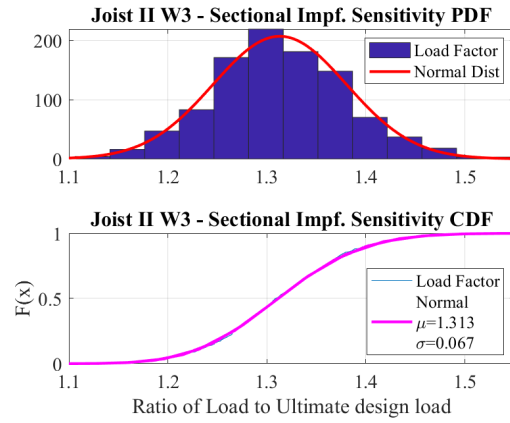


(b) Fitted distribution type for LPF results

Figure B.11: Joist II W3 yield strength sensitivity analyses results and fitted distribution



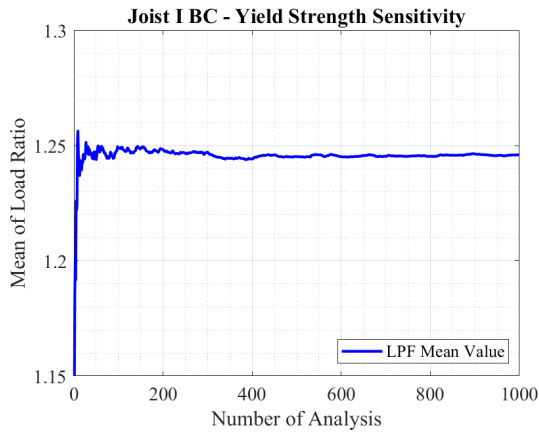
(a) Mean value of LPF at each step



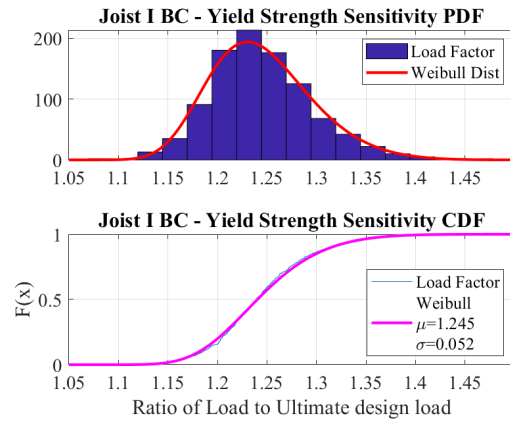
(b) Fitted distribution type for LPF results

Figure B.12: Joist II W3 cross-sectional imperfection sensitivity analyses results and fitted distribution

952 **B.2. Mean Value System Sensitivity Figures**

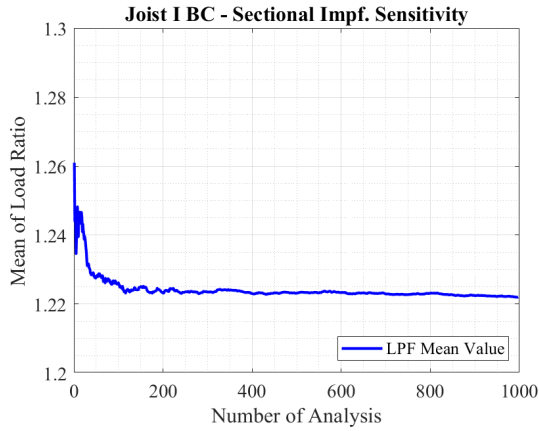


(a) Mean value of LPF at each step

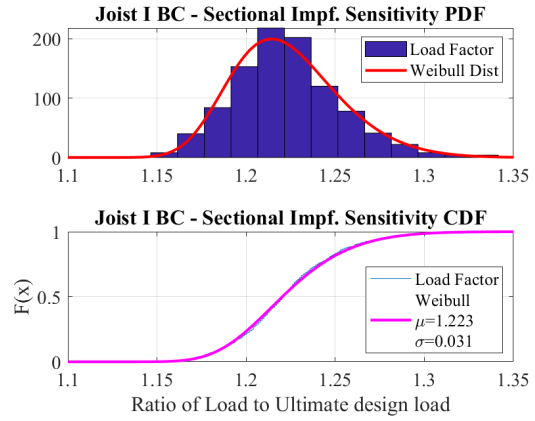


(b) Fitted distribution type for LPF results

Figure B.13: Joist I BC yield strength sensitivity analyses results and fitted distribution

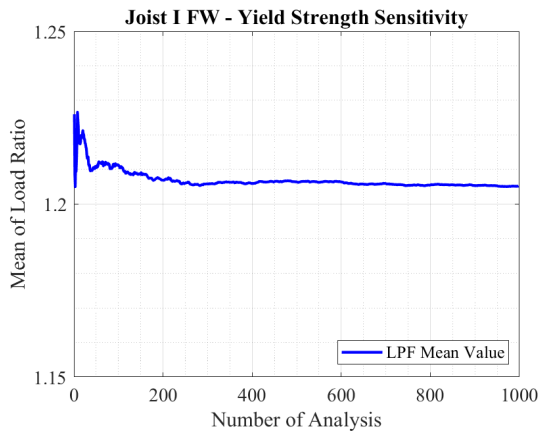


(a) Mean value of LPF at each step

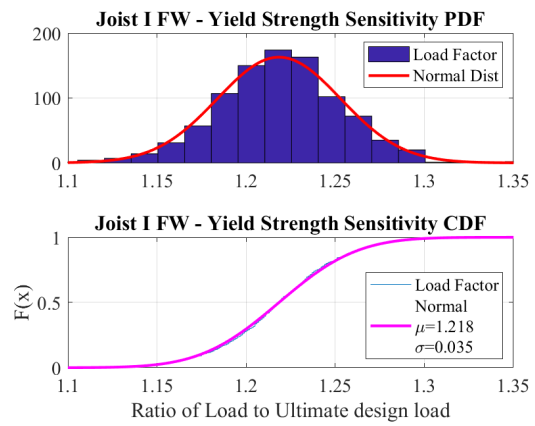


(b) Fitted distribution type for LPF results

Figure B.14: Joist I BC cross-sectional imperfection sensitivity analyses results and fitted distribution

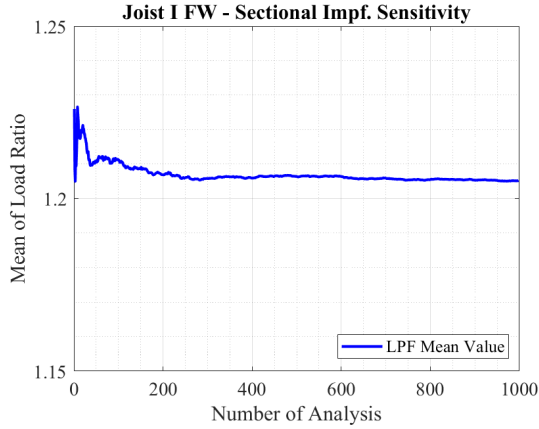


(a) Mean value of LPF at each step

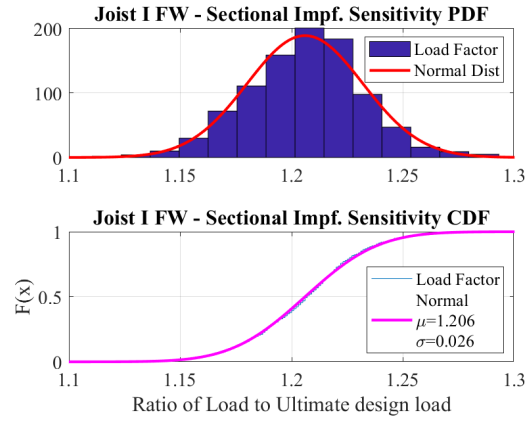


(b) Fitted distribution type for LPF results

Figure B.15: Joist I FW yield strength sensitivity analyses results and fitted distribution

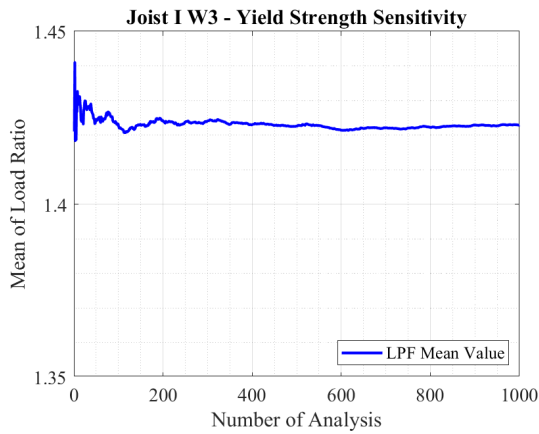


(a) Mean value of LPF at each step

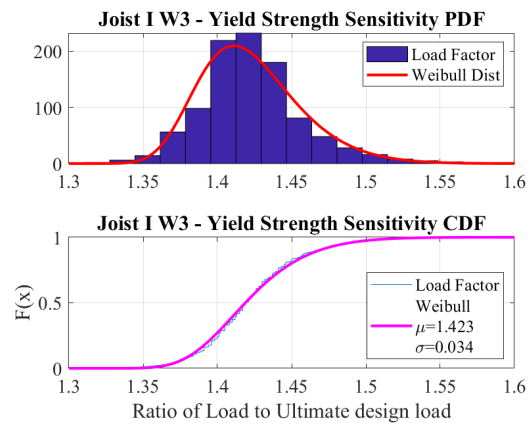


(b) Fitted distribution type for LPF results

Figure B.16: Joist I FW cross-sectional imperfection sensitivity analyses results and fitted distribution

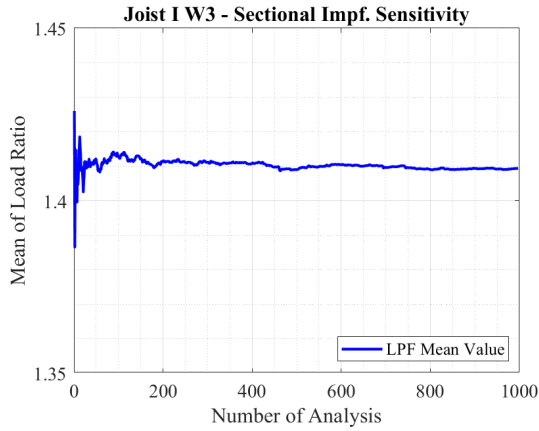


(a) Mean value of LPF at each step

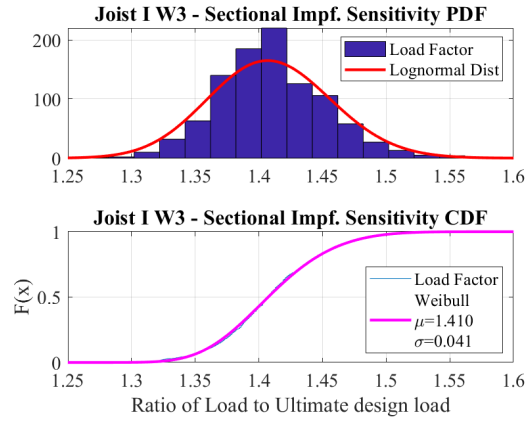


(b) Fitted distribution type for LPF results

Figure B.17: Joist I W3 yield strength sensitivity analyses results and fitted distribution

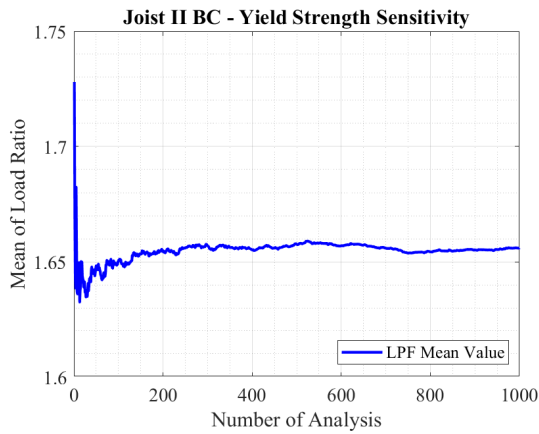


(a) Mean value of LPF at each step

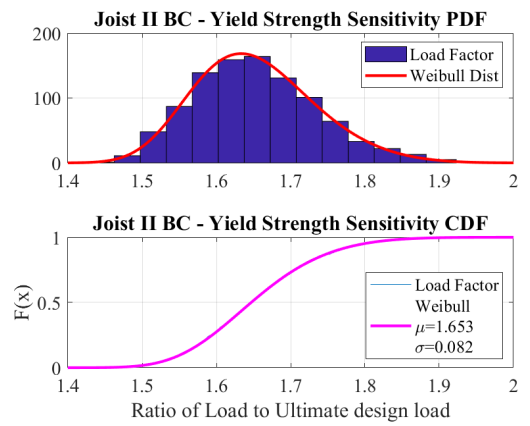


(b) Fitted distribution type for LPF results

Figure B.18: Joist I W3 cross-sectional imperfection sensitivity analyses results and fitted distribution

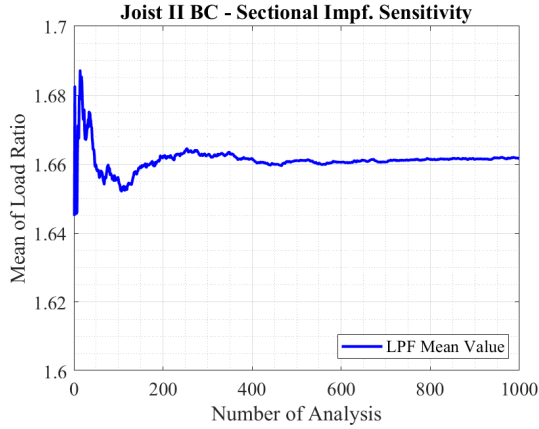


(a) Mean value of LPF at each step

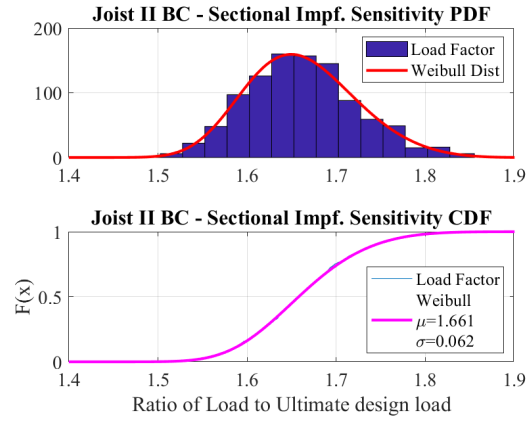


(b) Fitted distribution type for LPF results

Figure B.19: Joist II BC yield strength sensitivity analyses results and fitted distribution

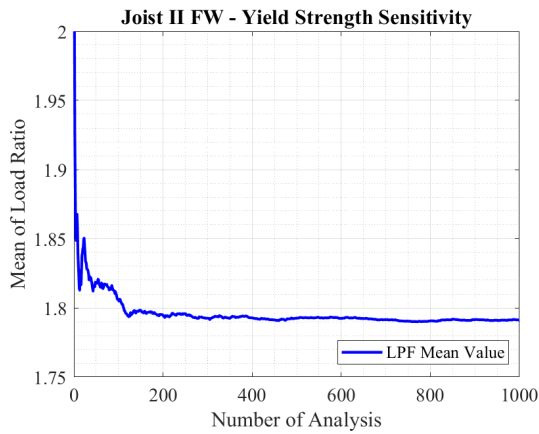


(a) Mean value of LPF at each step

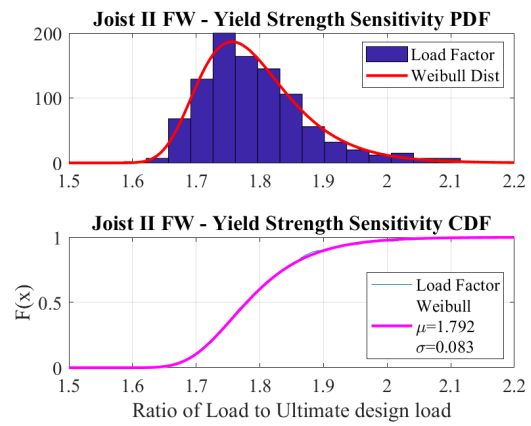


(b) Fitted distribution type for LPF results

Figure B.20: Joist II BC cross-sectional imperfection sensitivity analyses results and fitted distribution

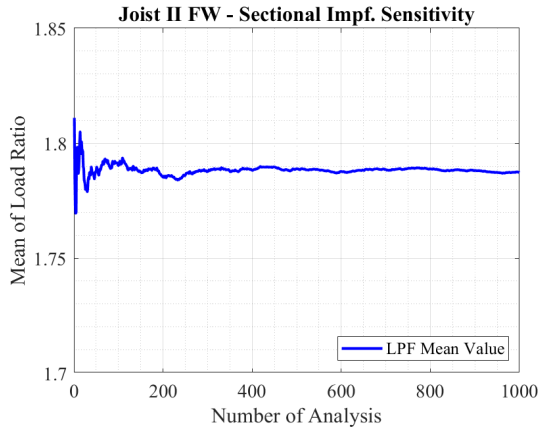


(a) Mean value of LPF at each step

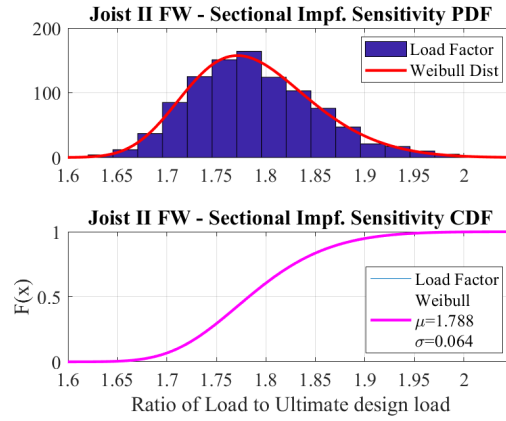


(b) Fitted distribution type for LPF results

Figure B.21: Joist II FW yield strength sensitivity analyses results and fitted distribution

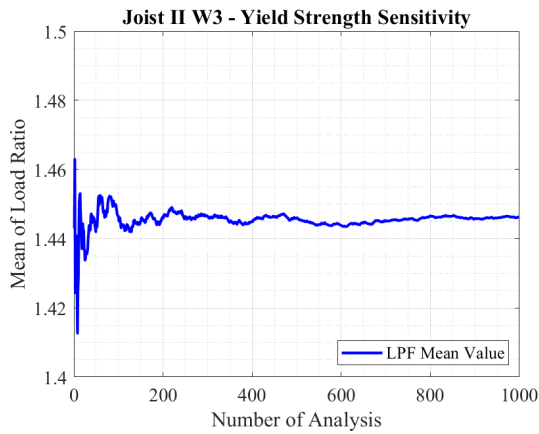


(a) Mean value of LPF at each step

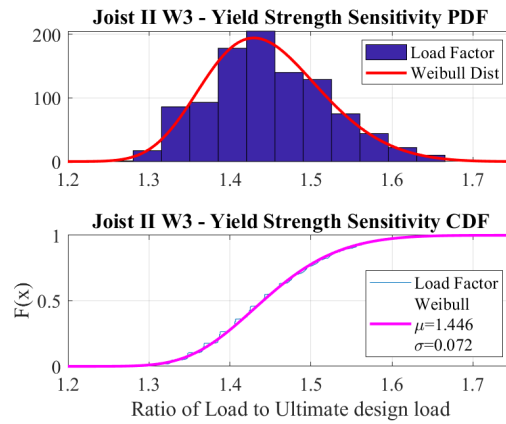


(b) Fitted distribution type for LPF results

Figure B.22: Joist II FW cross-sectional imperfection sensitivity analyses results and fitted distribution



(a) Mean value of LPF at each step



(b) Fitted distribution type for LPF results

Figure B.23: Joist II W3 yield strength sensitivity analyses results and fitted distribution

953 **B.3. Design Sheets**

STRESS ANALYSIS - PAGE 1



NEW MILLENNIUM
BUILDING SYSTEMS

Job Number: 00-0-0576	Job Name: SJI RESEARCH - SHOPORDERS	Date Run: 9/20/2022 4:31:17 PM
Location: BUTLER, IN	Joist Description: Short Span Crimp 30K9	Mark: 30K9BC

Geometry

Base Length: 50-0	Working Length: 49-8	Joist Depth: 30.00	Effective Depth: 28.90	BC Panel Length: 10 @ 4-0	Shape: Parallel Chords
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Variable	Left End	Right End
BC Panel	5-0	5-0
TC Panel	3-7	3-7
First Half	2-0	2-0
First Diag.	7-0	7-0
Depth	30.00	30.00

Loads, *** All loads are factored ***

Load Type	Category	Load1	Load2	Position	Direction	Loc/Begin	Sp/End	Reference
Uniform (plf)	LL	225.60	225.60	TC	+	0-0	50-0	L-BL
Uniform (plf)	DL	141.40	141.40	TC	+	0-0	50-0	L-BL

Stress Analysis Summary

Int. Panel TC: 24.00	Max Panel BC: 48.00	Reaction LE: 9,113.83	Reaction RE: 9,113.83	Minimum Shear: 2,278.46	Max TC Comp.: 46,980.63	Max BC Tension: 46,675.91
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Member	TC Tension	TC Compression	BC Tension	BC Compression	Web Tension	Web Comp.	Web Length	PP Dist.
W2	0.00	17,029.71	0.00	0.00	19,027.30	0.00	64.80	0-2
V1S	0.00	16,292.23	0.00	0.00	0.00	1,539.86	33.53	3-7
W3	0.00	16,292.23	22,297.86	0.00	0.00	9,624.51	37.57	5-0
W4	0.00	27,478.20	22,297.86	0.00	8,754.51	0.00	37.57	7-0
W5	0.00	27,478.20	32,049.08	0.00	0.00	7,913.33	37.57	9-0
W6	0.00	36,010.51	32,049.08	0.00	7,100.95	0.00	37.57	11-0
W7	0.00	36,010.51	39,362.49	0.00	0.00	6,317.39	37.57	13-0
W8	0.00	42,105.01	39,362.49	0.00	5,562.65	66.53	37.57	15-0
W9	0.00	42,105.01	44,238.10	0.00	561.96	4,836.72	37.57	17-0
W10	0.00	45,761.72	44,238.10	0.00	4,139.60	1,086.20	37.57	19-0
W11	0.00	45,761.72	46,675.91	0.00	1,639.25	3,471.29	37.57	21-0
W12	0.00	46,980.63	46,675.91	0.00	2,961.49	2,221.12	37.57	23-0
W12	0.00	46,980.63	46,675.90	0.00	2,961.49	2,221.12	37.57	25-0
W11	0.00	45,761.73	46,675.90	0.00	1,639.25	3,471.29	37.57	27-0
W10	0.00	45,761.73	44,238.10	0.00	4,139.60	1,086.20	37.57	29-0
W9	0.00	42,105.02	44,238.10	0.00	561.96	4,836.72	37.57	31-0
W8	0.00	42,105.02	39,362.49	0.00	5,562.65	66.53	37.57	33-0
W7	0.00	36,010.51	39,362.49	0.00	0.00	6,317.39	37.57	35-0
W6	0.00	36,010.51	32,049.08	0.00	7,100.95	0.00	37.57	37-0
W5	0.00	27,478.20	32,049.08	0.00	0.00	7,913.33	37.57	39-0
W4	0.00	27,478.20	22,297.86	0.00	8,754.51	0.00	37.57	41-0
W3	0.00	16,292.23	22,297.86	0.00	0.00	9,624.51	37.57	43-0
V1S	0.00	16,292.23	0.00	0.00	0.00	1,539.86	33.53	46-5
W2	0.00	17,029.71	0.00	0.00	19,027.30	0.00	64.80	45-0

Standard Verticals

Member	Position	Max Tension	Max Comp.	Length
V2	Interior	0.00	968.90	28.90

STRESS ANALYSIS - PAGE 2



NEW MILLENNIUM
BUILDING SYSTEMS

Job Number: 00-0-0576	Job Name: SJI RESEARCH - SHOPORDERS	Date Run: 9/20/2022 4:31:17 PM
Location: BUTLER, IN	Joist Description: Short Span Crimp 30K9	Mark: 30K9BC

Chord Properties

Chord	Area	Rx	Rz	Ryy	Y	Ix	Q	Material
TC	0.6209	0.6011	0.3559	1.2877	0.5763	0.2243	1.0000	A34A = 1.9380 x 0.176
BC	0.4776	0.5442	0.3206	1.2107	0.5190	0.1414	1.0000	A28A = 1.7500 x .150

Axial and Bending Analysis

K:	Fy:	Fb:	Mom of Inertia:	LL 360:	LL 240:	Max Bridg TC:	Max Bridg BC:
0.75	50,000.00	45,000.00	451.81	137.77	206.66	17-3 1/8	24-2 1/2

Top Chord Check	End Panel LE	First Panel LE	Interior Panel	First Panel RE	End Panel RE	Notes
Length	41.00	41.00	24.00	41.00	41.00	Gap Between Chords: 1.1250
Bending Load	367.00	367.00	367.00	367.00	367.00	Min Weld Len 2X: 0.5000
Axial Load	17,029.71	16,292.23	46,980.63	16,292.23	17,029.71	Max Load Fillers TC: 50,503.57
fa	13,713.73	13,119.85	37,832.69	13,119.85	13,713.73	Max Load no Fillers TC: 45,528.86
Maximum K L/r	68.21	115.20	33.72	115.20	68.21	TC OAL/Ryy: 462.85
Fcr	35,582.52	18,914.09	46,011.85	18,914.09	35,582.52	BC OAL/Ryy: 492.29
Fa	32,024.27	17,022.68	41,410.67	17,022.68	32,024.27	BC Stress: 1.09
F'e	61,521.02	61,521.02	319,187.78	61,521.02	61,521.02	BC L/Rz: 149.7193
Cm	0.9257	0.9289	0.9473	0.9289	0.9257	TC Shear Stress: 17,991.50
Panel Point Moment	5,709.10	5,709.10	1,468.00	5,709.10	5,709.10	BC Shear Stress: 23,711.88
Mid Panel Moment	3,809.25	2,137.33	734.00	2,137.33	3,809.25	
Panel Point fb	17,329.66	17,329.66	4,456.03	17,329.66	17,329.66	
Mid Panel fb	4,893.61	2,745.75	942.94	2,745.75	4,893.61	
Fillers	1	0	6	0	1	
Panel Point Stress	31,043.39	30,449.51	42,288.72	30,449.51	31,043.39	
Mid Panel Stress	0.5472	0.8368	0.9339	0.8368	0.5472	

Web Design

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
W2	19,027.30	19,451.71	0.00	5,599.71	5.69 x 0.150	1	C28AA = 1.125 x 1.347 x .150
W3	0.00	21,613.01	9,624.51	10,000.62	2.88 x 0.150	1	C28AA = 1.125 x 1.347 x .150
W4	8,754.51	11,808.24	0.00	5,630.10	3.74 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W5	0.00	16,380.48	7,913.33	7,969.79	2.65 x 0.134	1	C22AA = 1.125 x 1.086 x .134
W6	7,100.95	8,420.89	0.00	2,408.84	3.54 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W7	0.00	13,526.79	6,317.39	6,404.13	2.47 x 0.115	1	C18AA = 1.125 x 1.012 x .115
W8	5,562.65	7,177.20	66.53	2,000.43	3.26 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W9	561.96	11,808.24	4,836.72	5,630.10	2.07 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W10	4,139.60	7,177.20	1,086.20	2,000.43	2.42 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W11	1,639.25	11,808.24	3,471.29	5,630.10	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W12	2,961.49	8,420.89	2,221.12	2,408.84	2.00 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W12	2,961.49	8,420.89	2,221.12	2,408.84	2.00 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W11	1,639.25	11,808.24	3,471.29	5,630.10	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W10	4,139.60	7,177.20	1,086.20	2,000.43	2.42 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W9	561.96	11,808.24	4,836.72	5,630.10	2.07 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W8	5,562.65	7,177.20	66.53	2,000.43	3.26 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W7	0.00	13,526.79	6,317.39	6,404.13	2.47 x 0.115	1	C18AA = 1.125 x 1.012 x .115
W6	7,100.95	8,420.89	0.00	2,408.84	3.54 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W5	0.00	16,380.48	7,913.33	7,969.79	2.65 x 0.134	1	C22AA = 1.125 x 1.086 x .134

* Continued on Next Page...

STRESS ANALYSIS - PAGE 2



NEW MILLENNIUM
BUILDING SYSTEMS

<i>Job Number:</i> 00-0-0576	<i>Job Name:</i> SJI RESEARCH - SHOPORDERS	<i>Date Run:</i> 9/20/2022 4:31:17 PM
<i>Location:</i> BUTLER, IN	<i>Joist Description:</i> Short Span Crimp 30K9	<i>Mark:</i> 30K9BC

Web Design, Continued...

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
W4	8,754.51	11,808.24	0.00	5,630.10	3.74 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W3	0.00	21,613.01	9,624.51	10,000.62	2.88 x 0.150	1	C28AA = 1.125 x 1.347 x .150
W2	19,027.30	19,451.71	0.00	5,599.71	5.69 x 0.150	1	C28AA = 1.125 x 1.347 x .150
V1	0.00	7,177.20	1,539.86	2,511.00	2.00 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
V2	0.00	7,177.20	968.90	3,246.30	2.00 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07

STRESS ANALYSIS - PAGE 3



NEW MILLENNIUM
BUILDING SYSTEMS

Job Number: 00-0-0576	Job Name: SJI RESEARCH - SHOPORDERS	Date Run: 9/20/2022 4:31:17 PM
Location: BUTLER, IN	Joist Description: Short Span Crimp 30K9	Mark: 30K9BC

TCX Design

957 TCX Left		TCX Right	
TCX Length	0-0	TCX Length	0-0
TCX Type	R	TCX Type	R
TCX Depth	2 1/2	TCX Depth	2 1/2
BPL Length	0-4	BPL Length	0-4
Clear Bearing	0-4 1/4	Clear Bearing	0-4 3/8
BPL Material: 1714 = 1 3/4 x 1 3/4 x .143		BPL Material: 1714 = 1 3/4 x 1 3/4 x .143	
Total Load	367.00	Total Load	367.00
Reqd TL Def L/80	0.00	Reqd TL Def L/80	0.00
Live Load	225.60	Live Load	225.60
Reqd LL Def L/120	0.00	Reqd LL Def L/120	0.00
Section Modulus	0.0000	Section Modulus	0.0000
Reqd SM	0.0000	Reqd SM	0.0000
Mom of Inertia	0.0000	Mom of Inertia	0.0000
Reqd MI	0.0000	Reqd MI	0.0000
Seat Type: Lapped		Seat Type: Lapped	

Load Combinations

- Case 1a: DL
- Case 1b: 1.4(DL)
- Case 2a: LL
- Case 2b: SL
- Case 3a: 1.2(DL+CL)+1.6(TL+LL)
- Case 3b: 1.2(DL+CL)+1.6(TL+SL)
- Case 3c: 1.2(DL+CL)+1.6(TL+LL+FEM)
- Case 3d: 1.2(DL+CL)+1.6(TL+SL+FEM)
- Case 3e: DL+CL+TL+LL
- Case 3f: DL+CL+TL+SL
- Case 4a: 1.2(DL)+0.5(CL+LL)+1.6(WL+AX)+0.8(TL)
- Case 4b: 1.2(DL)+0.5(CL+LL)+1.6(WL-AX)+0.8(TL)
- Case 4c: 1.2(DL)+0.5(CL+LL)+1.6(WL+AX+IP)+0.8(TL)
- Case 4d: 1.2(DL)+0.5(CL+LL)+1.6(WL-AX+IP)+0.8(TL)
- Case 4e: 1.2(DL+CL)+1.6(WL+AX)+1.1(TL)+LL
- Case 4f: 1.2(DL+CL)+1.6(WL-AX)+1.1(TL)+LL
- Case 5a: 0.9(DL)+1.6(WL+AX)
- Case 5b: 0.9(DL)+1.6(WL-AX)
- Case 5c: 0.9(DL)+1.6(WL+AX+IP)
- Case 5d: 0.9(DL)+1.6(WL-AX+IP)
- Case 5e: 0.9(DL)+SM+AX
- Case 5f: 0.9(DL)+SM-AX
- Case 6a: 1.2(DL)+0.5(CL+SL)+1.6(WL+AX)+0.8(TL)
- Case 6b: 1.2(DL)+0.5(CL+SL)+1.6(WL-AX)+0.8(TL)
- Case 6c: 1.2(DL)+0.5(CL+SL)+1.6(WL+C+AX+IP)+0.8(TL)
- Case 6d: 1.2(DL)+0.5(CL+SL)+1.6(WL+C-AX+IP)+0.8(TL)
- Case 6e: 1.2(DL)+0.5(CL+SL)+1.6(WL+AX+IP)+0.8(TL)
- Case 6f: 1.2(DL)+0.5(CL+SL)+1.6(WL-AX+IP)+0.8(TL)
- Case 7a: 1.2(DL+CL)+0.8(WL+AX)+1.6(TL+LL)
- Case 7b: 1.2(DL+CL)+0.8(WL-AX)+1.6(TL+LL)
- Case 7c: 1.2(DL+CL)+0.8(WL+C+AX+IP)+1.6(TL+LL)
- Case 7d: 1.2(DL+CL)+0.8(WL+C-AX+IP)+1.6(TL+LL)
- Case 7e: 1.2(DL+CL)+0.8(WL+AX+IP)+1.6(TL+LL)
- Case 7f: 1.2(DL+CL)+0.8(WL-AX+IP)+1.6(TL+LL)
- Case 8a: 1.2(DL+CL)+0.8(WL+AX)+1.6(TL+SL)
- Case 8b: 1.2(DL+CL)+0.8(WL-AX)+1.6(TL+SL)
- Case 8c: 1.2(DL+CL)+0.8(WL+C+AX+IP)+1.6(TL+SL)
- Case 8d: 1.2(DL+CL)+0.8(WL+C-AX+IP)+1.6(TL+SL)
- Case 8e: 1.2(DL+CL)+0.8(WL+AX+IP)+1.6(TL+SL)
- Case 8f: 1.2(DL+CL)+0.8(WL-AX+IP)+1.6(TL+SL)
- Case 9a: 1.2(DL+CL)+0.7(LL)+0.9(TL)+SM+AX+FEM
- Case 9b: 1.2(DL+CL)+0.7(LL)+0.9(TL)+SM-AX+FEM
- Case 9c: 1.2(DL+CL)+0.7(SL)+0.9(TL)+SM+AX+FEM
- Case 9d: 1.2(DL+CL)+0.7(SL)+0.9(TL)+SM-AX+FEM
- Case 9e: 1.2(DL+CL)+LL+1.1(TL)+SM+AX+FEM
- Case 9f: 1.2(DL+CL)+LL+1.1(TL)+SM-AX+FEM
- Case 10a: 1.2(DL)+SM+AX
- Case 10b: 1.2(DL)+SM-AX
- Case 10c: 1.2(DL+CL)+SM+AX
- Case 10d: 1.2(DL+CL)+SM-AX

STRESS ANALYSIS - PAGE 1



NEW MILLENNIUM
BUILDING SYSTEMS

Job Number: 00-0-0576	Job Name: SJI RESEARCH - SHOPORDERS	Date Run: 9/20/2022 4:34:44 PM
Location: BUTLER, IN	Joist Description: Short Span Crimp 30K9	Mark: 30K9W2

Geometry

Base Length: 50-0	Working Length: 49-8	Joist Depth: 30.00	Effective Depth: 28.89	BC Panel Length: 10 @ 4-0	Shape: Parallel Chords
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Variable	Left End	Right End
BC Panel	5-0	5-0
TC Panel	3-7	3-7
First Half	2-0	2-0
First Diag.	7-0	7-0
Depth	30.00	30.00

Loads, *** All loads are factored ***

Load Type	Category	Load1	Load2	Position	Direction	Loc/Begin	Sp/End	Reference
Uniform (plf)	LL	225.60	225.60	TC	+	0-0	50-0	L-BL
Uniform (plf)	DL	141.40	141.40	TC	+	0-0	50-0	L-BL

Stress Analysis Summary

Int. Panel TC: 24.00	Max Panel BC: 48.00	Reaction LE: 9,113.83	Reaction RE: 9,113.83	Minimum Shear: 2,278.46	Max TC Comp.: 47,010.39	Max BC Tension: 46,705.48
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Member	TC Tension	TC Compression	BC Tension	BC Compression	Web Tension	Web Comp.	Web Length	PP Dist.
W2	0.00	17,040.50	0.00	0.00	19,036.96	0.00	64.80	0-2
V1S	0.00	16,302.56	0.00	0.00	0.00	1,540.15	33.52	3-7
W3	0.00	16,302.56	22,311.99	0.00	0.00	9,627.00	37.56	5-0
W4	0.00	27,495.61	22,311.99	0.00	8,756.77	0.00	37.56	7-0
W5	0.00	27,495.61	32,069.38	0.00	0.00	7,915.37	37.56	9-0
W6	0.00	36,033.32	32,069.38	0.00	7,102.79	0.00	37.56	11-0
W7	0.00	36,033.32	39,387.43	0.00	0.00	6,319.03	37.56	13-0
W8	0.00	42,131.70	39,387.43	0.00	5,564.09	66.55	37.56	15-0
W9	0.00	42,131.70	44,266.13	0.00	562.10	4,837.97	37.56	17-0
W10	0.00	45,790.73	44,266.13	0.00	4,140.67	1,086.48	37.56	19-0
W11	0.00	45,790.73	46,705.48	0.00	1,639.67	3,472.19	37.56	21-0
W12	0.00	47,010.39	46,705.48	0.00	2,962.26	2,221.69	37.56	23-0
W12	0.00	47,010.39	46,705.48	0.00	2,962.26	2,221.69	37.56	25-0
W11	0.00	45,790.72	46,705.48	0.00	1,639.67	3,472.19	37.56	27-0
W10	0.00	45,790.72	44,266.13	0.00	4,140.67	1,086.48	37.56	29-0
W9	0.00	42,131.70	44,266.13	0.00	562.10	4,837.97	37.56	31-0
W8	0.00	42,131.70	39,387.43	0.00	5,564.09	66.55	37.56	33-0
W7	0.00	36,033.33	39,387.43	0.00	0.00	6,319.03	37.56	35-0
W6	0.00	36,033.33	32,069.39	0.00	7,102.79	0.00	37.56	37-0
W5	0.00	27,495.61	32,069.39	0.00	0.00	7,915.37	37.56	39-0
W4	0.00	27,495.61	22,311.99	0.00	8,756.77	0.00	37.56	41-0
W3	0.00	16,302.56	22,311.99	0.00	0.00	9,627.00	37.56	43-0
V1S	0.00	16,302.56	0.00	0.00	0.00	1,540.15	33.52	46-5
W2	0.00	17,040.50	0.00	0.00	19,036.96	0.00	64.80	45-0

Standard Verticals

Member	Position	Max Tension	Max Comp.	Length
V2	Interior	0.00	969.05	28.89

STRESS ANALYSIS - PAGE 2



NEW MILLENNIUM
BUILDING SYSTEMS

Job Number: 00-0-0576	Job Name: SJI RESEARCH - SHOPORDERS	Date Run: 9/20/2022 4:34:44 PM
Location: BUTLER, IN	Joist Description: Short Span Crimp 30K9	Mark: 30K9W2

Chord Properties

Chord	Area	Rx	Rz	Ryy	Y	Ix	Q	Material
TC	0.6209	0.6011	0.3559	1.2877	0.5763	0.2243	1.0000	A34A = 1.9380 x 0.176
BC	0.5181	0.5633	0.3325	1.2357	0.5373	0.1644	1.0000	A30A = 1.8125 x .157

Axial and Bending Analysis

K:	Fy:	Fb:	Mom of Inertia:	LL 360:	LL 240:	Max Bridg TC:	Max Bridg BC:
0.75	50,000.00	45,000.00	472.11	143.96	215.94	17-3 1/8	24-8 1/2

Top Chord Check	End Panel LE	First Panel LE	Interior Panel	First Panel RE	End Panel RE	Gap Between Chords:
Length	41.00	41.00	24.00	41.00	41.00	1.1250
Bending Load	367.00	367.00	367.00	367.00	367.00	Min Weld Len 2X: 0.5000
Axial Load	17,040.50	16,302.56	47,010.39	16,302.56	17,040.50	Max Load Fillers TC: 50,503.57
fa	13,722.42	13,128.17	37,856.65	13,128.17	13,722.42	Max Load no Fillers TC: 45,528.86
Maximum K L/r	68.21	115.20	33.72	115.20	68.21	TC OAL/Ryy: 462.85
Fcr	35,582.52	18,914.09	46,011.85	18,914.09	35,582.52	BC OAL/Ryy: 482.33
Fa	32,024.27	17,022.68	41,410.67	17,022.68	32,024.27	BC Stress: 1.00
F'e	61,521.02	61,521.02	319,187.78	61,521.02	61,521.02	BC L/Rz: 144.3609
Cm	0.9256	0.9289	0.9473	0.9289	0.9256	TC Shear Stress: 17,993.16
Panel Point Moment	5,709.10	5,709.10	1,468.00	5,709.10	5,709.10	BC Shear Stress: 21,740.25
Mid Panel Moment	3,809.25	2,137.33	734.00	2,137.33	3,809.25	
Panel Point fb	17,329.66	17,329.66	4,456.03	17,329.66	17,329.66	
Mid Panel fb	4,893.61	2,745.75	942.94	2,745.75	4,893.61	
Fillers	1	0	6	0	1	
Panel Point Stress	31,052.08	30,457.83	42,312.68	30,457.82	31,052.08	
Mid Panel Stress	0.5475	0.8373	0.9345	0.8373	0.5475	

Web Design

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
* W2 *	19,036.96	14,742.43	0.00	3,629.88	6.38 x 0.134	1	C22AA = 1.125 x 1.086 x .134
W3	0.00	21,613.01	9,627.00	10,004.19	2.88 x 0.150	1	C28AA = 1.125 x 1.347 x .150
W4	8,756.77	11,808.24	0.00	5,632.08	3.74 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W5	0.00	16,380.48	7,915.37	7,972.61	2.65 x 0.134	1	C22AA = 1.125 x 1.086 x .134
W6	7,102.79	8,420.89	0.00	2,410.64	3.54 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W7	0.00	13,526.79	6,319.03	6,406.39	2.47 x 0.115	1	C18AA = 1.125 x 1.012 x .115
W8	5,564.09	7,177.20	66.55	2,001.93	3.26 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W9	562.10	11,808.24	4,837.97	5,632.08	2.07 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W10	4,140.67	7,177.20	1,086.48	2,001.93	2.42 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W11	1,639.67	11,808.24	3,472.19	5,632.08	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W12	2,962.26	8,420.89	2,221.69	2,410.64	2.00 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W12	2,962.26	8,420.89	2,221.69	2,410.64	2.00 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W11	1,639.67	11,808.24	3,472.19	5,632.08	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W10	4,140.67	7,177.20	1,086.48	2,001.93	2.42 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W9	562.10	11,808.24	4,837.97	5,632.08	2.07 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W8	5,564.09	7,177.20	66.55	2,001.93	3.26 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
W7	0.00	13,526.79	6,319.03	6,406.39	2.47 x 0.115	1	C18AA = 1.125 x 1.012 x .115
W6	7,102.79	8,420.89	0.00	2,410.64	3.54 x 0.090	1	C12AA = 1.125 x 0.715 x .090
W5	0.00	16,380.48	7,915.37	7,972.61	2.65 x 0.134	1	C22AA = 1.125 x 1.086 x .134

* Continued on Next Page...

STRESS ANALYSIS - PAGE 2



NEW MILLENNIUM
BUILDING SYSTEMS

<i>Job Number:</i> 00-0-0576	<i>Job Name:</i> SJI RESEARCH - SHOPORDERS	<i>Date Run:</i> 9/20/2022 4:34:44 PM
<i>Location:</i> BUTLER, IN	<i>Joist Description:</i> Short Span Crimp 30K9	<i>Mark:</i> 30K9W2

Web Design, Continued...

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
W4	8,756.77	11,808.24	0.00	5,632.08	3.74 x 0.105	1	C16AA = 1.125 x 0.943 x .105
W3	0.00	21,613.01	9,627.00	10,004.19	2.88 x 0.150	1	C28AA = 1.125 x 1.347 x .150
W2	19,036.96	19,451.71	0.00	5,600.82	5.70 x 0.150	1	C28AA = 1.125 x 1.347 x .150
V1	0.00	7,177.20	1,540.15	2,513.36	2.00 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07
V2	0.00	7,177.20	969.05	3,249.33	2.00 x 0.077	1	C10AA = 1.125 x 0.700 x 0.07

STRESS ANALYSIS - PAGE 3



NEW MILLENNIUM
BUILDING SYSTEMS

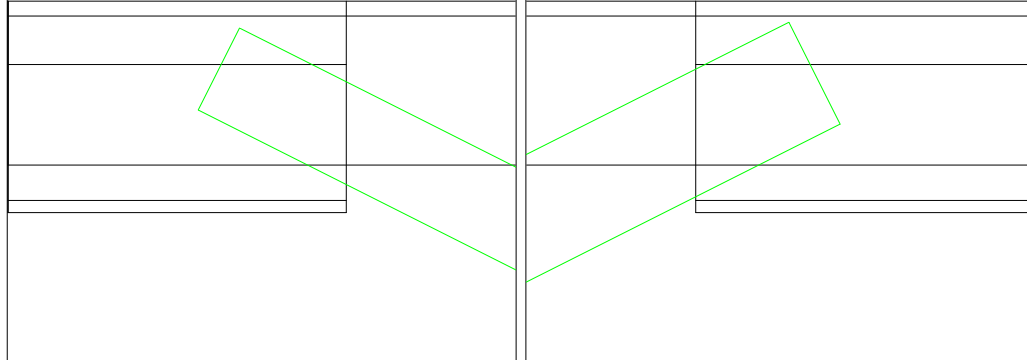
Job Number: 00-0-0576	Job Name: SJI RESEARCH - SHOPORDERS	Date Run: 9/20/2022 4:34:44 PM
Location: BUTLER, IN	Joist Description: Short Span Crimp 30K9	Mark: 30K9W2

TCX Design

961 TCX Left		TCX Right	
TCX Length	0-0	TCX Length	0-0
TCX Type	R	TCX Type	R
TCX Depth	2 1/2	TCX Depth	2 1/2
BPL Length	0-4	BPL Length	0-4
Clear Bearing	0-4 5/8	Clear Bearing	0-4 3/8
BPL Material: 1714 = 1 3/4 x 1 3/4 x .143		BPL Material: 1714 = 1 3/4 x 1 3/4 x .143	

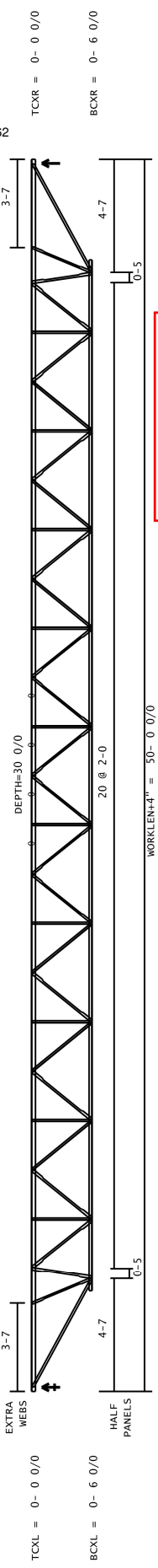
Total Load	367.00	Total Load	367.00
Reqd TL Def L/80	0.00	Reqd TL Def L/80	0.00
Live Load	225.60	Live Load	225.60
Reqd LL Def L/120	0.00	Reqd LL Def L/120	0.00
Section Modulus	0.0000	Section Modulus	0.0000
Reqd SM	0.0000	Reqd SM	0.0000
Mom of Inertia	0.0000	Mom of Inertia	0.0000
Reqd MI	0.0000	Reqd MI	0.0000

Seat Type: Lapped



Load Combinations

- Case 1a: DL
- Case 1b: 1.4(DL)
- Case 2a: LL
- Case 2b: SL
- Case 3a: 1.2(DL+CL)+1.6(TL+LL)
- Case 3b: 1.2(DL+CL)+1.6(TL+SL)
- Case 3c: 1.2(DL+CL)+1.6(TL+LL+FEM)
- Case 3d: 1.2(DL+CL)+1.6(TL+SL+FEM)
- Case 3e: DL+CL+TL+LL
- Case 3f: DL+CL+TL+SL
- Case 4a: 1.2(DL)+0.5(CL+LL)+1.6(WL+AX)+0.8(TL)
- Case 4b: 1.2(DL)+0.5(CL+LL)+1.6(WL-AX)+0.8(TL)
- Case 4c: 1.2(DL)+0.5(CL+LL)+1.6(WL+AX+IP)+0.8(TL)
- Case 4d: 1.2(DL)+0.5(CL+LL)+1.6(WL-AX+IP)+0.8(TL)
- Case 4e: 1.2(DL+CL)+1.6(WL+AX)+1.1(TL)+LL
- Case 4f: 1.2(DL+CL)+1.6(WL-AX)+1.1(TL)+LL
- Case 5a: 0.9(DL)+1.6(WL+AX)
- Case 5b: 0.9(DL)+1.6(WL-AX)
- Case 5c: 0.9(DL)+1.6(WL+AX+IP)
- Case 5d: 0.9(DL)+1.6(WL-AX+IP)
- Case 5e: 0.9(DL)+SM+AX
- Case 5f: 0.9(DL)+SM-AX
- Case 6a: 1.2(DL)+0.5(CL+SL)+1.6(WL+AX)+0.8(TL)
- Case 6b: 1.2(DL)+0.5(CL+SL)+1.6(WL-AX)+0.8(TL)
- Case 6c: 1.2(DL)+0.5(CL+SL)+1.6(WL+C+AX+IP)+0.8(TL)
- Case 6d: 1.2(DL)+0.5(CL+SL)+1.6(WL+C-AX+IP)+0.8(TL)
- Case 6e: 1.2(DL)+0.5(CL+SL)+1.6(WL+AX+IP)+0.8(TL)
- Case 6f: 1.2(DL)+0.5(CL+SL)+1.6(WL-AX+IP)+0.8(TL)
- Case 7a: 1.2(DL+CL)+0.8(WL+AX)+1.6(TL+LL)
- Case 7b: 1.2(DL+CL)+0.8(WL-AX)+1.6(TL+LL)
- Case 7c: 1.2(DL+CL)+0.8(WL+C+AX+IP)+1.6(TL+LL)
- Case 7d: 1.2(DL+CL)+0.8(WL+C-AX+IP)+1.6(TL+LL)
- Case 7e: 1.2(DL+CL)+0.8(WL+AX+IP)+1.6(TL+LL)
- Case 7f: 1.2(DL+CL)+0.8(WL-AX+IP)+1.6(TL+LL)
- Case 8a: 1.2(DL+CL)+0.8(WL+AX)+1.6(TL+SL)
- Case 8b: 1.2(DL+CL)+0.8(WL-AX)+1.6(TL+SL)
- Case 8c: 1.2(DL+CL)+0.8(WL+C+AX+IP)+1.6(TL+SL)
- Case 8d: 1.2(DL+CL)+0.8(WL+C-AX+IP)+1.6(TL+SL)
- Case 8e: 1.2(DL+CL)+0.8(WL+AX+IP)+1.6(TL+SL)
- Case 8f: 1.2(DL+CL)+0.8(WL-AX+IP)+1.6(TL+SL)
- Case 9a: 1.2(DL+CL)+0.7(LL)+0.9(TL)+SM+AX+FEM
- Case 9b: 1.2(DL+CL)+0.7(LL)+0.9(TL)+SM-AX+FEM
- Case 9c: 1.2(DL+CL)+0.7(SL)+0.9(TL)+SM+AX+FEM
- Case 9d: 1.2(DL+CL)+0.7(SL)+0.9(TL)+SM-AX+FEM
- Case 9e: 1.2(DL+CL)+LL+1.1(TL)+SM+AX+FEM
- Case 9f: 1.2(DL+CL)+LL+1.1(TL)+SM-AX+FEM
- Case 10a: 1.2(DL)+SM+AX
- Case 10b: 1.2(DL)+SM-AX
- Case 10c: 1.2(DL+CL)+SM+AX
- Case 10d: 1.2(DL+CL)+SM-AX



APPLIED LOADS

(D)Dead (Lr)Roof Live
 *** UNFACTORED UNIFORM LOADS (PLF) ***
 MAIN DESIG: 245 UNFACTORED TOTAL / 141 DEFL L/L7/5/R
 START LENGTH
 0-0 0/0 50-0 0/0
 LOAD COMBINATIONS
 1=1.0D+1.0Lr 2=0.56D+1.0W 3=0.78D+0.75W

DEFLECTION DATA

DEFLECTION -- MAINSPAN --
 LIMITS (L/360) F --
 MAXIMA -1.67

ADDITIONAL DESIGN DATA

LOAD COMBINATIONS FROM: IBC 2018
 JOIST DESIGNED WITH: ASD
 JOIST IXX DEV = 458. IN^4 JOIST EFF. DEPTH= 29.00 IN
 ALLOW LYY STRESS 16.4 FT
 TOP CHORD= 4.5 FT
 BOT CHORD= 20.8 FT
 TOP CHORD BRIDGING REQ= 2 ROWS HORIZ., 1 ROW BOLTED-'EX'
 BOT CHORD BRIDGING REQ= 3 ROWS
 MAX LE END REACTION= 6084 lbs
 MAX RE END REACTION= 6084 lbs
 STANDARD SJI CAMBER= 1 0/0''

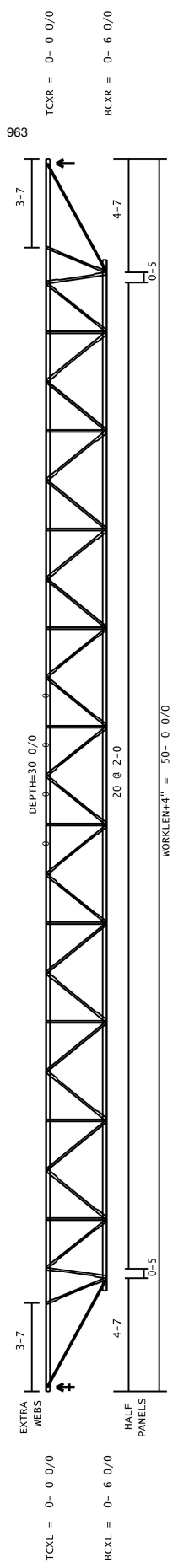
CHORD DATA

TOP CHORD= 2L 2 X 2 X 1/2X1-1/2X-170 X.163 FY= 50 KSI
 BOT CHORD= 2L 1-1/2X1-1/2X-170 FY= 50 KSI

TC MEM	REQ AXIAL	MP RATIO	BC MEM	REQ AXIAL	MP RATIO
1	-10497	0.67	1	+10988	0.52
2	-10145	0.59	2	+18314	0.74
3	-14877	0.52	3	+23993	0.91
4	-21358	0.58	4	+28048	1.02
5	-21358	0.77	5	+30580	1.08
6	-26233	0.80	6	+30280	1.08
7	-26233	0.84	7	+28048	1.02
8	-29467	0.88	8	+23993	0.91
9	-29467	0.91	9	+18314	0.74
10	-31089	0.93	10	+10988	0.52
11	-31089	0.93	11		
12	-31089	0.93			
13	-31089	0.93			
14	-29467	0.91			
15	-29467	0.88			
16	-26233	0.84			
17	-26233	0.84			
18	-21358	0.77			
19	-21358	0.67			
20	-14877	0.58			
21	-14877	0.52			
22	-10145	0.59			
23	-10497	0.67			
24					

WEB DATA

WEB QTY	DESCRIPTION	WELD SIZE	AXIAL	RATIO
1	L1-1/16 ROUND	2.5 X 0.230	+11966.	0.50
1	L1-1/4X1-1/4X-109	1.5 X 0.109	-1078.	0.33
1	L1-1/2X1-1/2X-170	2.5 X 0.170	+2416.	0.60
4	L1-1/2X1-1/2X-170	2.5 X 0.170	+701.	0.40
5	L1-1/2X1-1/2X-170	2.5 X 0.170	+5836.	0.79
6	L1-1/2X1-1/2X-170	2.5 X 0.170	+5275.	0.85
7	L1-1/2X1-1/2X-170	2.5 X 0.170	+649.	0.37
8	L1-1/2X1-1/2X-170	2.5 X 0.170	+4734.	0.88
9	L1-1/2X1-1/2X-170	2.5 X 0.170	+466.	0.37
10	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
11	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
12	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
13	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
14	L1-1/2X1-1/2X-170	2.5 X 0.170	+1092.	0.37
15	L1-1/2X1-1/2X-170	2.5 X 0.170	+1974.	0.66
16	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
17	L1-1/2X1-1/2X-170	2.5 X 0.170	+1093.	0.36
18	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
19	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
20	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
21	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
22	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
23	L1-1/2X1-1/2X-170	2.5 X 0.170	+1092.	0.37
24	L1-1/2X1-1/2X-170	2.5 X 0.170	+1974.	0.66
25	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
26	L1-1/2X1-1/2X-170	2.5 X 0.170	+1093.	0.36
27	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
28	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
29	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
30	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
31	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
32	L1-1/2X1-1/2X-170	2.5 X 0.170	+1092.	0.37
33	L1-1/2X1-1/2X-170	2.5 X 0.170	+1974.	0.66
34	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
35	L1-1/2X1-1/2X-170	2.5 X 0.170	+1093.	0.36
36	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
37	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
38	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
39	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
40	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
41	L1-1/2X1-1/2X-170	2.5 X 0.170	+1092.	0.37
42	L1-1/2X1-1/2X-170	2.5 X 0.170	+1974.	0.66
43	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
44	L1-1/2X1-1/2X-170	2.5 X 0.170	+1093.	0.36
45	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
46	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
47	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
48	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
49	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
50	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
51	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
52	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
53	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
54	L1-1/2X1-1/2X-170	2.5 X 0.170	+1092.	0.37
55	L1-1/2X1-1/2X-170	2.5 X 0.170	+1974.	0.66
56	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
57	L1-1/2X1-1/2X-170	2.5 X 0.170	+1093.	0.36
58	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
59	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
60	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
61	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
62	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
63	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
64	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
65	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
66	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
67	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
68	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
69	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
70	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
71	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
72	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
73	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
74	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
75	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
76	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
77	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
78	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
79	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
80	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
81	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
82	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
83	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
84	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
85	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
86	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
87	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
88	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
89	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
90	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
91	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
92	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
93	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
94	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
95	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
96	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
97	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
98	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
99	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
100	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
101	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
102	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
103	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
104	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
105	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
106	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
107	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
108	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
109	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
110	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
111	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
112	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
113	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
114	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
115	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
116	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
117	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
118	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
119	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
120	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
121	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
122	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
123	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
124	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
125	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
126	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
127	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
128	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
129	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
130	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
131	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
132	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
133	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
134	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
135	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
136	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
137	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
138	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
139	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
140	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
141	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
142	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
143	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
144	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
145	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
146	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
147	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
148	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
149	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
150	L1-1/2X1-1/2X-170	2.5 X 0.170	+2760.	0.92
151	L1-1/2X1-1/2X-170	2.5 X 0.170	+3708.	0.69
152	L1-1/2X1-1/2X-170	2.5 X 0.170	+3224.	0.52
153	L1-1/2X1-1/2X-170	2.5 X 0.170	+645.	0.37
15				



APPLIED LOADS

(D)Dead (Lr)Roof Live
 *** UNFACTORED UNIFORM LOADS (PLF) ***
 MAIN DESIG: 245 UNFACTORED TOTAL / 141 DEFL L/L7/5/R
 START LENGTH
 0- 0 0/0 50- 0 0/0
 LOAD COMBINATIONS
 1=1.0D+1.0LT 2=0.5D+1.0W 3=0.78D+0.75W

DEFLECTION DATA

DEFLECTION -- MAINSPAN --
 LIMITS (L/360) F --
 MAXIMA -1.60

ADDITIONAL DESIGN DATA

LOAD COMBINATIONS FROM: IBC 2018
 JOIST DESIGNED WITH: ASD
 JOIST IXX DEV = 479. IN^4 JOIST EFF. DEPTH= 28.89 IN
 ALLOW LYY STRESS SLENDER
 TOP CHORD= 4.4 FT 16.4 FT
 BOT CHORD= 24.4 FT
 TOP CHORD BRIDGING REQ= 2 ROWS HORIZ., 1 ROW BOLTED-EX'
 BOT CHORD BRIDGING REQ= 3 ROWS
 MAX LE END REACTION= 6084 lbs
 MAX RE END REACTION= 6084 lbs
 STANDARD SJI CAMBER= 1 0/0''

CHORD DATA

MEM	TC	REQ AXIAL	MP	RATIO	MP	RATIO	MP	RATIO
1	1	10539	0.67	0.83	18386	0.68	0.35	
2	3	14935	0.52	0.51	24087	0.93	0.76	
3	4	14935	0.58	0.50	28158	0.98	0.89	
4	2	2141	0.77	0.71	30600	0.98	0.96	
5	5	26326	0.80	0.87	30600	0.98	0.96	
6	7	26326	0.85	0.87	28158	0.93	0.89	
7	8	29582	0.89	0.98	24087	0.83	0.76	
8	9	29582	0.91	0.98	18386	0.68	0.58	
9	10	32111	0.93	0.95	11031	0.47	0.35	
10	11	32111	0.93	0.95				
11	12	32111	0.93	0.95				
12	13	32111	0.93	0.95				
13	14	32111	0.93	0.95				
14	15	29582	0.91	0.98				
15	16	29582	0.89	0.98				
16	17	26326	0.85	0.87				
17	18	26326	0.90	0.97				
18	19	2141	0.67	0.71				
19	20	14935	0.58	0.50				
20	21	14935	0.52	0.51				
21	22	10539	0.67	0.83				
22	23	10539	0.52	0.51				
23	24	10539	0.52	0.51				
24	25	10539	0.52	0.51				

W2 controls mat'l size reduced

WEB DATA

MEM	QTY	DESCRIPTION	WELD SIZE	AXIAL	RATIO
1	1	3/4 ROUND	2.9 X 0.200	12003.	1.01
2	1	L1-1/4X1-1/4X-109	2.9 X 0.190	5999.	0.37
3	1	L1-1/4X1-1/4X-109	4.0 X 0.170	2437.	0.82
4	1	L1-1/4X1-1/4X-109	4.0 X 0.170	702.	0.40
5	4	L1-1/2X1-1/2X-170	1.5 X 0.109	5846.	0.79
6	7	L1-1/2X1-1/2X-170	2.3 X 0.170	5284.	0.85
7	1	L1-1/2X1-1/2X-170	1.5 X 0.109	650.	0.37
8	1	L1-1/2X1-1/2X-170	2.6 X 0.123	474.	0.88
9	1	L1-1/2X1-1/2X-170	1.5 X 0.109	646.	0.87
10	1	L1-1/2X1-1/2X-170	2.0 X 0.123	3714.	0.69
11	1	L1-1/2X1-1/2X-170	1.5 X 0.109	3230.	0.52
12	1	L1-1/4X1-1/4X-109	1.7 X 0.109	2764.	0.37
13	1	L1-1/4X1-1/4X-109	1.5 X 0.109	1093.	0.37
14	1	L1-1/4X1-1/4X-109	1.5 X 0.109	1977.	0.66
15	1	L1-1/4X1-1/4X-109	1.5 X 0.109	1977.	0.66
16	1	L1-1/4X1-1/4X-109	1.5 X 0.109	646.	0.37
17	1	L1-1/4X1-1/4X-109	1.5 X 0.109	1095.	0.36
18	1	L1-1/4X1-1/4X-109	1.7 X 0.109	2764.	0.37
19	1	L1-1/4X1-1/4X-109	2.0 X 0.109	390.	0.52
20	1	L1-1/4X1-1/4X-109	2.0 X 0.109	390.	0.52
21	1	L1-1/2X1-1/2X-123	1.5 X 0.109	3714.	0.69
22	1	L1-1/2X1-1/2X-123	1.5 X 0.109	646.	0.37
23	1	L1-1/2X1-1/2X-123	2.6 X 0.123	4218.	0.68
24	1	L1-1/2X1-1/2X-123	2.6 X 0.123	4741.	0.88
25	1	L1-1/2X1-1/2X-170	1.5 X 0.109	650.	0.37
26	1	L1-1/2X1-1/2X-170	2.3 X 0.170	5846.	0.79
27	1	L1-1/2X1-1/2X-170	1.5 X 0.109	702.	0.40
28	1	L1-1/4X1-1/4X-109	4.0 X 0.109	6437.	0.82
29	1	L1-1/4X1-1/4X-109	2.0 X 0.170	5113.	0.63
30	1	L1-1/4X1-1/4X-109	2.0 X 0.170	1029.	0.33
31	1	L1-1/4X1-1/4X-109	2.9 X 0.200	12003.	1.01

WEBS FY= 50 KSI

STRESS ANALYSIS - PAGE 1



NEW MILLENNIUM
A Steel Dynamics Company

Job Number: 00-0-0511	Job Name: PHIL - SHOPORDERS	Date Run: 4/17/2024 10:00:20 AM
Location: ,	Joist Description: Short Span Crimp 30K162.8/162.8	Mark: CKUBI2

Geometry

Base Length: 50-0	Working Length: 49-8	Joist Depth: 30.00	Effective Depth: 28.89	BC Panel Length: 10 @ 4-0	Shape: Parallel Chords	TC Slope: 0.0000
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Variable	Left End	Right End	
BC Panel	5-0	5-0	
TC Panel	3-7	3-7	
First Half	2-0	2-0	
First Diag.	7-0	7-0	
Depth	30.00	30.00	
Trib Width	0-0	0-0	

Loads

Load Type	Category	Load1	Load2	Position	Direction	Loc/Begin	Sp/End	Reference
Uniform (plf)	LL	162.80	162.80	TC	+	0-0	50-0	L-BL

Stress Analysis Summary

Int. Panel TC: 24.00	Max Panel BC: 48.00	Reaction LE: 4,042.87	Reaction RE: 4,042.87	Minimum Shear: 1,010.72	Max TC Comp.: 20,853.66	Max BC Tension: 20,718.40
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Member	TC Tension	TC Compression	BC Tension	BC Compression	Web Tension	Web Comp.	Web Length	PP Dist.
W2	0.00	7,559.11	0.00	0.00	8,444.73	0.00	64.80	0-2
V1S	0.00	7,231.76	0.00	0.00	0.00	683.21	33.52	3-7
W3	0.00	7,231.76	9,897.53	0.00	0.00	4,270.50	37.56	5-0
W4	0.00	12,196.96	9,897.53	0.00	3,884.48	0.00	37.56	7-0
W5	0.00	12,196.96	14,225.87	0.00	0.00	3,511.23	37.56	9-0
W6	0.00	15,984.27	14,225.87	0.00	3,150.77	0.00	37.56	11-0
W7	0.00	15,984.27	17,472.13	0.00	0.00	2,803.10	37.56	13-0
W8	0.00	18,689.49	17,472.13	0.00	2,468.21	29.52	37.56	15-0
W9	0.00	18,689.49	19,636.31	0.00	249.35	2,146.11	37.56	17-0
W10	0.00	20,312.61	19,636.31	0.00	1,836.79	481.96	37.56	19-0
W11	0.00	20,312.61	20,718.40	0.00	727.35	1,540.25	37.56	21-0
W12	0.00	20,853.66	20,718.40	0.00	1,314.05	985.54	37.56	23-0
W12	0.00	20,853.66	20,718.40	0.00	1,314.05	985.54	37.56	25-0
W11	0.00	20,312.61	20,718.40	0.00	727.35	1,540.25	37.56	27-0
W10	0.00	20,312.61	19,636.31	0.00	1,836.79	481.96	37.56	29-0
W9	0.00	18,689.48	19,636.31	0.00	249.35	2,146.11	37.56	31-0
W8	0.00	18,689.48	17,472.14	0.00	2,468.21	29.52	37.56	33-0
W7	0.00	15,984.27	17,472.14	0.00	0.00	2,803.10	37.56	35-0
W6	0.00	15,984.27	14,225.88	0.00	3,150.77	0.00	37.56	37-0
W5	0.00	12,196.96	14,225.88	0.00	0.00	3,511.23	37.56	39-0
W4	0.00	12,196.96	9,897.53	0.00	3,884.48	0.00	37.56	41-0
W3	0.00	7,231.76	9,897.53	0.00	0.00	4,270.50	37.56	43-0
V1S	0.00	7,231.76	0.00	0.00	0.00	683.21	33.52	46-5
W2	0.00	7,559.11	0.00	0.00	8,444.73	0.00	64.80	45-0

Standard Verticals

Member	Position	Max Tension	Max Comp.	Length
V2	Interior	0.00	429.87	28.89

STRESS ANALYSIS - PAGE 2



Job Number: 00-0-0511	Job Name: PHIL - SHOPORDERS	Date Run: 4/17/2024 10:00:20 AM
Location: ,	Joist Description: Short Span Crimp 30K162.8/162.8	Mark: CKUBI2

Chord Properties

Chord	Area	Rx	Rz	Ryy	Y	Ix	Q	Material
TC	0.6209	0.6011	0.3559	1.2877	0.5763	0.2243	1.0000	A34A = 1.938 x 1.938 x 0.176
BC	0.5181	0.5633	0.3325	1.2357	0.5373	0.1644	1.0000	A30A = 1.813 x 1.813 x 0.157

Axial and Bending Analysis

K: 0.75	Fy: 50,000.00	Fb: 30,000.00	Mom of Inertia: 472.11	LL 360: 143.96	LL 240: 215.94	Max Bridg TC: 17-3 1/8	Max Bridg BC: 24-8 1/2
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Top Chord Check	End Panel LE	First Panel LE	Interior Panel	First Panel RE	End Panel RE	Gap Between Chords: 1.1250
Length	41.00	41.00	24.00	41.00	41.00	Min Weld Len 2X: 0.5000
Bending Load	162.80	162.80	162.80	162.80	162.80	Max Load Fillers TC: 33,946.65
Axial Load	7,559.11	7,231.76	20,853.66	7,231.76	7,559.11	Max Load no Fillers TC: 30,599.07
fa	6,087.22	5,823.61	16,793.09	5,823.61	6,087.22	TC OAL/Ryy: 462.85
Maximum K L/r	115.20	115.20	50.58	115.20	115.20	BC OAL/Ryy: 482.33
Fcr	18,914.09	18,914.09	41,470.98	18,914.09	18,914.09	BC Stress: 0.67
Fa	11,348.46	11,348.46	24,882.59	11,348.46	11,348.46	BC L/Rz: 144.3609
F'e	61,521.02	61,521.02	319,187.78	61,521.02	61,521.02	TC Shear Stress: 8,744.15
Cm	0.9505	0.9527	0.9647	0.9527	0.9505	BC Shear Stress: 10,675.04
Panel Point Moment	2,532.54	2,532.54	651.20	2,532.54	2,532.54	
Mid Panel Moment	1,689.77	948.11	325.60	948.11	1,689.77	
Panel Point fb	7,687.38	7,687.38	1,976.68	7,687.38	7,687.38	
Mid Panel fb	2,170.79	1,218.00	418.29	1,218.00	2,170.79	
Fillers	0	0	0	0	0	
Panel Point Stress	13,774.60	13,510.99	18,769.77	13,510.99	13,774.60	
Mid Panel Stress	0.6096	0.5540	0.6880	0.5540	0.6096	

Web Design

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
W2	8,444.73	12,967.80	0.00	3,733.26	3.79 x 0.150	1	C28AA = 1.125 x 1.347 x 0.150
* W3 *	0.00	9,017.86	4,270.50	4,270.22	2.50 x 0.115	1	C18AA = 1.125 x 1.012 x 0.115
W4	3,884.48	7,872.16	0.00	3,754.09	2.52 x 0.105	1	C16AA = 1.125 x 0.943 x 0.105
W5	0.00	10,920.32	3,511.23	5,314.19	2.00 x 0.134	1	C22AA = 1.125 x 1.086 x 0.134
W6	3,150.77	5,613.92	0.00	1,606.83	2.36 x 0.090	1	C12AA = 1.125 x 0.716 x 0.090
W7	0.00	9,017.86	2,803.10	4,270.22	2.00 x 0.115	1	C18AA = 1.125 x 1.012 x 0.115
W8	2,468.21	4,784.80	29.52	1,334.40	2.17 x 0.077	1	C10AA = 1.125 x 0.699 x 0.077
W9	249.35	7,872.16	2,146.11	3,754.09	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x 0.105
W10	1,836.79	4,784.80	481.96	1,334.40	2.10 x 0.077	1	C10AA = 1.125 x 0.699 x 0.077
W11	727.35	7,872.16	1,540.25	3,754.09	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x 0.105
W12	1,314.05	5,613.92	985.54	1,606.83	2.00 x 0.090	1	C12AA = 1.125 x 0.716 x 0.090
W12	1,314.05	5,613.92	985.54	1,606.83	2.00 x 0.090	1	C12AA = 1.125 x 0.716 x 0.090
W11	727.35	7,872.16	1,540.25	3,754.09	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x 0.105
W10	1,836.79	4,784.80	481.96	1,334.40	2.10 x 0.077	1	C10AA = 1.125 x 0.699 x 0.077
W9	249.35	7,872.16	2,146.11	3,754.09	2.00 x 0.105	1	C16AA = 1.125 x 0.943 x 0.105
W8	2,468.21	4,784.80	29.52	1,334.40	2.17 x 0.077	1	C10AA = 1.125 x 0.699 x 0.077
W7	0.00	9,017.86	2,803.10	4,270.22	2.00 x 0.115	1	C18AA = 1.125 x 1.012 x 0.115
W6	3,150.77	5,613.92	0.00	1,606.83	2.36 x 0.090	1	C12AA = 1.125 x 0.716 x 0.090
W5	0.00	10,920.32	3,511.23	5,314.19	2.00 x 0.134	1	C22AA = 1.125 x 1.086 x 0.134

* Continued on Next Page...

STRESS ANALYSIS - PAGE 2



NEW MILLENNIUM
A Steel Dynamics Company

<i>Job Number:</i> 00-0-0511	<i>Job Name:</i> PHIL - SHOPORDERS	<i>Date Run:</i> 4/17/2024 10:00:20 AM
<i>Location:</i> ,	<i>Joist Description:</i> Short Span Crimp 30K162.8/162.8	<i>Mark:</i> CKUBI2

Web Design, Continued...

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
W4	3,884.48	7,872.16	0.00	3,754.09	2.52 x 0.105	1	C16AA = 1.125 x 0.943 x 0.105
* W3 *	0.00	9,017.86	4,270.50	4,270.22	2.50 x 0.115	1	C18AA = 1.125 x 1.012 x 0.115
W2	8,444.73	12,967.80	0.00	3,733.26	3.79 x 0.150	1	C28AA = 1.125 x 1.347 x 0.150
V1	0.00	4,784.80	683.21	1,675.30	2.00 x 0.077	1	C10AA = 1.125 x 0.699 x 0.077
V2	0.00	4,784.80	429.87	2,165.86	2.00 x 0.077	1	C10AA = 1.125 x 0.699 x 0.077

STRESS ANALYSIS - PAGE 3



NEW MILLENNIUM
A Steel Dynamics Company

Job Number: 00-0-0511	Job Name: PHIL - SHOPORDERS	Date Run: 4/17/2024 10:00:20 AM
Location: ,	Joist Description: Short Span Crimp 30K162.8/162.8	Mark: CKUBI2

TCX Design

967 TCX Left		TCX Right	
TCX Length	0-0	TCX Length	0-0
TCX Type	R	TCX Type	R
TCX Depth	2 1/2	TCX Depth	2 1/2
BPL Length	0-4	BPL Length	0-4
Clear Bearing	0-4 3/8	Clear Bearing	0-4 3/8
BPL Material: 1714 = 1 3/4 x 1 3/4 x 0.143		BPL Material: 1714 = 1 3/4 x 1 3/4 x 0.143	
Total Load	162.80	Total Load	162.80
Reqd TL Def L/80	0.00	Reqd TL Def L/80	0.00
Live Load	162.80	Live Load	162.80
Reqd LL Def L/120	0.00	Reqd LL Def L/120	0.00
Section Modulus	0.0000	Section Modulus	0.0000
Reqd SM	0.0000	Reqd SM	0.0000
Mom of Inertia	0.0000	Mom of Inertia	0.0000
Reqd MI	0.0000	Reqd MI	0.0000
Seat Type: Lapped		Seat Type: Lapped	

Load Combinations

- | | |
|--|--|
| Case 1: DL
Case 2a: LL
Case 2b: SL
Case 3a: DL+CL+TL+LL
Case 3b: DL+CL+TL+SL
Case 3c: DL+CL+TL+LL+FEM
Case 3d: DL+CL+TL+SL+FEM
Case 3e: DL+CL+TL+LL
Case 3f: DL+CL+TL+SL
Case 4a: DL+WL+AX
Case 4b: DL+WL-AX
Case 4c: DL+WL+AX+IP
Case 4d: DL+WL-AX+IP
Case 4e: DL+SM+AX
Case 4f: DL+SM-AX
Case 5a: 0.6(DL)+WL+AX
Case 5b: 0.6(DL)+WL-AX
Case 5c: 0.6(DL)+WL+AX+IP
Case 5d: 0.6(DL)+WL-AX+IP
Case 5e: 0.6(DL)+WL+AX+SM
Case 5f: 0.6(DL)+WL-AX+SM
Case 6a: DL+CL+0.85(TL)+WL+AX
Case 6b: DL+CL+0.85(TL)+WL-AX
Case 6c: DL+CL+0.85(TL)+WL+C+AX+IP | Case 6d: DL+CL+0.85(TL)+WL+C-AX+IP
Case 6e: DL+CL+0.85(TL)+WL+AX+IP
Case 6f: DL+CL+0.85(TL)+WL-AX+IP
Case 6g: DL+CL+0.85(TL)+SM+AX
Case 6h: DL+CL+0.85(TL)+SM-AX
Case 7a: DL+CL+0.85(TL)+0.75(WL+AX+LL)
Case 7b: DL+CL+0.85(TL)+0.75(WL-AX+LL)
Case 7c: DL+CL+0.85(TL)+0.75(WL+C+AX+LL+IP)
Case 7d: DL+CL+0.85(TL)+0.75(WL+C-AX+LL+IP)
Case 7e: DL+CL+0.85(TL)+0.75(WL+AX+LL+IP)
Case 7f: DL+CL+0.85(TL)+0.75(WL-AX+LL+IP)
Case 7g: DL+CL+0.85(TL)+0.75(SM+AX+LL)
Case 7h: DL+CL+0.85(TL)+0.75(SM-AX+LL)
Case 8a: DL+CL+0.85(TL)+0.75(WL+AX+SL)
Case 8b: DL+CL+0.85(TL)+0.75(WL-AX+SL)
Case 8c: DL+CL+0.85(TL)+0.75(WL+C+AX+SL+IP)
Case 8d: DL+CL+0.85(TL)+0.75(WL+C-AX+SL+IP)
Case 8e: DL+CL+0.85(TL)+0.75(WL+AX+SL+IP)
Case 8f: DL+CL+0.85(TL)+0.75(WL-AX+SL+IP)
Case 8g: DL+CL+0.85(TL)+0.75(WL+AX+SL+SM)
Case 8h: DL+CL+0.85(TL)+0.75(WL-AX+SL+SM)
Case 9a: 1.2(DL)+0.5(LL)+0.8(TL)+SM+AX+FEM
Case 9b: 1.2(DL)+0.5(LL)+0.8(TL)+SM-AX+FEM |
|--|--|

STRESS ANALYSIS - PAGE 1



NEW MILLENNIUM
A Steel Dynamics Company

Job Number: 00-0-0511	Job Name: PHIL - SHOPORDERS	Date Run: 5/13/2024 4:53:19 PM
Location: ,	Joist Description: Short Span Crimp 30K152.5/152.5	Mark: HKUBI

Geometry

Base Length: 50-0	Working Length: 49-8	Joist Depth: 30.00	Effective Depth: 28.88	BC Panel Length: 11 @ 4-0	Shape: Parallel Chords	TC Slope: 0.0000
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Variable	Left End	Right End
BC Panel	4-7	4-7
TC Panel	3-7	3-7
First Half	0-5	0-5
First Diag.	5-0	5-0
Depth	30.00	30.00
Trib Width	0-0	0-0

Loads

Load Type	Category	Load1	Load2	Position	Direction	Loc/Begin	Sp/End	Reference
Uniform (plf)	LL	152.50	152.50	TC	+	0-0	50-0	L-BL

Stress Analysis Summary

Int. Panel TC: 24.00	Max Panel BC: 48.00	Reaction LE: 3,787.08	Reaction RE: 3,787.08	Minimum Shear: 946.77	Max TC Comp.: 19,412.29	Max BC Tension: 19,539.03
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Member	TC Tension	TC Compression	BC Tension	BC Compression	Web Tension	Web Comp.	Web Length	PP Dist.
W2	0.00	6,472.01	0.00	0.00	7,370.45	0.00	60.36	0-2
V1S	0.00	6,318.87	0.00	0.00	0.00	431.45	31.27	3-7
W3	0.00	6,318.87	6,865.63	0.00	0.00	3,205.00	29.31	4-7
W4	0.00	9,273.58	6,865.63	0.00	4,000.71	0.00	37.55	5-0
W5	0.00	9,273.58	11,428.06	0.00	0.00	3,639.07	37.55	7-0
W6	0.00	13,329.07	11,428.06	0.00	3,289.41	0.00	37.55	9-0
W7	0.00	13,329.07	14,976.60	0.00	0.00	2,951.72	37.55	11-0
W8	0.00	16,370.68	14,976.60	0.00	2,626.01	0.00	37.55	13-0
W9	0.00	16,370.68	17,511.29	0.00	27.66	2,312.28	37.55	15-0
W10	0.00	18,398.42	17,511.29	0.00	2,010.53	233.59	37.55	17-0
W11	0.00	18,398.42	19,032.09	0.00	451.51	1,720.75	37.55	19-0
W12	0.00	19,412.29	19,032.09	0.00	1,442.95	681.40	37.55	21-0
W13	0.00	19,412.29	19,539.03	0.00	923.27	1,231.03	37.55	23-0
W13	0.00	19,412.29	19,539.03	0.00	923.27	1,231.03	37.55	25-0
W12	0.00	19,412.29	19,032.09	0.00	1,442.95	681.40	37.55	27-0
W11	0.00	18,398.42	19,032.09	0.00	451.51	1,720.75	37.55	29-0
W10	0.00	18,398.42	17,511.28	0.00	2,010.53	233.59	37.55	31-0
W9	0.00	16,370.68	17,511.28	0.00	27.66	2,312.28	37.55	33-0
W8	0.00	16,370.68	14,976.61	0.00	2,626.01	0.00	37.55	35-0
W7	0.00	13,329.06	14,976.61	0.00	0.00	2,951.72	37.55	37-0
W6	0.00	13,329.06	11,428.06	0.00	3,289.41	0.00	37.55	39-0
W5	0.00	9,273.58	11,428.06	0.00	0.00	3,639.07	37.55	41-0
W4	0.00	9,273.58	6,865.63	0.00	4,000.71	0.00	37.55	43-0
W3	0.00	6,318.88	6,865.63	0.00	0.00	3,205.00	29.31	45-0
V1S	0.00	6,318.88	0.00	0.00	0.00	431.45	31.27	46-5
W2	0.00	6,472.01	0.00	0.00	7,370.45	0.00	60.36	45-5

Standard Verticals

Member	Position	Max Tension	Max Comp.	Length
V2	Interior	0.00	402.06	28.88

STRESS ANALYSIS - PAGE 2



Job Number: 00-0-0511	Job Name: PHIL - SHOPORDERS	Date Run: 5/13/2024 4:53:19 PM
Location: ,		Joist Description: Short Span Crimp 30K152.5/152.5
		Mark: HKUBI

Chord Properties

Chord	Area	Rx	Rz	Ryy	Y	Ix	Q	Material
TC	0.6254	0.6208	0.3951	1.2830	0.5603	0.2410	0.9528	2016 = 2 x 2 x 0.163
BC	0.6254	0.6208	0.3951	1.2830	0.5603	0.2410	0.9528	2016 = 2 x 2 x 0.163

Axial and Bending Analysis

K: 0.75	Fy: 50,000.00	Fb: 30,000.00	Mom of Inertia: 522.56	LL 360: 159.35	LL 240: 239.02	Max Bridg TC: 17-2 3/8	Max Bridg BC: 25-7 7/8
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Top Chord Check	End Panel LE	First Panel LE	Interior Panel	First Panel RE	End Panel RE	Gap Between Chords: 1.1250
Length	41.00	17.00	24.00	17.00	41.00	Min Weld Len 2X: 0.5000
Bending Load	152.50	152.50	152.50	152.50	152.50	Max Load Fillers TC: 33,255.84
Axial Load	6,472.01	6,318.87	19,412.29	6,318.88	6,472.01	Max Load no Fillers TC: 30,690.51
fa	5,174.30	5,051.87	15,519.90	5,051.87	5,174.30	TC OAL/Ryy: 464.54
Maximum K L/r	103.77	43.03	45.56	43.03	103.77	BC OAL/Ryy: 464.54
Fcr	22,499.07	41,875.14	41,226.14	41,875.14	22,499.07	BC Stress: 0.52
Fa	13,499.44	25,125.08	24,735.69	25,125.08	13,499.44	BC L/Rz: 121.4882
F'e	65,619.59	381,683.47	340,452.22	381,683.47	65,619.59	TC Shear Stress: 8,204.01
Cm	0.9606	0.9934	0.9695	0.9934	0.9606	BC Shear Stress: 8,054.47
Panel Point Moment	2,009.45	2,009.45	610.00	2,009.45	2,009.45	
Mid Panel Moment	1,703.82	1,434.01	305.00	1,434.01	1,703.82	
Panel Point fb	6,002.08	6,002.07	1,822.03	6,002.07	6,002.08	
Mid Panel fb	1,980.60	4,283.28	354.55	4,283.28	1,980.60	
Fillers	0	0	0	0	0	
Panel Point Stress	11,176.37	11,053.94	17,341.93	11,053.94	11,176.38	
Mid Panel Stress	0.4514	0.3364	0.6390	0.3364	0.4514	

Web Design

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
W2	7,370.45	26,972.16	0.00	5,102.58	2.62 x 0.245	1	R112 = round 1 1/8
* W3 *	0.00	7,857.08	3,205.00	3,203.90	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W4	4,000.71	7,857.08	0.00	2,593.86	2.47 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W5	0.00	13,296.14	3,639.07	5,819.16	2.00 x 0.155	1	1515 = 1 1/2 x 1 1/2 x 0.155
W6	3,289.41	7,857.08	0.00	2,593.86	2.43 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W7	0.00	10,670.07	2,951.72	4,097.33	2.00 x 0.123	1	1512 = 1 1/2 x 1 1/2 x 0.123
W8	2,626.01	7,857.08	0.00	2,593.86	2.43 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W9	27.66	10,670.07	2,312.28	4,097.33	2.00 x 0.123	1	1512 = 1 1/2 x 1 1/2 x 0.123
W10	2,010.53	7,857.08	233.59	2,593.86	2.43 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W11	451.51	7,857.08	1,720.75	2,593.86	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W12	1,442.95	7,857.08	681.40	2,593.86	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W13	923.27	7,857.08	1,231.03	2,593.86	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W13	923.27	7,857.08	1,231.03	2,593.86	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W12	1,442.95	7,857.08	681.40	2,593.86	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W11	451.51	7,857.08	1,720.75	2,593.86	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W10	2,010.53	7,857.08	233.59	2,593.86	2.43 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W9	27.66	10,670.07	2,312.28	4,097.33	2.00 x 0.123	1	1512 = 1 1/2 x 1 1/2 x 0.123
W8	2,626.01	7,857.08	0.00	2,593.86	2.43 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W7	0.00	10,670.07	2,951.72	4,097.33	2.00 x 0.123	1	1512 = 1 1/2 x 1 1/2 x 0.123

* Continued on Next Page...

STRESS ANALYSIS - PAGE 2



NEW MILLENNIUM
A Steel Dynamics Company

<i>Job Number:</i> 00-0-0511	<i>Job Name:</i> PHIL - SHOPORDERS	<i>Date Run:</i> 5/13/2024 4:53:19 PM
<i>Location:</i> ,	<i>Joist Description:</i> Short Span Crimp 30K152.5/152.5	<i>Mark:</i> HKUBI

Web Design, Continued...

Member	Web Tension	Allow Tension	Web Comp	Allow Comp	Weld	Qty	Material
W6	3,289.41	7,857.08	0.00	2,593.86	2.43 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W5	0.00	13,296.14	3,639.07	5,819.16	2.00 x 0.155	1	1515 = 1 1/2 x 1 1/2 x 0.155
W4	4,000.71	7,857.08	0.00	2,593.86	2.47 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
* W3 *	0.00	7,857.08	3,205.00	3,203.90	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
W2	7,370.45	26,972.16	0.00	5,102.58	2.62 x 0.245	1	R112 = round 1 1/8
V1	0.00	7,857.08	431.45	3,061.03	2.00 x 0.109	1	1210 = 1 1/4 x 1 1/4 x 0.109
V2	0.00	6,213.91	402.06	1,432.68	2.00 x 0.109	1	1010 = 1 x 1 x 0.109

STRESS ANALYSIS - PAGE 3



NEW MILLENNIUM
A Steel Dynamics Company

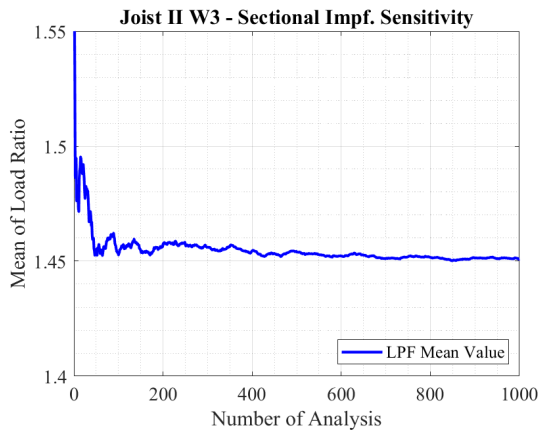
Job Number: 00-0-0511	Job Name: PHIL - SHOPORDERS	Date Run: 5/13/2024 4:53:19 PM
Location: ,	Joist Description: Short Span Crimp 30K152.5/152.5	Mark: HKUBI

TCX Design

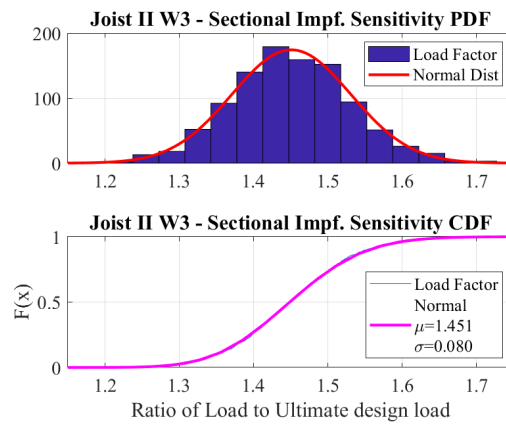
971 TCX Left		TCX Right	
TCX Length	0-0	TCX Length	0-0
TCX Type	R	TCX Type	R
TCX Depth	2 1/2	TCX Depth	2 1/2
BPL Length	0-4	BPL Length	0-4
Clear Bearing	0-4 1/2	Clear Bearing	0-4 5/8
BPL Material: 1714 = 1 3/4 x 1 3/4 x 0.143		BPL Material: 1714 = 1 3/4 x 1 3/4 x 0.143	
Total Load	152.50	Total Load	152.50
Reqd TL Def L/80	0.00	Reqd TL Def L/80	0.00
Live Load	152.50	Live Load	152.50
Reqd LL Def L/120	0.00	Reqd LL Def L/120	0.00
Section Modulus	0.0000	Section Modulus	0.0000
Reqd SM	0.0000	Reqd SM	0.0000
Mom of Inertia	0.0000	Mom of Inertia	0.0000
Reqd MI	0.0000	Reqd MI	0.0000
Seat Type: Lapped		Seat Type: Lapped	

Load Combinations

- | | |
|---|---|
| <p>Case 1: DL
 Case 2a: LL
 Case 2b: SL
 Case 3a: DL+CL+TL+LL
 Case 3b: DL+CL+TL+SL
 Case 3c: DL+CL+TL+LL+FEM
 Case 3d: DL+CL+TL+SL+FEM
 Case 3e: DL+CL+TL+LL
 Case 3f: DL+CL+TL+SL
 Case 4a: DL+WL+AX
 Case 4b: DL+WL-AX
 Case 4c: DL+WL+AX+IP
 Case 4d: DL+WL-AX+IP
 Case 4e: DL+SM+AX
 Case 4f: DL+SM-AX
 Case 5a: 0.6(DL)+WL+AX
 Case 5b: 0.6(DL)+WL-AX
 Case 5c: 0.6(DL)+WL+AX+IP
 Case 5d: 0.6(DL)+WL-AX+IP
 Case 5e: 0.6(DL)+WL+AX+SM
 Case 5f: 0.6(DL)+WL-AX+SM
 Case 6a: DL+CL+0.85(TL)+WL+AX
 Case 6b: DL+CL+0.85(TL)+WL-AX
 Case 6c: DL+CL+0.85(TL)+WL+C+AX+IP</p> | <p>Case 6d: DL+CL+0.85(TL)+WL+C-AX+IP
 Case 6e: DL+CL+0.85(TL)+WL+AX+IP
 Case 6f: DL+CL+0.85(TL)+WL-AX+IP
 Case 6g: DL+CL+0.85(TL)+SM+AX
 Case 6h: DL+CL+0.85(TL)+SM-AX
 Case 7a: DL+CL+0.85(TL)+0.75(WL+AX+LL)
 Case 7b: DL+CL+0.85(TL)+0.75(WL-AX+LL)
 Case 7c: DL+CL+0.85(TL)+0.75(WL+C+AX+LL+IP)
 Case 7d: DL+CL+0.85(TL)+0.75(WL+C-AX+LL+IP)
 Case 7e: DL+CL+0.85(TL)+0.75(WL+AX+LL+IP)
 Case 7f: DL+CL+0.85(TL)+0.75(WL-AX+LL+IP)
 Case 7g: DL+CL+0.85(TL)+0.75(SM+AX+LL)
 Case 7h: DL+CL+0.85(TL)+0.75(SM-AX+LL)
 Case 8a: DL+CL+0.85(TL)+0.75(WL+AX+SL)
 Case 8b: DL+CL+0.85(TL)+0.75(WL-AX+SL)
 Case 8c: DL+CL+0.85(TL)+0.75(WL+C+AX+SL+IP)
 Case 8d: DL+CL+0.85(TL)+0.75(WL+C-AX+SL+IP)
 Case 8e: DL+CL+0.85(TL)+0.75(WL+AX+SL+IP)
 Case 8f: DL+CL+0.85(TL)+0.75(WL-AX+SL+IP)
 Case 8g: DL+CL+0.85(TL)+0.75(WL+AX+SL+SM)
 Case 8h: DL+CL+0.85(TL)+0.75(WL-AX+SL+SM)
 Case 9a: 1.2(DL)+0.5(LL)+0.8(TL)+SM+AX+FEM
 Case 9b: 1.2(DL)+0.5(LL)+0.8(TL)+SM-AX+FEM</p> |
|---|---|



(a) PDF of LPF values



(b) Fitted distribution type for LPF results

Figure B.24: Joist II W3 cross-sectional imperfection sensitivity analyses results and fitted distribution

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